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APOLLO 12 (MISSION H-1) SPACECRAFT DISPERSION ANALYSIS VOLUME IV DESCENT AND ASCENT DISPERSION ANALYSES PART 1 - LUNAR DESCENT

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> Landing Analysis Branch MISSION PLANNING AND ANALYSIS DIVISION

> > MANNED SPACECRAFT CENTER HOUSTON, TEXAS

00/98

# MSC INTERNAL NOTE NO. 69-FM-275

# PROJECT APOLLO

# APOLLO 12 (MISSION H-1) SPACECRAFT DISPERSION ANALYSIS VOLUME IV - DESCENT AND ASCENT DISPERSION ANALYSES PART 1 - LUNAR DESCENT

By Gilbert L. Carman and Moises N. Montez Landing Analysis Branch

October 31, 1969

MISSION PLANNING AND ANALYSIS DIVISION NATIONAL AERONAUTICS AND SPACE ADMINISTRATION MANNED SPACECRAFT CENTER HOUSTON, TEXAS

Approved:

Floyd V. Bennett, Chief Landing Analysis Branch

Approved: John P Mayer, Chief

Mission Planning and Analysis Division

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# APOLLO 12 (MISSION H-1) SPACECRAFT DISPERSION ANALYSIS

VOLUME IV - DESCENT AND ASCENT DISPERSION ANALYSES

#### PART 1 - LUNAR DESCENT

By Gilbert L. Carman and Moises N. Montez

#### 1.0 SUMMARY

The results of the Apollo 12 (Mission H-1) dispersion analysis for the LM descent are presented in the form of statistical tables and 99 percent, 90 percent, and 50 percent landing dispersion ellipses. The study is based on a nonlinear Monte Carlo analysis, and 100 descents were run.

In summary, there were no violations of known systems or trajectory constraints. All 100 descents were successful. The 99 percent landing dispersion ellipse (3.2 n. mi. by l.l n. mi.) does not indicate a significant improvement from Apollo 11 because DOI execution errors that result from systems uncertainties overshadow any improvement in the orbital navigation accuracies. To determine these numbers, it was assumed that no update of the landing site vector during P63 was used and that no state vector update from the ground was incorporated post-DOI. Reduction of the accelerometer bias uncertainty and a correction to the landing site increase the probability of a pinpoint landing (i.e., a landing which occurs within a 1-km radius of the designated landing point).

A reduction in the accelerometer bias uncertainty has been confirmed since the data for this report were generated. The major effect of this reduction is a reduction in the landing dispersions (from 3.2 by l.l n. mi. to l.2 by 0.7 n. mi.). The effect of this reduction on other trajectory dispersions is minimal.

#### 2.0 INTRODUCTION

The purpose of this document is to present the technical approach assumptions and the results of the final dispersion analysis performed for the lunar descent phase of Apollo 12 (Mission H-1) as defined in reference 1. The purpose of the dispersion analysis is to assess the effects of navigation, terrain, and systems uncertainties on the probabilities for mission success and flight safety. A nonlinear Monte Carlo analysis of the mission was performed to permit inclusion of nonlinear effects so that the resultant non-Gaussian sample statistic could be computed. The covariance matrices sampled by the Monte Carlo simulation were generated by the Mathematical Physics Branch (ref. 2). Samples from the simulation were analyzed by the TRW statistical processor (ref. 3).

#### 3.0 ABBREVIATIONS

APS	ascent propulsion system
DAMP	descent ascent Monte Carlo program
DOI	descent orbit insertion
DPS	descent propulsion system
FTP	fixed throttle point
GAC	Grumman Aerospace Corporation
G&N	guidance and navigation
LAB	Landing Analysis Branch
LGC	LM guidance computer
LM	lunar module
LPD	landing point designator
LR	landing radar
PDI	powered descent initiation
PGNCS	primary guidance and navigation control subsystem
RCS	reaction control subsystem
t <sub>GO</sub>	time to go
$t_{IG}$	time of ignition
ΔV	change in velocity

# 4.0 ANALYSIS

Dispersion data for this Monte Carlo analysis were generated by the LAB DAMP program. This study considered the effects of propulsion uncertainties, landing radar errors, terrain, and terrain slope on the lunar landing trajectory from lunar orbit. Initial systems errors for each Monte Carlo cycle were selected by a random number generator. Navigation uncertainties were incorporated into the initial state vector for each cycle by sampling a covariance matrix. Statistics were generated for the dispersion data at nine points in the trajectory. A detailed description of the major points which constituted this Monte Carlo analysis is given in subsections 4.1 through 4.3.

# 4.1 Descent Trajectory and Guidance

The latest descent targeting philosophy was used to generate the desired conditions used in this study; these conditions are documented in reference 1.

The simulation was initialized over the landing site one revolution prior to landing. The sequence of events was as follows.

- a. Target the DOI burn.
- b. Coast with an ENCKE program to  $t_{TC}$  for DOI.
- c. Perform the DOI burn.
- d. Coast with an ENCKE program to PDI.
- e. Perform the powered descent.

All the navigation and guidance routines used in the simulation were acquired from reference 4 except for the ENCKE and the DOI targeting routine.

#### 4.2 Error Sources

The PGNCS errors considered in this analysis were accelerometer bias, scale factor, gyro drift, and misalinement. The 30 values for these errors were obtained from reference 5 and are listed in table I. The terrain variation model for site 7 (ref. 6) was used with a  $3\sigma$  uncertainty of  $\pm 1^{\circ}$  in terrain slope superimposed on the terrain for ranges of less than 40 kilometers. Elevation uncertainties are computed in the following manner.

If range < 40 km, use -TS \*Range If range > 40 km, use -TS \*(40 km)

where TS is the tangent of the uncertainty in the terrain slope. A positive slope is defined as one which slopes up (from the LM) toward the landing site.

The LM DPS model (Victory 7) used in this analysis is described in reference 7. It is a linear DPS engine model that uses basic acceptance test data and adjusts them to flight interface conditions. Interface conditions calculated in Victory 7 are functions of vehicle longitudinal acceleration and propellant flow rates. Engine tag values and class coefficients which were used in this analysis are documented in reference 8.

Navigation uncertainties for a position and velocity vector one revolution prior to landing were used in the form of a covariance matrix (ref. 2). These covariance matrices are listed in table II. The data presented in this table describe the uncertainty of the estimated state vector from the actual state vector. Initially, the actual state vector is assumed to be in the nominal 60-n. mi. altitude circular orbit.

Entries in the matrix are given in a UVW system which is defined as follows.

$$U = \frac{r}{|r|}$$
, vertical

 $V = W \times U$ , down range

$$W = \frac{\underline{r} \times \underline{v}}{|\underline{r} \times \underline{v}|}$$

where  $\underline{r}$  is the position vector and  $\underline{v}$  is the inertial velocity in selenocentric coordinates.

The landing radar model used in the studies for the report was the GAC mathematical model of reference 9. This model includes terrain effects and detailed track logic based on signal to noise ratio calculations. A detailed error model is also included which introduces the following error sources into the range and velocity measurements.

a. Deterministic errors

1. Terrain bias error

- 2. Preamplifier slope error
- 3. VCO drift error
- 4. Dynamic lag error
- 5. Doppler compensation error
- b. Random bias errors
  - 1. Boresight misalinement error
  - 2. Installation misalinement error
  - 3. Modulation rate error
- c. Random fluctuation errors
  - 1. Spread spectrum error
  - 2. Doppler compensation error
  - 3. Quantization error

The triaxial potential function was modified as suggested in reference 10 to obtain the R2 potential function which was used in this study.

All the parameters which are randomized during each Monte Carlo cycle are listed in table III.

## 4.3 Statistical Output

Covariance matrices were generated at landing and at 3 minutes prior to nominal PDI. The format for these matrices is the following.



