

THE HINDU MUSICAL SCALE

AND

THE TWENTY-TWO SHRUTEES

BY

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(Retired Deputy Collector)

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List of abbreviations used in the book.

Names of the seven notes of the Hindu Musical Scale. Corresponding names used by European

		Scientists.	Artists.
प.	पङ्कज	C	Do.
ऋ.	ऋषभ	D	Re.
ग.	गङ्गधार	E	Mi.
म.	मध्यम	F	Fa.
प.	पञ्चम	G	Sol.
धै.	धैवत	A	La.
नि.	निषाद	B	Si.

अ. को.	अदकोमल	ff	... Double flat.
को.	कोमल	f	... flat.
त. ती.	तरतीव्र	ss	... Double sharp.
ती.	तीव्र	s	... Sharp.

INTRODUCTION.

The work accomplished by Mr. DEVAL, it would hardly be an exaggeration to say, marks an epoch in the history of Indian Music. As he tells us, many treatises have already been written on the subject, but those, who have heard Indian Music and who have sufficiently keen musical perception to appreciate the smoothness and beauty of the intervals used, must have laid down some of those books after reading them with a feeling of bewilderment. If Mr. Deval's results are accepted, the Indian scale which is several thousand years old will stand out as the most perfect example of a natural untempered scale.

That Mr. Deval's 22 Shruties are the correct ones may in the first place be presumed from the fact that he has studied the latest European literature on the subject of the formation of scales, and has spent eight years in testing the notes used by various singers in order to ascertain the exact intervals which the singers endeavour to produce. As he tells us he has been guided by the principle laid down by old Indian writers on Music, that the simplest ratios are always the best.

Secondly it will be found that, although Mr. Deval did not test his Shruties by major and minor thirds, they will stand that test. One of the principal intervals, C to E, is avowedly formed by 'Anuvadi' or imperfect consonance. Indian singers are quite familiar with thirds, and in their more elaborate efforts make a frequent use of arpeggio forms with thirds, fifths and other harmonic intervals; it may be inferred that the relationships by thirds which exist among the 22 Shruties are not by any means accidental.*

* The major thirds.	The minor thirds.
(1) Sa : ti. ga.	(1) Sa. : K. ga.
(2) K. ri. : K. ma.	(2) a. k. ri. : ti. ga.
(3) ti. ri. : ti. m.	(3) m. ri. : k. ma.
(4) K. ga. : pa.	(4) k. ga. : t. t. ma.
(5) ti. ga. : ak. dha.	(5) ti. ga. : pa.
(6) K. ma. : m. dha.	(6) K. ma. : k. dha.
(7) t. t. ma. : k. ni.	(7) ti. ma. : ti. dh.
(8) pa. : ti. ni.	(8) pa. : k. ni.
(9) K. dha. : Sa'.	(9) ak. dha. : ti. ni.
(10) m. dha. : ak. ri.	(10) m. dha. : sa'.
(11) ak. ni. : m. ri.	(11) ak. ni. : k. ri.
(12) k. ni. : ti. ri.	(12) ti. ni. : ti. ri.

Thirdly, a test may be applied based on the three Gramas. This subject is not well understood at the present day. So far as I can gather, the ancient system permitted of two kinds of Modulation, modulation from one mode or Raga to another using in each Raga certain well defined combinations of the Tivra and Komal notes of the scale as essential notes and certain others as auxiliary notes or 'Murchchhanas,' and modulation from one Grama to another. The Shadj Grama is referred to Panchama or G as the fundamental note, the Madhyam Grama to Komal Madhyam or F and the Gandhara Grama to Tivra Gandhara or E. Mr. Deval's Atikomāl Rishab or C sharp, would in the Shadj Grama correspond nearly with Tivra Madhyam.* The intervals used in the Gandhara and Madhyam Gramas have been described by various authors. The first has its semi-tones between the 2nd and 3rd and 5th and 6th and therefore corresponds with E, F sharp, G, A, B, C, D, E. The 'Madhya Dhaivat' of 400 vibrations appears to be required in this Grama. The Madhyam Grama in which a scale like our just major scale is used, requires Madhya Rishab, Madhya Dhaivat and Atikomāl Nishad; I ascertained from Mr. Deval's monochord that Prof. Abdul Kareem actually used these notes in the Bhimpalas Raga which is evidently set in the Madhyam Grama. Lastly it must be noted that the tenth note, Atikomāl Madhyam, is the familiar dominant seventh.† As one would expect it is only used in conjunction with E or Tivra Gandhara. Of the remaining notes some are said to be used only as 'Murchchhanas' or auxiliary notes; in this connection it is to