# where 4 escribes the uncertainty of the actual about the reference $6 \times 6 \text{ AR}$ describes the uncertainty of the estimated about the actual

 $\frac{1}{1 \times 1}$  describes the uncertainty in weight

Statistics were computed for the parameters defined in table IV at each of the following points in the descent trajectory.

a. DOI cutoff

b. PDI minus 3 minutes

c. High gate

d. Ranges of 20 000, 10 000, 5000, and 2000 feet

e. Vertical descent initiation

f. Landing

Statistics were generated only for cases which did not violate any of the following abort criteria.

a. Propellant depletion prior to lunar landing

b. Failure to achieve landing radar altitude update initiation prior to high gate

c. Lunar landing prior to the vertical descent phase

d. Violation of the 4-second APS abort boundary (altitude versus altitude rate constraint) prior to 600-foot altitude above lunar surface

#### 5.0 DISCUSSION AND RESULTS

One hundred descents were run, and none of these violated the abort criteria defined in the preceding section. The results for the 100 successful landings are presented in the form of statistical tables and landing dispersion ellipses. This discussion includes dispersions at DOI cutoff and PDI; landing radar acquisition; throttle recovery; dispersions at high gate, glide path, and low gate; dispersions at vertical descent; pitch dispersions at landing and DPS burn time; landing dispersion ellipses, landing velocity;  $\Delta V$  and propellant dispersions; and time histories with associated 30 dispersions for selected parameters.

The summary for the statistical parameters is presented in table V while the covariance matrices which were generated in this study are presented in table VI.

# 5.1 Dispersions at DOI Cutoff

The DOI burn is well behaved, and the accuracy with which the burn is performed is acceptable to establish a safe perilune altitude at which the powered descent can be initiated. The dispersions in burn duration are attributed primarily to navigation uncertainty and accelerometer bias error. A 3 $\sigma$  variation in burn time is  $\pm 0.6$  second, and a 3 $\sigma$  variation in  $\Delta V$  is  $\pm 1.5$  fps. A 1-fps variation in  $\Delta V$  causes a variation in perilune altitude uncertainty of 0.7 n. mi. A 3 $\sigma$  variation in  $\Delta V$  would reflect an altitude uncertainty at perilune which is well within the limit of a safe perilune for performance of a powered descent. The mean and the standard deviation in the  $\Delta V$  residuals at DOI cutoff, in body coordinates, are as follows.

> $\Delta V_{x-body} = 0.09 \pm 0.04$  fps  $\Delta V_{y-body} = 0.00 \pm 0.02$  fps  $\Delta V_{z-body} = 0.00 \pm 0.02$  fps

The residuals will not be trimmed.

#### 5.2 Dispersion at PDI

No convergence problems caused by dispersions at PDI were encountered in the ignition computations. Because of systems uncertainties, the 3o dispersion in perilune altitude is 4800 feet. The 3o dispersions in vertical and horizontal velocity (at PDI minus 3 min) are  $\pm4.5$  fps and  $\pm9.0$  fps, respectively. Dispersions of this magnitude can be corrected by the G&N system and will result in a safe landing.

#### 5.3 Landing Radar Acquisition

Landing radar acquisitions of altitude and velocity data nominally occur at altitudes of 36 000 feet and 16 700 feet, respectively. The 30 high and low altitudes for landing radar altitude acquisition are 41 520 feet and 30 500 feet, respectively. The 30 high and low altitudes for velocity acquisition are 18 500 feet and 14 900 feet, respectively.

## 5.4 Throttle Recovery

Throttle recovery nominally occurs at  $t_{GO} = 180$  seconds (approximately 118 sec prior to high gate because target switch occurs when  $t_{GO} = 62$  sec). A 3 $\sigma$  high value for  $t_{GO}$  at throttle recovery is 195 seconds, and a 3 $\sigma$  low value would be 165 seconds. The shutoff value malfunction, which would reduce the  $t_{GC}$  at throttle recovery by

60 seconds, is not incorporated in these values. These statistics indicate that without a shutoff valve malfunction there will be at least a 105-second period of throttle recovery in which to meet the target conditions at high gate. A minimum throttle recovery time of 30 seconds has been shown to be adequate in previous studies.

#### 5.5 High-gate Dispersions

Nominally, high gate occurs at an altitude of 6700 feet with a flight-path angle of  $-22^{\circ}$  and a vertical velocity of -167 fps. The  $3\sigma$  high values for altitude, flight-path angle, and vertical velocity are 7750 feet,  $-28^{\circ}$ , and -200 fps, respectively. The  $3\sigma$  low values, in the same order, are 5650 feet,  $-17^{\circ}$ , and  $-13^{4}$  fps. These dispersions do not indicate a flight safety problem at high gate.

### 5.6 Glide Path

The 3 $\sigma$  altitude dispersions at ranges of 20 000 feet, 10 000 feet, 5000 feet, and 2000 feet are  $\pm$ 750 feet,  $\pm$ 546 feet,  $\pm$ 450 feet, and  $\pm$ 369 feet, respectively. These dispersions cause the approach to be outside the desired approach corridor of reference 22 [fig. 1(a)]. The approach trajectory dips into the sun angles (visibility washout) at a range of approximately 7000 feet and an altitude of 1500 feet. Altitude versus range for the nominal trajectory as well as the 3o altitude dispersions are presented in figure 1(b).

# 5.7 Low Gate (Range of 2000 ft)

Low gate occurs nominally at an altitude of 500 feet. The approach trajectory has been designed to provide a more efficient automatic trajectory and an improved redesignation capability at low gate. The statistics presented in this section were computed at a range of 2000 feet, which is approximately the range at which low gate occurs. The nominal values for horizontal velocity, vertical velocity, and pitch are 84 fps, -18 fps, and 23°, respectively. The 30 dispersion of these parameters are  $\pm 3.6$  fps,  $\pm 9$  fps, and  $\pm 0.9^{\circ}$ , respectively. These dispersions are considered to be within the capability of the pilot to perform his takeover function.

# 5.8 Vertical Descent

The nominal altitude at vertical descent initiation is 100 feet (no terrain). A 3 $\sigma$  high altitude at vertical descent initiation is 156 feet, and a 3 $\sigma$  low altitude is 48 feet. These altitudes include terrain effects and are for completely automatic landings. Terminal propellant dispersions are extremely sensitive to altitude dispersions at vertical descent initiation because of the small vertical rate. For each second of time, approximately 9 pounds of propellant is expended, and altitude is reduced by only 3 feet. Therefore, altitude dispersions are 3 lb/ft.

# 5.9 Pitch at Landing (Landing Gear Probe Contact)

The nominal pitch (from local vertical) at landing is  $0^{\circ}$ . The  $3\sigma$  low and high samples are  $-0.5^{\circ}$  and  $0.9^{\circ}$ , respectively. These values were well within the  $6^{\circ}$  constraint of reference 12.

#### 5.10 Powered Descent Burn Time

The nominal DPS burn time is 676 seconds, and there is a 99 percent probability that the time will be less than 706 seconds. The smallest sample was 642 seconds. These dispersions indicate that there is no conflict with the DPS burn time constraint, which is approximately 910 seconds.

#### 5.11 Landing Dispersion Ellipses

The current estimate of the LM landing dispersion ellipses is based on a sample size of 100 runs and is given in table VII. The 99 percent ellipse (3.2 n. mi. by l.l n. mi.) does not indicate a significant improvement from Apollo 11 because DOI execution errors that result from systems uncertainties overshadow any improvement in the orbital navigation accuracies. These numbers assume that no update of the landing site vector during P63 was used and that no state vector update from the ground was incorporated post-DOI. Reduction of the accelerometer bias and a correction to the landing site increase the probability for a pinpoint landing.

The dispersion ellipses for different 30 values for accelerometer bias as well as different navigation accuracies used with an Apollo 12 (H-1) mission timeline are presented in table VII. Also included in the table are the dispersion ellipses in which a perfect state vector update was incorporated prior to PDI. The data in table VII indicate that a reduction in the accelerometer bias increases the probability for a pinpoint landing. A state vector update prior to PDI or during P63 increases the probability even more. There is no method currently in existence that can be used to correct cross-range errors. Therefore, cross-range dispersions remain the same with or without a landing site correction. The ellipses in this case are rotated 90° primarily because of a platform misalinement which has a greater effect on the cross-range dispersions. A scatter plot of the samples and the 99 percent, 90 percent, and 50 percent dispersion ellipses are presented in figure 2(a). The dispersion ellipses for the reduced accelerometer bias  $3\sigma$  uncertainty (0.2 cm/sec<sup>2</sup>) are presented in figure 2(b).