* Perhaps madhya dhaivat is used in this Grama. This note with ak. ri. and ti. Ga. forms a major chord.

† In several Ragas ti. ma. (F sharp) and K. dha. (A flat) are found together. The former note has been tested and cannot be mistaken for any other such as G flat. This, together with the tonic and dominant pedal and the progression of melody used, appears to show that the 'augmented sixth' is known to Indian Music.

be remembered that in a Murchchhana, the quarter tone involved is frequently combined in a peculiar kind of ornamentation with its fifth. It follows that each note used as a Murchchhana must have its fifth amongst the remaining Shruties.

In this way Atikomāl Rishab which, as I have said, may be an essential note in the Shadj Grama, but which is generally used as a Murchchhana upon the note Sa, has its corresponding note 'Atikomāl Dhaivat.' If the notes of the Tivra and Komal scales, those I have mentioned as being traceable to the Gramas, and their corresponding fifths, are eliminated, there remain Tivratar Madhyam of $345 \frac{3}{5}$ vibrations and Tivratar Nishad of $455 \frac{5}{8}$. These notes appear to be actually used as essential notes in combination with 'Madhya Dhaivat' and 'Tivra Gandhara' in one Raga. This involves the use of harmony which is unknown to European Music. Tivratar Madhyam also corresponds with G flat in its harmony with Komal Gandhara and Komal Nishad.

Mr. Deval's 22 Shruties appear to throw considerable light on the question of the constitution of the Ancient Greek Modes and will, I have no doubt, prove of the highest interest to European Scientists. In his book on the "Sensations of Tone," Prof. Helmholtz expresses doubt whether the Greek Modes were built up from the relations of F or those of G, and he suggests that they may possibly have been built up from both. If the Komal notes of Mr. Deval's scale are taken with Sa and Pa, as in the scale which he calls the Indian Diatonic Minor Scale, a scale is obtained which is in all probability identical with the Doric Mode. If the identity is accepted, it follows (1) that B flat is the fifth above E flat and is a relation of G, (2) that A flat is the fifth above D flat and is a relation of F. It also follows that in the ancient scales until the time of Pythagoras, tuning exclusively by fifths or thirds was unknown, the simplest intervals, which are obtained by fifths and thirds combined, being used.

It is only in a system like the European, where transposition from one fixed key to another, and extensive modulation is practised, that tuning by a long series of fifths, tempered or otherwise, is likely to lead to anything but confusion. The Indian Tivra scale substitutes F sharp for F and the fifth above, D for the A in our major scale, thus producing the smoothest and most harmonious scale possible, one in which every note is in primary or secondary harmony with G. This scale appears to be identical with Syntono-Lydian Mode. As regards the question of tonality, writers who accuse Indian Music of being deficient in that respect are probably not aware that it is an almost invariable rule for Indian Ragas to be accompanied by a pedal bass of the tonic and its fifth. The effect is certainly to suggest harmonies which lead to a full close on the tonic in most Ragas and in some perhaps to a half close on the same chord.*

Indian Musicians owe a great debt of gratitude to Mr. Deval, for, now that the Shruties are known, it will be possible to construct harmoniums which will be in tune with Indian Music. The tempered harmoniums now in use which have a painful effect upon Indian ears will then be discarded. I have no doubt that with the advent of properly constructed keyed instruments, Indian Music will enter upon a new era of progress and development, possibly in the direction of harmony, for harmony is already extensively practised in the form of irregular Arpeggios. This progress will be hastened by the invention of a simple musical notation; and for that purpose also Mr. Deval's researches will be of the utmost value.

BELGAUM, 21st Oct. 1910.

E. CLEMENTS.

* The 3rd being omitted the over-tones would strongly suggest a major chord. Mr. Deval has promised to undertake a careful examination of the Ragas. Such an examination ought to set at rest many doubtful points which suggest themselves in the present state of knowledge on the subject.

PREFACE.

Two years ago I published a small brochure entitled "Music East and West" dealing mainly with the scientific value of the Hindu musical scale and the question of "*Shrutees*." But further study of the subject has enabled me to state more fully my humble views and hence the present pamphlet. I read specially Capt. Day's Book on "Music of Southern India" which was suggested to me by Sir J. W. Muir Mackenzie, the late Revenue Member of the Government of Bombay. He has a fine ear for Music. About 3 years ago I had an opportunity of explaining the subject to Sir J. W. Muir Mackenzie, when I laid before him my views, and practically demonstrated them with the help of Professor Abdul Kareem, an artist of great renown on this side of India. I also perused with great interest and profit the late Mr. A. J. Ellis' paper on the "Musical Scales of the World." Besides the valuable light thrown on the subject by these treatises, I had also much and invaluable enlightenment from Helmholtz's "Sensations of Tone" a masterly work on the Science of Music. The perusal of these and other works has served to strengthen the views previously held by me. The tables of Scales in the present brochure are almost entirely worked out afresh, and in some respects differ from those in the old pamphlet. In that work I had touched upon the question of *Shrutees* so far only as the Diatonic Scale of seven notes was concerned. In this brochure, I have arrived at a probable solution of the whole question of 22 *Shrutees*. The paper read in the Kirloskar Sangit Theatre on the *Shrutees* is incorporated in this pamphlet.

It should be remembered while reading this pamphlet that there are two kinds of tones—the tones of the *natural* scale

and those of the *tempered* scale. According to Blaserna the vibrations of these notes are as follows :—

Natural Scale or Just Major.

C	D	E	F	G	A	B	C
240,	270,	300,	320,	360,	405*	450,	480.

Tempered Scale.

240, 269 $\frac{2}{5}$, 302 $\frac{2}{5}$, 320 $\frac{2}{5}$, 359 $\frac{3}{5}$, 403 $\frac{3}{5}$, 453, 480.

It will thus be seen that the above two scales are quite different. When a European repeats the seven notes of the Modulator, Dho. (d); Ray, (r);* Me, (m); Fah, (f); Soh, (s); Lah, (l); Te, (t); Dho, (d); he necessarily refers to the notes of the tempered scale, which is now universally used in Europe in vocal as well as in instrumental music. The Hindoo Musician, who repeats the seven notes of the natural scale, refers to the natural scale which is given above. The notes in the natural scale are indicated by the letters C, D, E, &c., as has been done in Scientific Books, and not by the usual small letter Solfa notation to prevent ambiguity and confusion. I am, however, for the present concerned with the notes of the Hindoo Music and as such with the notes of the natural scale only, noted above.

The sharp and flat notes :—The sharp and flat notes of the tempered scale are the result of the sub-division of the interval between any two principal notes, into aliquot parts or equal divisions. Such is not the case with Hindoo Music.

The interval between C and D or between 240 and 270 vibrations or the length of wire between 32" and 36" is divided into 4 parts which, as measured by Ellis's cents, are not equal parts, but 70, 42, 70, 22 cents respectively. The notes making up these intervals are called अ० को० ऋ, क्रो० ऋ, म० ऋ, री० ऋ. The Indian word Komal must not be confused with

* Blaserna gives 400 as the vibrations of A, whereas our A is of 405 vibrations, which is exactly the Panchama or the 5th of D, vibrations 270.

flat, nor Tivra with sharp, nor must Atikomāl be confused with double flat or Tivratar with double sharp. The nomenclature is quite different. As a matter of fact Tivra coincides with sharp in the case of only one note F sharp, and Komal with flat in the case of four notes D flat, E flat, A flat and B flat.