### 5.12 Landing (Landing Gear Probe Contact) Velocity

Nominal horizontal and vertical velocities at landing are 0.008 fps and -3 fps, respectively. The  $3\sigma$  dispersions, in the same order, are  $\pm 0.6$  fps and  $\pm 0.6$  fps. No free-fall effects are reflected in these velocity uncertainties. The  $3\sigma$  velocity error ellipse is compared in figure 3 with the landing gear constraints at landing specified in reference 12.

# 5.13 $\Delta V$ and Propellant Summary

The  $\Delta V$  and propellants are summarized in this document for an automatically guided descent only; that is, manual translation and landing site redesignation (manually input) are not considered. The  $\Delta V$  and propellants required are tabulated at major event points during the descent in table VIII(a). The fuel, oxidizer, and total propellant results are derived by use of the linear propulsion system model (ref. 7). The propellant status for the total descent is presented in table VIII(b), which includes loaded propellant, propellant consumed, and usable remaining propellant. Usable remaining propellant is, by definition, the propellant remaining at landing which can be used for  $\Delta V$ . The usable remaining propellant values do not allow for system malfunctions, biases, or contingency situations (redline low-level sensor, engine valve malfunction).

### 5.14 Time Histories and Dispersions for Selected Parameters

Time histories as well as the 30 dispersions for true altitude, LPD angle, pitch, vertical velocity, glide angle, and commanded thrust are plotted in figure 4. Time histories for engine parameters and their associated dispersions were not included because they would be identical to the time histories which will appear in the LM data book (ref. 14).

# 6.0 CONCLUSIONS

There were no violations of known systems or trajectory constraints. All 100 descents were successful. The 99 percent landing dispersion ellipse (3.2 n. mi. by 1.1 n. mi.) does not indicate a significant improvement from Apollo 11 because DOI execution errors that result from systems uncertainties overshadow any improvement in the orbital navigation accuracies. To determine these numbers it was assumed that no update of the landing site vector during P63 was used and that no state vector update from the ground was incorporated post-DOI. Reduction of the accelerometer bias uncertainty and a correction to the landing site increase the probability for a pinpoint landing.

A reduction in the accelerometer bias uncertainty has been confirmed since the data for this report were generated. The major effect of this reduction is a reduction in the landing dispersions (from 3.2 by l.l n. mi. to l.2 by 0.9 n. mi.). The effect of this reduction on other trajectory dispersions is minimal.

TABLE	Τ	тмп	ERRORS
	т. <u>е</u> —	1110	THURDING

Component	3o error	Equivalent errors in program units	
Gyro misalinement	0.057 deg	0.0009948 rad	
Coasting flight gyro drift	.09 deg/hr	.436332 × 10 <sup>-6</sup> rad/sec	
Powered flight gyro drift	.3 deg/hr	$.14544 \times 10^{-5} \text{ rad/sec}$	
Accelerometer bias	.6 $cm/sec^2$	.019685 ft/sec <sup>2</sup>	
Accelerometer scale factor	300/10 <sup>6</sup>	.003	

TABLE  ${\rm I\!I}$  - Covariance matrix of navigation uncertainties^a

(a) 95 % confidence

		I				•	13	
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posterio dana di Angelesia.	0.0000000 0.0000000 0.0000000000000000	1.000000 0.000000 0.0000000 5.8225999+02			<u>й.შ000000</u> 0.9500000		0, 20000000	5, 4225999+02
	4, 6677530-04 9,5562319-02 7,3334499+01	-8,4823219-05 -7,1466230-07 1,7123640+00 0,0000000			4.9677260-04 9.5578140-02	7,3334499+61 -8,4837289-65	-7.154000-07 1.7123640+00	0+000000
	-1,2397320+02 -1,6991330+01 -2,9048970-04	-1.0190390-01 -1.1107730-01 -7.1466230-01 0.0000000			*1:2398280+02 4:2423040+00	-3,4259770-34	1,1008790-01 -7,1540000-07	1.000000.0
VARIANCE MATRIX	1.5501240,02 -8.0119659402 -4.5841160-03	2,4503470+00 1,0190390-01 -8,4823219-05 0,000000	5 % confidence	VARIANCE MATZIX	-3,5497220+02 -3,9669820+02	-5,5767810=03. 2,1004940+00	-1, 20/95/0+01 -8, 4837289405	
INPLT CO	2,0001800-01 5,3273990-01 1.0460470400	-4.9641905-03 -2.9048970-04 7.3334499+01 0.000000	(b) 55	INPUT CO	2,0890670*01 6,4432210*00	1,0450470476 15,7767810103	7, 3334499401	
	-2,5334860,04 8,8513800+05 5,3273990+05	0,000000 0,000000 0,000000 0,000000			*2,5289830+04 4,3045420+05	4 4 4 2 2 2 4 0 4 0 0 4 7 8 6 6 9 8 2 0 4 0 2 8 9 8 9 4 9 4 9 4 0 0	9.5578140.02	
-	1:40700+C5 -2:5334860+C4 2:0901800+C1	0.00000		1.		1.549720+01	4,9677265-C4	3

σzż ۶XŻ <sup>o</sup>yz ozz ٩Xż đyż σxÿ وبن σzÿ ۰xÿ ٥yý <sup>a</sup>Format for covariance matrix ° XX ٩x. σzX ۶ÿ đxz ¢yz σzz đxy °yy

đxx

TABLE III.- PARAMETERS RANDOMIZED DURING EACH MONTE CARLO CYCLE

(a) IMU

Gyro misalinement Coasting flight gyro drift Powered flight gyro drift Accelerometer bias Accelerometer scale factor

(b) LR

Boresight misalinement error Installation misalinement error Modulation rate error Spread spectrum error Doppler compensation error Quantization error

(c) Engine model and propulsion system

Thrust

Specific impulse Mixture ratio Pressure drop ratio across the injector Loaded fuel Loaded oxidizer Dry weight of LM + APS propellant

(d) State vector

Navigated position and velocity vectors

(e) Terrain

Terrain slope

# TABLE IV.- DEFINITION OF SYMBOLS

- FPAG Estimated flight-path angle, deg
- FPAGT True flight-path angle, deg
- HORV Estimated horizontal velocity, fps
- HORVT True horizontal velocity, fps
- HDOT Estimated vertical velocity, fps
- VERVT True vertical velocity, fps
- PVRT Estimated pitch from vertical, deg
- PVRTT True pitch from vertical, deg
- HEST Estimated altitude, ft
- HTRU Altitude above the local terrain, ft
- RANGE Z component of LM position vector in the guidance coordinate system, ft
- HVIS True altitude at landing sight visibility acquisition, ft
- HORZ True altitude at horizon visibility acquisition, ft
- LATLM Latitude of LM, deg
- LONLM Longitude of LM, deg
- HLRA True altitude at landing radar altitude acquisition, ft
- HLRV True altitude at landing radar velocity acquisition, ft
- ELANG Glide angle, deg
- ELAS LPD angle, navigated, deg
- HPER LM perilune altitude, ft
- HAPO LM apolune altitude, ft
- ECC Eccentricity, n.d.

# TABLE IV.- DEFINITION OF SYMBOLS - Concluded

TFIG	Total DPS burn time, sec
BURN	Burn time at FTP (fixed throttle point), sec
TFXA	TGO at throttle down time, sec
WT	Weight deviation from nominal, lb
TTVIS	Total landing sight visibility time, sec
WPR	DPS propellant remaining, lb
WF	DPS fuel remaining, lb
WOX	DPS oxidizer remaining, lb
FC	Thrust commanded by the guidance, lb
THF	DPS thrust, 1b
PIO	Oxidizer interface pressure, lb
PIF	Fuel interface pressure, lb
DWO	Oxidizer flow rate, lb/sec
DWF	Fuel flow rate, lb/sec
RE	Mixture ratio, n.d.
REE	Effective mixture ratio, n.d.
CISP	Specific impulse, sec
EISP	Effective specific impulse, sec

Total actual accumulated  $\Delta V,\ {\rm fps}$ 

DEVMT

<b>NRAMETERS</b>	
đ	
STATISTICAL	
Щ	
ABLE Y SUMMARY	
	TABLE Y SUMMARY OF STATISTICAL PARAMETERS

Descent orbit insertion cutoff

	1,0591442482 3,6340807-05 0,000000 5,29159864+03 0,000000 0,000000	1.0565901402 3.6343764405 9.6840800 5.2916418403 0.0000000 0.0000000	1,2022115400 5,60,46529402 0,0000000 2,5495097400 0,0000000 0,0000000	6.2881044-01 5.1248875404 5.1248875404 5.5749514403 0.000000 0.0000000	8,2946678+01 5,11075404 6,0200000 5,5767813403 0,0000000 0,0000000	1.2583462+00 1.7814844+02 1.7814844+02 0.0000000 3.6413812+09 0.0000000 0.0000000
	P KRT HE ST HE ST HORVT D & C B & C C C C C C C C C C C C C C C C C C C	Р К К Т Н Е С Т К К К И О К V ( М L R V ( D # 0	PVRT HEST 1FXA H0RVT HLRV D#0	PVRT 1584 1584 HORV7 D80	PVRT HEST TFXA HORVT HLRV D#0	PVRT TFXA HORVT HLRV D#0
	-2.2532273+01 3.6245437+05 3.5551719+07 3.5551171940 0.0000000 2.4057164402 2.4057164402	-2.2475418401 3.6245757405 3.546727405 3.544727405 3.4702046400 0.0000000 2.4060471402 0.0000000	1,2000074400 7,1554174401 1,8371837-01 1,3499074400 0,0000000 3,2400689-01 0,0000000	2,5036166+02 5,125625494 3,2982109+03 -2,0006226+01 0,0000000 2,4057164+02 2,4057164+02	2,5041158+02 5,145,270+04 3,2746,0376+03 4,2746,040 2,4060471+02 2,4060471+02 2,4060471+02 0,000000	00+2+10750142+0 
	Е С А Н Т Я С С К А Н Т Я Г А И К В И С Н Г Я А В 1 Г Я В 1 В Я В 1 В Я В Я В Я В Я В Я В Я В Я В Я В Я В В В В	ELAS H1784 VERV1 H178 F16 P15 F15 F15 F15 F15 F15 F15 F15 F15 F15 F	ELAS HTRU TFIG HERA FIF EISP	H 140 H 1780 H 1780 H 1687 P 16 F 15 F 15 F 15 F 15 F 15 F 15 F 15 F 15	ELAS 11716 17716 17716 1716 1716 1716 157 157	ELAS HTRU VERVT HLRA PIF EISP
	2.6142434-02 8.2960120+01 7.3327939+01 0.0000000 1.7043951+02 2.4061340+02 2.4061340+02 0.0000000	2.6126245-02 8.2958807+01 7.2263819+01 0.000000 1.7043297-02 2.4064523+02 0.000000	1.4450605-04 4.6875000-02 6.054561-01 0.0000000 1.0126157-01 3.1715286-01 0.0000000	111	2.6854469-02 9.8394937.00 7.324810401 0.0000000 -1.4245521-00 2.40645521-00 2.4064523402 0.000000	1.452430.04 3.939137-02 6.054614-01 0.0000000 8.4470186-02 3.1715286-01 0.3000000
	ECC ELANG DEVAT FC LONLM PIO CISP	ЕСС ЕГАNG DE VM5 PIONLM CISP CISP	ECC DECANG DECANG Clsp Clsp Clsp		ECC ELANG FLANG C VHT C VHT C VHT C	ECC ELANG DEVMT FC Lont PIO C i SP C i SP
AL VALUES	0.800060 0,000000 1.0000000 0.0000000 6.37221400 0.0000000 1.600175240 V41U55	0+0000000 0+0000000 0+0000000 0+0000000 0+000000	0.0000000 0.0000000 0.0000000 1.0630146+01 0.0000000 1.3949102*02 0.000000 3.0929632~03	a descent initiation AL VALUES 0.0000000 0.0000000 0.0000000 0.0000000 0.0000000 1.0001752400 1.0001752400 VALUES	0.000000 0.000000 1.09262440 0.0000000 0.0000000 0.000000 0.001753400 1.001753400 RD DEVIATION	0,0000000 0,0000000 1,00,001146-01 0,0000000 1,943348-02 0,0000000 1,943348-02 0,0000000 0,0000000 0,0000000 0,0000000
NIWON	HAP0 RANGE TTVIS Latem Ree Ree HFAN	HAPO Range Wox TTVIS Latlm Ref Standa	НАРО W MAPO W 0 X G T T T T V G R F F T I S R F F T I S M G F F F F F F F F F F F F F F F F F F	POWGFO NOMIN Rand Range Tavis Latla Tavis Ref Mean	HAPO Range Wox Tivis Later Ree Standa	HAPO RANGE Wox Titvis Titř Reé
	5.4776625404 -1.4138336400 6.8472948403 0.00001000 1.0591672402 8.3370611-02 1.5959122400	5.4902628+04 -1.4902628+00 6.8412/112+03 0.0000003 1.0058/130+02 9.2355096-02 1.5959025+00	1.6709183+03 2.0264407-02 5.9160744+0 0.000000 1.141564083+09 3.7038714+02 3.7038714+02 2.9851121~02	4.9803562+04 -24.019562404 6.8472948403 0.000000 8.287308401-02 8.337061-02 1.5959122400	4,999491-04 -2.0224210401 6.8477112+03 0.0000000 8.29349401 9.2365096-02 1.5959025+00	1.673583+03 2.0175885=01 5.9160798+00 0.0000000 1.2712309+00 3.7038714-02 2.985112103
	н	НРЕ Н D D T 4 2 4 2 4 2 7 7 7 7 7 7 7 7 7 7 7 7 7	НРЕК 44601 44 4415 765546 765565 76571	Н Н Р Е К Н Н Р Е К Н 4 Г Р И Г С Р И П Г К Г С К К Г С К К Г С К К Г С К С С	4PER 4D01 *F 4V15 PVR15 RESV6 RESV6	HPER HDOT WF HVIS PVRTT RESVG RESVG
	-1.5308590-62 5.2915844.03 1.28402124.04 0.000000 -1.7167937-02 3.6245437+05 0.0000000	-1.5239996-02 5.2915679403 5.291567404 1.5840337404 0.000000 3.6245757405 3.6245757405 0.0000000	2.1987106-04 2.449487700 1.3856406+01 0.0000000 7.1554174+01 7.1554174+01 0.0000000	-2+0748393-01 5+5769283433 1+840712+04 0+0000000 -2+0553655-01 3+6245437+05 0+000000	-2.077720-01 5.5769164.03 1.7840337494 0.000000 -2.0698200-01 3.4245757405 0.0000000	2+076987-03 2+2360480+00 1+356496+01 1+3556496+01 1+6533956-02 1+6533956-02 7+1554174+01 0+000000
	Т Т Т Т Т Т Т Т Т Т Т Т Т Т	F PAG H ORV W PR B URN B URN D # 0 R I D # 6 T	FPAG HORV #PR BURN HORZ HORZ €F7	7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7	FPAG HORY #PR BURN FPAGT FPAGT HORZ	FFAG NORV BRLRN FFPAGT NORZ