The formulæ embodied in the pamphlet, which have been deduced from rules laid down by Sanskrit writers, have been worked out for me by my learned and esteemed friend Mr. Nilkanth Vinayak Chhatre B. A., L. C. E., Fellow of the University of Bombay and retired Deputy Educational Inspector C.D. I take this opportunity of thanking him for the great interest he evinced in discussing the subject and suggesting several improvements. I must also express my obligations to my friends, Dr. G. K. Garde, the Hon. Mr. V. R. Natu, Professor R. K. Joshi, late of the Fergusson College, Poona, and others, who helped me much by their valuable contribution to the discussion of the subject.

I am extremely thankful to Dr. Hamilton who has a very fine ear and who very patiently heard my demonstration and encouraged me to continue my efforts in this line. Mr. Mac-Millan, Assistant Collector, Ahmednagar, kindly came over to Poona and very sympathetically went through the whole programme of the last demonstration which took place at the Kirloskar Theatre in Poona and made several valuable suggestions.

I cannot adequately express my gratitude to Mr. E. Clements, District Judge, Belgaum, who voluntarily and promptly extended his sympathy towards my efforts. He is educated in European Music and has also a very keen appreciation for Hindoo Music. He has not only written an intelligent introduction full of appreciation and suggestion at my request but has improved this pamphlet in matter as well as in form and has thus made it intelligible to the European as well as to the

Indian Public. Not only this, but Mr. Clements has suggested to me that there is a branch of Indian Music which requires scientific and systematic treatment on similar lines. He has convinced me that without the development of this latter branch, the present attempt will be incomplete. I allude to the composition of Indian Rag's and Ragini's and especially to their notation, a subject, which I mean to take up as soon as I can.

SANGLI,
29-10-1910. }

K. B. DEVAL.

THE HINDU MUSICAL SCALE

AND

THE 22 SHRUTEES.

BY

Mr. K. B. Deval.

(Retired Deputy Collector.)

For more than the last eighty years, several attempts have been made to determine the Hindu Musical Scale with mathematical precision, by Indian and European scholars. But hitherto they have not been crowned with success; the solutions arrived at do not satisfy the tests of reason. Neither do they agree with conclusions noted by Sanskrit writers on Hindu Music. Hence it is that I propose to lay before the public a few thoughts about the Hindu Musical Scale and the lines of its development and progress. It might be stated here at the outset that the Hindu Musical Scale dates as far back as the Brahman Period which is calculated, according to modern researches, to extend from 2500 B. C. to 1400 B. C. It is possible that further researches might modify this date or might, perhaps, carry it still farther back. But we may be certain that our Scale dates farther back than the Greek Scale which is acknowledged to be the parent of modern European Scales. Capt. Day in his "Music of Southern India" observes:—"The Historian Strabo shows that the Greek influence extended to India, and also that Greek musicians of a certain school attributed the greater part of the science of music to India." The antiquity of the Scale apart, the most important point to be noted about it is that it is formed in consonance with the laws of the constitution of musical sound. It is a progressive Scale and the lines of its progress are laid down in old Sanskrit works on Hindu Music. The ancient sages of India, with their austere methods of study, meditating for years together in the quiet and tranquil recesses of nature undisturbed by the bustle of human habi-