TABLEY - SUMMARY OF STATISTICAL PARAMETERS - Continued

High gate

<del>59898401</del> 53257+03 53257+03 568916+02 568916+02 191180+01	725645401 182093403 182093403 18494121402 1489447404 148125402 1816314400 103764400 162764400 162764400	190710-01 197133401 196028403 1966151402 1966151402 1966151402 196750401 198750401	935615603 149857402 1948857402 1948947402 1948947402	1043283+01 2136226+02 1461252+00 755633+00
4 K 8 M 9 N		2.00 2.10 2.10 2.10 2.10 2.10 2.10 2.10		1 - 2 -
9481 HEST 15X1 HEXX HLRV D#0	РУЯТ НЕБТ НЕГХ НСТХ НСТХ РКТ НСТ НСТ НСТ НСТ НСТ НСТ НСТ НСТ НСТ НС	0 8 0 8 0 8 0 8 0 8 0 8 0 8 0 8 0 8 0 8	H H H H H H H H H H H H H H H H H H H	PVRT HEST TFXA HORV
7.5645180.01 5.050519303 5.0500000402 -1.6683920902 3.6116537909 2.3633367902 2.015578792 3.015578792	7,5924962*01 6,9123569+03 5,62600902 -1,7104546002 3,597665509 2,3536350902 2,3536350902 2,3536350902 2,3536350902 2,3536350902 1,0007626+00 1,0784060001 1,7685477403	3.8527587-01 1.1771755500 4.5018617401 5.3110602402 5.31600000402 5.31600000402 3.6116627404 2.372691597404 2.3726915904 2.3726915904		6.5611047=01 2.4984945+02 1.5712256+00 8.2838144+00
ELAS TFIG VERVI HLRA PIF FISP	Е С А С А С А С А С А А А А А А А А А А	E 15 HIR HIR HIR HIR HIR HIR HIR HIR	1110 1110 1110 1110 1110 1110 1110 111	ELAS HTRU TFIG Vervt
9.9416371-01 1.57177970 5.5001451+03 5.99504090+03 -2.3218641+01 2.32218641+01 2.32218641+01 2.32218641-02 3.0180053+02	9,9408028-01 1,5970861401 5,9961532403 6,0961532403 6,0340342403 2,3629257402 3,0203498402 5,2504426-04 6,577121-01 9,1515025408 1,423525-02	3.8017455-01 1.3360974+09 9.9552210-01 1.4848904+01 1.4848904+01 1.4848904-01 2.3719180-02 2.3719180-02 2.3719180-02 2.3719180-02	9.455556/481 1.496535601 5.600845403 5.6257922403 -2.3256093401 2.3717385402 2.3717385402	5.1790047-04 5.7099100-01 8.4113019+00
С 1 1 1 1 1 1 1 1 1 1 1 1 1	П	PICOLO PICOLO	ELANG DEVMT FC LONLM PIO CISP	ECC DEVHT
AL VALUES 0.0000000 2.3824884+04 2.3824884+04 2.3900000 0.0000000 0.0995120+00 5.9955120+03 1.5916522+00 1.5916525+00 1.5916525+00 1.5916525+00 1.5916525+00 1.5916525+00 1.5916525+00 1.5916552+00 1.59165555555555555555555555555555555555	0.0000000 2.2578217464.04 2.2578217403 0.000000 3.0011920400 3.0011920400 1.5917942400 1.5917942400 1.5917942400 0.0000000 2.4675494402 2.4675494402 2.4675494402 2.4675494402 2.407228401 0.0000000	2.1142/275-04 14479813-02 4.13.609413-02 Range to gi Range to gi 1.973.573.640403 2.14125.60403 8.0000000 2.991553.6400 1.5917810400 1.5917810400	0.0000000 1.9546681.04 2.13232994003 8.433999400 -2.9899653.00 5.6304111.03 1.5947174400 1.5947174400 ARD DEVIATION	0.000000 2.2966062+02 3.2942184+01
HAPO NOMIN' HAPO NOMIN' Range Tituis Thi Thi Rem Rem	HAPO HAPO TTVS Latla TtvS Standa Randa Randa Fatuda Hapo Fatuda Kanda Fatuda Kanda Fatuda Kanda Fatuda Kanda	LATLA THIT FILT FILT FILT TTV FILT FILT FILT FILT FILT FILT FILT FILT	HAPD RANGE 111415 Latten REE Stand	HAPO Range Wox 6
-5.478497 <u>5+40</u> 6 -1.6673588402 1.3606557403 0.00003000 5.969256401 6.3370611-02 1.5867653400		1.004487624640 3.7038714-02 4.6802464403 1.285102464402 1.285173403 2.9978586401 8.3370611-02 1.5877164400		2.8043395+03 8.2175616+00 8.2175616+00 1.9639724+01
HPER HDOT #F HVIS PVRIT RESVG	Н Н Р Р Р Ч Н Р Р Р Р Р Р Р Р Р Р Р Р Р	Р К И Т К Е С К К Е С С Н К Г Р К Г К Е С С Р К Т Т К Е С С	HPER H001 HV15 PVR11 RESVG	HPER HDOT WE
-2.0741182401 4.3569817402 3.6200507403 3.6200500402 3.6205427401 3.6245437405 7.6878637405	=2+123371+401 +3773077402 3.6339014403 3.635766001402 =2*1256801401 =2*1256801401 =2*1251401401 4.9868969400 1.245855400 1.245856960 1.245854900 1.245854900 1.245854900 1.245854900 1.245854900 1.245854900 1.245854900 1.245854900 1.245854900 1.245854900 1.245854000 1.245854000 1.245854000 1.2458540000 1.2458540000 1.2458540000 1.24585400000 1.2458540000000 1.2458540000000000000000000000000000000000	1.2749524+00 7.1554174+01 1.12387064=01 3.6350018+02 3.4268739+03 3.4268739+03 3.4268739+03 3.4269739+03 3.6245437+05 7.2045296400	-71234916401 3.8287730402 3.8287730402 3.8276600402 1.9772990401 3.6245757405	1 • 1 0 1 2 6 4 6 + 0 0 3 • 2 4 3 9 8 4 8 + 0 0 4 • 8 9 6 0 4 4 3 + 0 1
FPAG HORV HPR BURN FPAGT HORZ	1000 1000 1000 1000 1000 1000 1000 100	PRPAGT PRPAGT PRPAGT PRPAGT PRPAGT PRPAGT PRPAGT PRPAGT PRPAGT	НО Но Праст Праст Ст Ст Ст	7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7