tations, have preserved the results of their labours in their precious works, which excite even to-day the wonder and admiration of the cultured world. In recent times the attention of educated Indians turned to this Art of Arts, and men like the late Mr. Kunte, Messrs. Pingalé and Sahasrabuddhe, Mr. Banhatti, Raja Surendra Mohun Tagore, Mr. Chinnaswami Mudliar, have written copiously on Hindu Music. But difficult as the subject is, several points have been enshrouded in mystery, *e.g.* the Shrutees. In some of these recent publications there appear misinterpretations of shlokas from the Sanskrit works. Hence they have given rise to a number of wrong notions about the Hindu Musical Scale, and consequently about the value of Hindu Music, not only among Indians but also among scholars of the West. European writers on Hindu Music *e.g.* Capt. Willard ("Music of Hindustan"—a paper sent to the Society of Arts in 1834), Sir William Jones (paper on Musical Scales), Mr. Bosanquet (paper read before the Royal Society of Arts in London in 1877 on the Hindu Division of the Octave), Mr. Patterson, Captain Day (Music of Southern India), Mr. A. J. Ellis (paper read before the Society of Arts in 1885 on the Musical Scales of the World), have come to hold erroneous views about the theory of the Hindu Musical Scale. This might be due partly to their ignorance of the Sanskrit works on Music, partly to the erroneous information supplied to them by recent publications, and partly to the assumption that the Hindus must have followed a system similar to the equal 'temperament' system at present in vogue in Europe. In 1885, the late Mr. A. J. Ellis, the distinguished English physicist, scientist, and translator and editor of Helmholtz's "Sensations of Tone", in his paper on "the Musical Scales of the World", after comparing and examining the Scales of the various nations—among them the Hindu Musical Scale also—came to the following conclusion:

"The Musical Scale is not 'one', not 'natural', nor even founded necessarily on the laws of the constitution of Musical sound so beautifully worked out by Helmholtz, but very diverse, very artificial, and very capricious."

This I humbly submit cannot be said at least of the Hindu Musical Scale, as will be seen from the following. Now as observed by Professor Pietro Blaserna, of the Royal University

of Rome, in his valuable treatise on the "Theory of Sound in its Relation to Music", by a musical scale is meant "the collection of all the notes comprised between the fundamental note and its octave, which succeed each other and are intended to succeed each other with a certain pre-established regularity." "The musical scale is always the product of the musical activity of a nation extending over a number of centuries." Hence to allow such wrong impressions about the Hindu Musical Scale to stand permanently on record and to suffer them to prejudice the minds of Western and Oriental Scholars as to the rank which the Hindu Musical Scale should take in the musical scales of the world, is neither just nor reasonable when there exists abundant evidence to disprove the above allegations. To elucidate all the difficult points of so difficult and scientific a subject as Music requires an amount of labour, energy, and talent which is given to but a few; it is a stupendous task, and personally I feel it quite hazardous on my part to attempt to undertake it. But approaching the subject with the humility and diffidence of a student, I have pursued my attempts hitherto and I lay before the public the results of my humble labours.

2. It would be proper to state at the outset the laws of the constitution of musical sound which the ancient Sanskrit authors observed in their works on Hindu Music. In order to make this point quite clear, I place in juxta-position the laws observed by Sanskrit writers and those followed by modern scientists of renown.

Both make a clear distinction between *Sound*
and *Musical Sound*.

1. Sound.

European Scientists.

(a) Sound in our apprehension is that which is heard and therefore our only means of recognizing its existence is through the sensation on our ear. The auditory nerve alone can perceive sound.

(Holmes' *Vocal Physiology*—*Ed.* 1900—p. 52).

(b) Sound on the other hand is produced in our ears and is therefore subjective; but vibration is objective. It exists in sounding bodies independently of the listener. To a deaf man the vibration exists but the sound does not. Sound is the result of vibrations.*

Blaserna p. 27.

2. Musical Sound.

(a) Musical sound strikes us as being even, smooth and melodious like the tones of all musical instruments. *Holmes p. 61.*

* So does *संदन* (= vibration) exist to a deaf man and *श्रुति* (= sound) is the result of 'संदन'.

Authors on Aryan Music.

(a) श्रुति or (नाद) श्रु = to hear
श्रवणयोग्या एव श्रुतयः ।
रागविबोध आर्या १४ टीका.