T CHANNEL CTUTIOTOTICAL CONTENTS	L - SUMMARY UP STATISTICAL PARAMETERS - CONTINUED	
LUCAT	LAOL L	

Range to  $go = 10\ 000\ ft$ 

FPAG	-1.4416463+01	HPER	~5,6902892+06	HAPO	0.000000	ECC	9.9828001-01	ELAS	4.2586700+01	PVRT	2.9633542+01
HORV	2+4325069+02	HDOT	-4.2530672+01	RANGE	9.7749811+03	ELANG	1-2854854+01	HIRU	2.2404087+03-	+1534	2,2391044+03
R P R	2+8844980+03	2 E	1.0762404+03	XOM	1.8082570+03	DEVMT	5.8803499+03	TFIG	5+4800000+02	TFXA	1+8066028+02
BURN	3 • 5 800000 + 02	SIVH	6.4291670+03	TTVIS	4.0000000401	r. L	4.5165341+03	VERVT	-6.2549973+01	HORVI	2.4322731+02
1001		1 - X - 4	10++8/0+94*2			L UNLM	-2.3355128+U1	HLKA	CC433C370C - C		1+0/00/01/01
DWF	5+8449227+00	2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	1.5935233+00	REE MEAN	1.5917327+00 4 VALUES	CISP	2,9800835+02	EISP	3,0130685+02	2	
FPAG	-1.4691748+01	HPER	-5.6902204+06	HAPO	0.000000	ECC	9.9825621-01	ELAS	4.2674915+01	PVRT	2.9580421+01
HORV	2.4421394+02	HOOT	-6.4045299401	RANGE	9.8087977+03	ELANG	1.3001396+01	HTRU	2,2848915+03	HEST	2+2745437+03
R P R	2-8911851+03	7	1,0792195+03	XOM	1.8119640+03	DEVMT	5,8797800+03	TFIG	5,4834000+02	TFXA	1.8149857+02
BURN	3.5766000+02	SIVH	6+5706101+03	TIVIS	4.002000+01	L C	4.5471720+03	VERVT	+0+060060+01	HORVT	2141292442
FPAGT	-1.4671300+01	PVRTT	2,9590444+01	LATLM	-2.9642887+00	LONLM	-2,3353875+01	HLRA	3+5976625+04	HLRV	1.6948947+04
HORZ	3+6245757+05 5-0822002+00	RESVG		4+5	4 * 5 4 8 5 8 7 1 + 0 3	014	2.3955708+02 2.9817041107	P11 1010	2.3964970+02	DMO	9.3722154+00
5		1		STAND	ARD DEVIATION	5		5			
5046	7.014B147_01	HPER	5 19743005		0,00000		E 7003032.04	94 13	1 1 2 2 6 2 2 2 4 0 0	+070	1. 1247895-01
											0.07777000
- AUUU	UD*728215592			XAZ60	*0+ ***********************************		8=9031249401	0¥1#		1034	20.ecterosel
NATIO	104/71/01/04		10-0000074*1	11210	10+000001100	DEVII	U1+0+/18//•/		1,*200000041	T T T T T	004307077047°0
10401			20.02.00003.7		10-0+-/07-0		10+2111400+0	VERV	00+000+000+0 	I A LOL	DALEALAAAAAAA
	7.1554.74401		10-0/2000C+0 20-0128702-1		<pre>2.1.267870-02</pre>		0.4344471=UC	8 1 1 0 1 1 0	1010220220101	7140	0./2024884001
D W F	7.1822171-02	39.2	4.6418831-03	REE	4.1683035-03	CISP	1.1813161+00	E1SP	1.1763456+00		
					Range to	go = 5 0(	00 ft				
			2	A A O A		,					
					VAL VALUES						
PPAG NORV	-101956019+01	HPER	-5.6934563+06.	HAPO	0+000000	ECC	10-2206866	ELAS	10+99991+0++	PYRT	2.7369879401
N P R	2+5167462+03		10-1		50+5160+60+L	ELANG	1.2999584+01	HTRU	1.1024264+03	HEST	1.0857971+03
NNDO	3+5800000+02	SIVH	6.4291670+03	TTVIS	61+111226511 6-6000004-6	DEVMI	6+0744095+03	TFIG	5 • 7 400000 + 02	TFXA	1.8066028+02
FPAGT	-1-1468788+01	PVRTT	2.7377112+01	LATLM	-2-9525568400	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	0,000000000000000000000000000000000000	VERVT	-3.0577596+01	HORVI	1+5071387+02
HORZ	3 • 6 2 4 5 4 3 7 + 0 5	RESVG	8.3370611-02	THF	3.8309992+03		10+9104010-7-	HLRA	3.6116537+04	HLRV	1.6760927+04
	4+9717352+00	Ш.	1+5973543+00	REE Mean	1.5918138+00 1 VALUES	CISP	2.9666948+02	112	20+9+54010+5	0	7.941622700
FPAG	#1+204988401	HPER	- <u>6+6933680+66</u>	0 d V H	0.000000	FCC	•.9935951=11	61.45	# . 106719150)	1040	
HORV	1.5367826+02	НООТ	-3,2875855+01	RANGE	4.8224597+03	E A NG					
щ Р.К.	2+5328838+03	A F	9.4114751402	XOX	1.5917345+03	DEVMT	A. DABARA2403	15.15			
BURN	3 • 5 7 6 4 0 0 0 + 0 2	HV15	6+57061U1+D3	TIVIS	6.5280000+01		2 - 2 7 2 2 1 0 1 0 2 0 2 0 2 0 2 0 2 0 2 0 2 0				
FPAGT	-1-2029760+01	PVRTT	2.7539045+01	LATLM	-2-9513650+00	I ONI W				A NOR	704100001041
HORZ	3 • 6245757+05	RESVG	9.2365096-02	THF	3.8494355+03	014	2.4054784402				
DMF	5-0183603+00	RE	1+5371434+00	REE	1.5917428+00	CISP	2.9690366+02	EISP	3.0118203+02		
				STANDA	RD DEVIATION						•
FPAG	1+0354004+00	HPER	2,8506953+03	HAPO	0.000000	EČC	4.6482990-04	ELAS	1.8549958400	PURE	4. 22886 73m01
A NOH	2+1798975+00	HDOT	2,9826924400	RANGE	1.0549052+02	ELANG	1.5967087+00	HIRU	1.5058122+02	HEST	1.4529808+02
SPR	4-9956856+01	- WE	2+0768629+01	- NOX-	3.3158789+01	DEVHT	9.000000400	7816			
	3.9299282+00	517H	3+0351936+02	TTVIS	1.0008236+00	L U	3,9785361+01	VERVT	2.5487076+00	HORVT	2.6800860+00
	8+8718361-01	PVRTI	4.7256746-01	LATLM	2.1484375-02	LONLM	6+4541842-02	HLRA	1 • 7685474+03	HLRV	6.7342006+02
7 101	7.1554174401	242	3.7030714-02	THF	4.2638011+01	P10	3,3874192-01	PIF	3.2997987-01	DWO	7.9017122-02
			Chevanietty-	XTT	*****	€ I SP	1.8736975+00	EISP	1.1862658+00	1	

TABLE  $\mathbf{X}$  - SUMMARY OF STATISTICAL PARAMETERS - Continued Range to go = 2 000 ft

	2,3363805+01 6,207628+02 1,880628+02 8,3673345+01 1,6760927+09 7,0067791+00	2.3130405+01 5.9472211+02 1.8149555+02 8.449555+01 1.6948947+04 1.6948947+04 7.076323000	3,6372201-01 1,145998482 5,34610 5,346788409 6,7362006402 1,152654081		7.3940725.00 1.0121773402 1.8066028402 5.2083862290 1.6760927409 6.0715221400	<ul> <li>A state of the sta</li></ul>	7.4409325400 1.0140803402 1.8149857402 5.7524552400 1.6948947404	00+5114450+9	3.6991293-01 8.674557400 5.346017900 1.2660017900 5.35309087 5.53090829 5.53090829 5.530908290
	PVRT 1557 1557 1574 H1774 D40 D40	PVRT HEST TFXA HORVT HLRV DWO	PVRT HEST TFXA HLRV HLRV BWO		PVRT HEST 15XA Horvt HLRv D#0	1	PVRT HEST 15XA Horvt	0	Р V R T HEST TF XA Horvt HLRV 000
	4.1318802+01 6.1689375+02 5.9800000102 1.8346626401 3.6116537+04 2.4117478402 3.0089680+02	4.0231040+01 6.0233609+02 5.9825999+02 -1.7801854+01 -1.7801854+01 3.6776625+04 2.4115394+02 3.0098001+02	3.2897722+00 1.233 <del>9645</del> 02 1.4825469+00 3.10425469+00 1.7685474403 3.3071891-01 1.2066709+00		7.3694072401 1.0256737402 6.4800000402 -3.7781125400 -3.4148035402 3.4148035402 3.0049842402 3.0049842402	s subar se sono anno a	7.3616596+01 1.0430284402 6.4834000+02 -3.4518660400	2.4153733+02 3.0058449+02	1.8177792+00 1.4720 <del>94</del> 8+01 1.5000000400 1.6949351+00 1.7685474+03 3.3946189-01 1.2366474+00
	ELAS HTRU VERVT HLRA PIF EISP	НТКU 1716 Vерки 16 16 615 615 615	ELAS H <del>17R</del> U TFIG VERVT VERVT PIF PIF Elsp		ELAS H17RU VERV VERV HLRA P15 F15		ELAS HTRU TFIG Vervt	EISP EISP	ELAS #170 1616 VERV1 HLRA P15 F15 F15
	9,9984267-01 1,7935719404 6,2299287404 3,3721880403 3,3721880403 2,410395402 2,410390402 2,9592064402 2,9592064402	9,9983888-01 1,7082480+01 6,2312332403 3,4178055+03 -2,4106685+02 2,4106685+02 2,9615238+02 2,9615238+02	5,3904790-04 3,1087204+09 7,9686887+00 5,4677453+01 6,4541842-02 3,2625958-01 1,85448395+00	u	9.999668-01 6.6299549401 6.5231778403 6.5231778403 2.9152533403 -2.3449735401 -2.44139483402 2.9521291402 2.9521291402	· · · · · · · · · · · · · · · · · · ·	9,999637=01 6,6175589+01 6,5247631+03 2,9108903+03	2.4145193402- 2.9538721402	5.3904790-04 1.7514991+00 7.5828754+00 1.215830+02 6.4100919-02 3.3729739-01 1.8418953+00
	ECC ELCC DECANG DECANG PFC CISP CISP	ECC ELANG DEVMT Con Con Con Con Con Con Con Con Con Con	ECC ELANG DEVMT FC Lonlm Pio CISP CISP	nt initiatic	ECC ELANG DEVMT FC Lonlm CISP CISP		ECC ELANG DEVMT FC		ECC DECANG FC WAT FC CALA FC CALA CISP CISP CISP
AL VALUES	U=0U00000 1+9165020+03 1+4U35719+03 9-0000000-01 -2+9453618+00 3-369279+03 1.5919410+00 VALUES	0+0000000 1+9280074+03 1+9280074+03 8+949000401 -2*9439353+00 3+954877+03 1+5918706+00 1+5918706+00 15918706+00	0.000000 3.1323414401 3.274528401 3.4125515501 3.4125515501 5.5031769401 4.1143309-03	Vertical desce al values	0.000000 4.4389219401 1.0736682403 1.000000402 2.9105117403 2.59105117403 1.5922465400	VALUES	0.0000000 4.453/285401 1.0754257403 1.3032000402	2.9066079403 2.9066079403 1.5921789400 4rd deviation	0.000000 2.2641732+00 3.3691152+01 3.3790123+00 2.1760039-02 1.2070108+02 4.0779524+03
NIWON	HAPO Range Wox TTVIS Latlm Ree Rean	HAPO Range Wux Tivis Tivis Thi Ree Standa	HAP0 Range Wax Fit Latlm Ree Ree Ree	NIWON	HAPO HANGE TTVIS TTVIS TAILA TRIF TAILA Ref	MEAN	HAPO RANGE WOX TTVIS	LA'L" THF REE Stand/	HAP0 Range Titvis Titvis Ree Ree
	-5.6947456406 -1.8296334401 8.2279978402 6.4291670403 5.3371023401 8.3370611-02 1.6000954400	-5.6747341+06 -1.8011885+01 8.2457300+02 6.57705101+03 2.3140399+0 2.3140399+0 1.5998880+00 1.5998880+00	2.6106980403 3.5195535404 1.9862221401 3.05427550 3.65427550 3.65427550 3.65427560 2.96507760 2.96507760		-5.6951839+06 -3.7162234908 6.1678073+02 5.4291670+03 7.4012433403 8.3370611-02 1.6029661+00	. !	-5.6951826+06 -3.6553151+00 6.1851488+02 6.5706101+03	1.6030131+00	2.6106980+03 1.8106554+00 2.0545205+01 3.0351936+02 3.015172234+02 3.01038714~02 3.0247831+03
	HPER HPER FVIS FVIS FVIS FCII F	HPER HDOT #F HVIS FVRT RE KE	HPER HUDI WF HVIS PVRTT RESVG		НРЕК 47001 4715 7415 74115 765546 76577		НРЕ R 4 10 0 Т 4 4 I S	RESVG	HPER HD01 WF HV15 PVR11 RESVG RESVG
	-1.2323558+01 8.3742114+01 2.2283724+03 3.5900000+02 -1.2366583705 +.3789758+03	-1.2052817+01 8.4213890461 2.229580401 2.52766800403 3.5766800402 -1.1886729401 3.62865727405 4.4230237+00	2,2876176,00 9,07992329,01 4,68443911401 1,99429382,00 1,994694340 1,994177491 7,2167351-02 7,2107351-02		-3.4754613+01 5.35621440400 1.6904496403 3.558000001+02 -3.5956762401 3.787421+00 3.7877421+00		-3.2503690+01 5.2603690+01 1.66939423+03 3.5766000+02	-3+0339851+01 3+2245757+05 3+7803886+00	1 • 1 480281 +01 2 • 2 2 3 0 1 9 4 • 01 5 • 0 0 3 3 1 1 4 + 01 3 • 9 2 9 9 2 8 2 • 0 0 1 • 0 9 2 7 1 41 + 01 7 • 1 5 5 4 1 7 4 • 01 1 • 5 9 3 4 1 3 7 • 01
	F H 2 4 2 6 7 7 6 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7	15746 15746 1677 16746 17746 17746 17746 1777 1777	F P A 6 H 0 R V B V R V H 0 R V H 0 R Z D W T D W T		FPAG HORV Bupr Fpagr HOR2 D#F		FPAG 8074 8074 8074 8074 8074 8074 8074 8074	FPAGT HORZ DWF	F P A G HOR V B P R D R N F P A G T D # F

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TABLE  $\mathbf{Y}$ . - SUMMARY OF STATISTICAL PARAMETERS - Concluded

Landing (probe contact)

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	1.459745450 1.5393326401 1.829427402 2.4254677404 1.45740927+04 5.8323653400		10-010085/-1	10+12884+01	20+1594119*1	4.1540342-01	1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-1-	5.4004252400		and the second	1+7478577=01	4.4243526+00	5+3441252+00	2+1878169-01	-4.7342004+02	4.064776502	
	PVRT HEST TFXA H0RVT HLRV DW0	i. A'	- FRV4	HEST	TFAA	HORVT	HERV	0.0			PVRT	HEST		LAROX	HLAV-		
			5.2205338+01	1.2046466+01	6+8212000+02	-2.7416656+00	3.5976625+04	2.4171062+02	3+0033187+02		1.1032304+01	2.4343127+00	10+5090611+1	1.3968485-01	1.7685474+03	10-78-2121 6	1,2527314+00
	11140 11140 11140 11140 11140 11140 11140 11140		ELAS	HTRU	1F1G	VERVT	HLRA	PIF	E1SP-		ELAS	HTRU	9131	VERVT	HLRA	1	ETSP
	<b>9,8999238-01</b> 6,0244581+01 6,6735784+03 2,795158+03 2,4159702+02 2,415944962 2,9495449+02	. ,	9.999218=01	5,2074092401	6.7060234+D3	2.7894441+03	-2.3449685+01	2.4162672+02	2,9509575+02		5.0330879-04	1 0880638401		7078861401	6.4541842-02		3.2400687-00 1.68516779+00
	ELANG ELANG FCC VHT FCC VHT C45P C45P C45P		ÉÉC	ELANG	DEVMT	F.C	LONLM	P10	c i sP		FCC				PNC H		e159
IAL VALUES	0+0000000 7.6110553+00 9.0804427+02 1.3000000402 2.940369+89 2.77224270+03 1.5924270+03	I VALUES	0.0000000	7,5485133+00	8.7446946+02	1.3096000+02	-2.9392749+00	2.7829759+03	1.5923982+00	ARD DEVIATION	0.00000	2 4430344101			2.2014016-02		1.8381376+01
IWON	HAPD Range Wox TTVIS Latlm THF Ref	MEAN	HAP0	RANGE	XOM	TTVIS	LATLM	THF	REE	STAND	Carn		A NGP		STATE T		REE
		2	-5+6951706+06	-2.9541672+00	4*9444265+82	6.5706101+03	1.6713420-01	9.2365096-02	-+++++++++++++++++++++++++++++++++++++			CD11104/6/47	7.5965/98+02	4.5587241401	3.0351936402	1 A= 4 = 1 = 1 = 0 = 1	3.7038714-02 2.9801161-03-
	HPER HDOT #F HVIS PVRTI RESVG		HPER	HDOT	14 H	SIVH	PVR11	RESVG	RE			7 1 2 2	ноот	<u>й</u> Е	1715 1115	- 1 × 1	RESVG RE
	-84.8170060+01 9.4747324-02 1.44215359403 3.55800000+02 3.6245437405 3.6245437405 3.6245437405	in the solution of the solution of the	-8+5752+72+01	7.8766852-02	1-3709138+03	3+5766000+02	=5+4397409+01	3 • 62 45757 + 05	-3-6219749+00-	•		1 • 5208201+01	9.3028788-02	1.1540892402	3.9299282+00	1 = 2 + 0 3 + 4 3 + 0 1	7.1554174+01 2.5059819=02
	FFAG HORV HORV BURN FFAGI HORZ	÷	EPAG	HORV	New	BURN	FPAGT	HORZ	DWF	١		FPAG	HORV	RPR	BURN	FPAGI	HORZ