(b) श्रवणेंद्रियग्राह्यत्वाद् ध्वनिरेव
श्रुतिर्भवेत्—विश्रावस्तु सं. रं. पृष्ठ १५.

(c) प्रथमश्रवणाच्छब्दः श्रुयते ह्रस्व-
मात्रकः सा श्रुतिः संपरिज्ञेया
स्वरावयवलक्षणा ॥

माघ सर्ग १. श्लोक १० टीका
also संगीत रत्नाकर.

(d) श्रुतिर्नाम = स्वरारंभकावयवः
शब्दविशेषः ।
माघ सर्ग १. श्लोक १० टीका.

(a)+(b) } May be translated
as follows :—
Any sound which
is heard by the ear
and } is a Shrutī श्रुति and
a श्रुति and sound are
(c)+(d) } one and the same
and are perceived,
because the ear
hears them.

(a) तंत्री-मेरु-सारी-संश्लेषोद्भवा ये
ध्वनयः ते श्रुतयः श्रुतिशब्द-
वाच्याः ॥
रा. वि. वि. १ आर्या २०

European Scientists.

(b) A note not accompanied by its *harmonics* may sometimes be sweet, but it is always thin and poor and therefore but little musical.

Blaserna p. 165.

(c) In order that a sound may acquire a musical character, it must satisfy the essential condition of being agreeable to the ear.

Blaserna p. 74.

3. Harmonics.

Harmonics defined.

Strings in vibrating do not only swing as a whole but have also several secondary motions, each of which produces a sound proper to itself. A string, when struck, vibrates first in its entire length, secondly in two segments; thirdly in three; fourthly in four, and so on. All of these motions are simultaneous and the sounds proceeding from them are blended into one note. The lowest note is the loudest and is called the fundamental or prime tone, and the others are called over-tones, upper partial tones or harmonics.

Holmes p. 69.

Authors on Aryan Music.

(b) श्रवणयोग्यता अनुरणनात्मकस्य
स्वराख्यस्य हीधेध्वनेवेतते.
रा. वि. आर्या १४ टीका.

(c) श्रुत्यन्तरभावी यः स्निग्धोऽनु-
रणनात्मकः । स्वतो रंजयति
श्रोतृचित्तं सः स्वर उच्यते ॥

सं. र. स्वराध्याय प्र० ३ श्लो० २३.

स्वरशब्दस्य व्याख्यानाहः—
मनः श्रोतृचित्तं स्वतः कारणान्तरनिरपेक्षं
अनुरक्तं कुर्वतीति स्वराः.
रा. वि. आर्या १४ टीका.

In Sanskrit, *Harmonics* are
called अनुरणनात्मकध्वनिः

(a) श्रुत्यन्तरभावी यः स्निग्धोऽनु-
रणनात्मकः ॥

स्वतो रंजयति श्रोतृचित्तं सः स्वर
उच्यते ॥

सं. र. श्लोक २३

(b) अनुरणनात्मको ध्वनिविशेषो-
यस्मात् संभवति तादृग्लक्षणो
उद्गीयात्—तथाप्रथमतंत्री बंधनीया-
रा. वि. आर्या १९ विवेक २.

(c) रणद्विराघटनया नभस्वतः
पृथग्विभिन्नश्रुतिमंडलेः (Harmo-
nics) स्वरैः ।

स्फुटीभवद्द्वयामविशेषमूर्च्छनामवे-
क्षमाणं महतीं सुहृत्सुहृः ॥

माघ सर्ग १ श्लोक १०.

वायोराघातेन पृथक् संकीर्णं

ध्वनद्विः अनुरणनोत्पद्यमानैः

स्फुटीभवांति... टीका.

The above Sanskrit piece marked (c) translated by Sir W. Jones runs as follows :—

× × “Nārada sat watching from time to time his large Veenā (sonometre or monochord) which by the impulse of breeze, yielded notes that pierced successively the regions of his ear, and proceeded by musical intervals.”