# TABLE VI. - COVARIANCE MATRICES

(a) Powered descent initiation minus 3 min

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	3 3 4 7 3 9 4 9	-1.00415.04.07				a a suprame as investors as a		
	3.16/3049+06	-1+2061524+07	-8.9850609+03	1.0313026+04	-2,2886843+03	6+6289970+01	-3.3903353+06	
	-1.2061524+07	7.3872555+07	1,4862947+04	+5.8781028+04	8.8860824+03	-1.2307412+02	1+2419903+07	
	1.0113034.04	1.4002997404	3,2249068+03	-1,5777566+01	6,2702526+00	-2,2785938+01	1+0659712+04	
	-7.2084843.03	P-0940014+03	*1.5///500+UI	4.7200006401	-7.5711884+00	1+2577474-01		
	6+6289970+01	+1.2309412+02	-2-2985938+01	-/+5/11809+00	1.6550311+00	-4.6340727-02	2.94/2487+03	
	-3,3903353+06	1.2419903+07	1-0659712+04	=1.0696687+04	2.4472487.03	-7.4157419+01	3.6451051404	
	6.7751270+06	-2.2258358+07	+4.3134474+04	1.9595803+04	=4.8896338+03	3.0731394+02	-7.5082091+04	
	1+2797005+05	-1.9029474+05	-2.5527272+03	2.0897877402		1.9206046+01	-1.4130450405	
	-5.3402692+03	1.0190572+04	4.2265385+01	#1+0312668+01	3.8114346+00	+2.9815271+01	6.0750444403	
	2,5376855+03	-9.8191660+03	-7.3382897+00	8.3713944+00	-1.8345686+00	5.4249784-02	-2-7140993+03	
	6+2940544+01	-7.4464709+02	1-7466935+01-	5-5701523-01	-4-7415302-02	-1.7481729-01		
	0.0000000	0.0000000	0.0000000	0.0000000	0.0000000	0.000000	0.0000000	
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	0+//912/0+06	1+2/9/005+05	-5,3402692+03	2.5376855+03	6.2940544+01	0.000000		
	-2+258358+07	+1.9029474406	1.0190572+04	-9.8191660+03	-7.4464709+02	0.000000		
		-2,532/2/2+03	4.2205385+01	-7.3382847+00	1.7666935+01	0.000000		
		-8.0444459.01	-1,0312668+01	8+3/13944+00	5,5701523-01	0.000000		
	3.0731304.03	1.0204044.01	-2 0010970+00 -2.0010970-01	-1.8345680+00	-4.7415302-02	0.000000		
· · · · ·	=7.5082091.04				-1.2481929-01	0.0000000		
	2.2987025-07	2.1564041-05	-2.0210410403	-24/1-U973403 6.38854444-63	-4 5555975.00	0.00000000		
	2.1562941.05	1.0843094404	-2.351324917707	343703978970703		0.0000000		
	-2-0219619-04	-7-3513000+03	1 0490070+01	1.0/7281/+02	-5.8999754+02	0.000000		
	5.3485446.03	1.0742817+02	-4.1447494+00	2.0400325400	5.080500/-01	0.0000000		
		-5.9999754+02	5-4865887-01	E-08300523700	3 0093444400		a a success an aris in the	
	0.000000	0.000000	0.0000000	0.000000	2.0073014+00	0.0000000		
			310000000	010000000	0.000000	0.0000000		
	<u>`</u>							
				(b) Landing				
	•							
	8.9401294+03	4.0214718+05	=1.0083222+05	=1+2097859+01	8.6492727+00	-1.1516702+00	#8.8730659+03	· · · · · · · · · · · · · · · · · · ·
	4+0214718+05	3+9267974+07	-9.2973420+06	-1+3411112+03	-3.6956773+02	6.3481602+01	-3.9622443+05	
2 m s	+1+0083222+05	-7+2973420+04	4.7320261+06	1,9858105+02	3,8236894+02	1.5695294+03	9.8686791+04	
	+1+2097859+01	-1+3411112+03	1,9858105+02	3.6349326-01	-3.3748975-01	-7.7699443-02	1.0686285+01	
	8=6492727+00	-3.6956773+02	3.8236894+02	-3+3748975-01	1.7117478+00	2.4129552-01	-7.0454865+00	
	-1+1516702+00	6.3481602+01	1.5695294+03	-7.7699443-02	2,4129552-01	3.8811944+00	1+5804325+00	
, <u> </u>	-8.8730659+03		9+8686791+04	1+0486285+01	-7.0454865+00	1,5004325+00	8+8257081+03	
	-4+0329169+05	-3.9439116+07	9.3088287+06	1.4202701+03	2.8849388+02	-8.0859516+01	3.9697603+05	
	1+0082805+05	9.2907747+06	=4,7318451+04	-1+9839669+02	-3,8256238+02	-1.5095157+03	-7.8683830+04	
<b>,</b> .	1+368441/+01	1.4038240+03	-2,1431258+02	-3+68243/0-01	3.4607133-01	9.2035043#02	-1+2123991+01	
3	1,4497831,00	-2.5037333401	-1.5790583403	2.8881402-02	-2 2220732-01	-2.0759540400	-1.8024008400	
,	-7.4410589.01	-1.1380413404	7 4954475502	5,7635970+00	-5 3495343+00	-318/3/308/00		<u></u>
	-/19310377901			00+2+258+0+00	-343913501400	-11101//32+00	210323808+01	
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		· ·						
	-4+0329169+05	1.0082805+05	1.3684417+01	-9.7567078+00	1.4497831+00	-7+6410599+01		
	-307437116+07	7.270//1/+00	1.4038240+03	2+2174289+02	-2.5037333+01	-1+1-80413+04		
	7+3088287+06	-1.0030//07	#2+1431258+02	*3+>006725+02	-1.5790503+03	7.6054475+02		1 A. 1
	1.4202701+03	-1.70.7667+02	-3.6824370-01	3+6/81936=01	6.7881402-02	5+2725870+00		
		-1.6496167.03	9.443604133401	-1+/7010/0+00 -2.461/087	-2,3230/32+01	-313075262+00		
	-0:0007010+01	-1+30/313/403		7.84144434-0	-3.8/3/568+00	-1+1+17/52+00		
	3.9438618.07	-7:0003830+04	-1.4839243403	/+0019603400	4.0127117401	310-33008701		
	-9.3081902.04	4.7316430404	2.1412162403	3.50700444407	1-6790370403	-7.4437144409		
		2.1412142403	3.7874774-01	=3.7920440=0	++++++++++++++++++++++++++++++++++++++			
	=1.3203040±02	3-5028944+02	=3.792044i)=D1	1.7887020+00	2.5408944-01	5.9572344+00		
	4.0127117+01	1.5790370+03	-8.4080655-02	2.5408946-01	3.8712511+00	1.0098373+00		
	1.3258336+04	-7.6437164+02	-5,3058452+00	5.9572344+00	1.0098373+00	1+2433774+02		

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Accelerometer bias (3σ) cm/sec <sup>2</sup>	Percent ellipse	Down-range semimajor axis, n. mi.	Cross-range semiminor axis, n. mi.
95	% confidenc	e navigation uncert	ainties
0.6 .6 .6	99 90 50	3.2 2.3 1.2	1.1 .8 .4
.2 .1 0	99 99 99	1.2 .95 .9	•7 •7 •7
55	5% confidenc	e navigation uncert	tainties
.6 .2	99 99	3.0 1.2	1.2 .8
No navigati	lon uncertai	nties (perfect upda	ate prior to PDI)
.6 .2 .1	99 99 99	.5 .24 .18	•7 •54 •48

TABLE VII.- CURRENT ESTIMATE OF LM LANDING DISPERSION ELLIPSE

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TABLE VIII.- AV AND PROPELLANT SUMMARY

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(a) Major event points<sup>a</sup>

Event	. ΔV, fps	Propellant, 1b	Oxidizer, lb	Fuel, 1b
DOI	71.8 ± 0.5	251 ± 3	155 ± 2	т ∓ 96
Braking (high gate)	5500 ± 9	14 471.0 ± 43	8989 ± 29	5582 ± 16
Approach (low gate)	6278 <b>.</b> 0 ± 8	16 854 <b>.</b> 0 ± 46	10 359.0 ± 32	6154.0 ± 18
Landing	6674.0 ± 58	16 670.9 ± 114	10 241.0 ± 72	6429.9 ± 44

(b) Total descent

Item	Propellant, lb	Oxidizer, lb	Fuel, lb
Loaded (tank)	18 091.9	11 148.0 ± 10	6943.9 ± 6.3
Required	16 670.5	10 241.1 ± 72	6428.6 ± 45
Usable remaining	1290.4 ± 115	794.7 ± 71	495.7 ± 44

 $^{\mathbf{a}}All$  uncertainties presented are lot

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Figure 1.- Altitude dispersion corridor.





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Figure 3.- Landing gear constraints at landing and three-sigma velocity error ellipse at probe contact.



Figure 4.- Time histories of selected parameters.



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Figure 4.- Continued.

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Figure 4. - Continued.

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Figure 4. - Continued.

(d) Vertical velocity.

Vertical velocity, fps



Figure 4. - Continued.

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Figure 4.- Concluded.

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