Pingale's treatise, p. 251.

It need hardly be noted here that the great sage Nārada perceived these Musical intervals (otherwise called harmonics) as arising from the whole length of the wire set free to vibrate on its own account and creating natural nodes and ventral segments as distinguished from artificial nodes and segments which it is necessary to produce (as will be seen in the sequel) in the construction of the Musical Scale.*

* Nārada's Veenā is called ब्रह्मवीणा Page 22 of “Hindu Music” Gayan Samaja.

महती is the name given to the ब्रह्मवीणा of Nārada in the stanza quoted here.

Here we have in the clear poetic way of Māgha, noted down a fact which ought to arrest our attention. Nārada is descending from the heaven to the earth and the wind strikes his *big lute* the Mahati. He was observing his instrument with the Murchhana of the several Gramas displayed or unfolded by the several Swaras (upper partial tones) each showing on the string its distinct successive ventral segments. Sir William Jones seems to have understood the word *Shruti* in the ordinary meaning of ear and not as the primary tone going to build up the secondary or upper partial or over tones. He interprets Mandala to mean regions or more scientifically, the encircling channels (of the ear). According to him the various Swaras pierced the various recep-

A string when rubbed is in a state of rapid vibration; at the extremities where it rests on two bridges, it appears to be at rest. But when the middle part is examined, it is found that the string loses its sharpness of out-line. It appears sensibly thickened and this thickening reaches its maximum at about the middle of the string which proves that each particle of the string performs a to and fro movement in direction perpendicular to the length of the string. Vibrations of this sort are called transverse. The most simple form of a vibration is that in which the whole string vibrates simultaneously in one single vibration. This effect can easily be obtained by *leaving the string quite free*. The note thus obtained is called the fundamental note. × ×

श्रुतिमंडलैः Ventral segments and the consequent production of harmonics as defined by Blaserna were observed by Nārada in vibrating strings which were set free to vibrate by the breeze.

What an amount of patient and careful observation must have been bestowed in the time of Māgha when the poet could describe the celestial musician Nārada as having detected by his eyes and ears these ventral segments and harmonics!

Somanāth refers to harmonics in his रागविबोध. In Aryas 30 and 31 he gives their importance; he calls them स्वयंभू notes. स्वस्मादेव भवतीति स्वयंभुवः! And again in commentary to आर्या 34, he states मेरुगतस्वयंभूस्वरपंक्तिप्रामाण्येन। स्वयंभू tones means harmonics or upper partial tones which

tive channels in regular order or succession. Whether we interpret the adjectival compound qualifying the Swaras in the Jonesian way or we do it in the method of Mallinath who draws out the meaning giving accurate quotations from works on Music, we can well understand that the Poet makes Nārada observe with amusement the action of the wind on the lute and note the same phenomena (Nodal points, Ventral segments and upper partial tones) as a modern European physicist may well observe with all the precision of his latest advanced notions of the theories of sound.

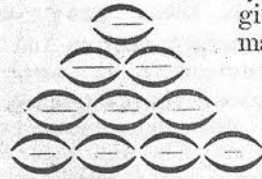
The foregoing interpretation of the Shloka has been accepted and found to be correct by Prof. V. G. Vijapurkar M. A., Prof. V. K. Rajwade M. A., Mr. Vinayakrao alies Annasaheb Patwardhan, Sardar K. C. Mehendale, Mr. Raddi Shastri of Elphinstone High School and other Sanskrit Scholars.

It would be interesting to note here that while Harmonics were unobserved by the Europeans as admitted by Blaserna till the latter half of the last century, it was a matter of common knowledge to the Hindoos at least as far back as the 6th century. Māgha makes a passing reference to it in his Sishupala-vadha which is a poem merely of general interest, which fact proves that in the days of Māgha general readers of poetic literature were expected to be familiar with the phenomena.

European Scientists.

But if the string be touched in the middle, a note which is double in pitch, which practical musicians call the *octave* of the fundamental note, is obtained. The string in this case vibrates in two parts in such a way that the point touched remains at rest. This fixed point is called a node of the vibrating string and has been produced artificially by touching the string at the point indicated. Successively higher and higher notes can be obtained by the string by touching it at a third, a fourth, a fifth of its length, etc. etc.

(Blaserna, Chapter I, pages 11-14).



By the figures given in the margin Blaserna has shown the different modes of

vibration which a string assumes in different cases when it vibrates as a whole or into 2, 3, 4 &c. parts. In the first case no node is formed, in the others we have one, two, three, &c. nodes. The parts of the string between the nodes which contain these points of maximum movements are called ventral segments. This is what we have in श्रुतिमंडलैःस्वरैः of Māgha.

Authors on Aryan Music.

are heard when the whole string resting on two fixed bridges is made to vibrate. He warns musicians to always test the correctness of their notes, wherever possible, by referring them to these स्वयंभू harmonics.

5. Reflection of sound.

European Scientists.

ECHO—The best understood of all the cases of reflection is that which is called ECHO.

—Blaserna, page 43.

The reflection of sound has been utilized in various ways. Nature and art have combined to solve some problems not unknown in history. The celebrated "ear of Dionysius" is well known; it is a sort of hole excavated in the rocks near Syracuse where the least sound is transformed into a deafening roar. Similar phenomena are often met with under the large arches of bridges, viaducts, &c. &c.

6. Sympathetic Resonance.

Experiment shows that whenever a body vibrates, other bodies placed near it, are able to enter into a state of vibration on this condition only that such bodies shall be capable by themselves of producing the same note.

Blaserna, Ch. II, p. 49.

What is the limit of audible sounds? Does our ear perceive as a note any number of vibrations

Author on Aryan Music.

सं. र. पान ३५ कोहल.

आनन्द्यं हि श्रुतीनां च सूत्रयन्ति
विपश्चितः ।

यथाध्वनिविशेषाणाममानं गगनोदरे ॥
टीका—तेषां अतिस्वल्पभागकल्पनयाऽमानघ.

(५) प्रतिध्वन्यवयवभूतध्वनिबहुत्व-
विवक्षयाऽऽनन्द्यं दर्शितम्
उत्तालपवनोद्देहजलराशिसमुद्भवाः ।
इत्ययः प्रतिपद्यन्ते न तरंगपरम्पराः ॥
रागविबोध, विवेक २, आयां ३२.

अष्टम्येकादशयोः सार्योरुध्वं समापर-
ध्वनितः ॥

तत्तैः समाः सपसमाः स्वयंभुवो मुक्त-
तन्त्रीजाः ॥

टीका—तत्तैरिति ॥ × × मंद्रप मध्यसम-
मध्यमानां स्वयंभूत्वाद्धेतोः तैः मंद्र-
पंचमादिभिः समाः । सदृशनादाः मुक्ततंत्री-
जाः मुक्ताः वामहस्तांगुलिश्लेषरहिताः याः
तंत्र्यः प्रथमादयश्चतस्रः ताभ्यो जाताः
सपसमाः अनुमंद्रषड्जानुमंद्रषड्जमंद्र-
मध्यमाः स्वयंभुवः ज्ञयाः इति शेषः ॥
नीचोच्चस्थाचकृत एवैषां भेदो न रूपभेद-
इत्यर्थः ॥ रा. वि. वि. २ आ. ३२.

7. Pitch.

According to Sanskrit writers there are five divisions of sound.

European Scientists.

whatever or is our perception confined between certain limits? Twenty or twenty-five vibrations just take place per second in order to produce appreciable note. The notes that are too low are badly heard and those that are too high are unpleasant.

Blaserna, pp. 66-67.

The well-known voice of a single singer embraces about two octaves. In the case of a woman a little more.

8. *Laws of the vibrations of strings and of artificially produced harmonics.*

Blaserna, pp. 71-72.

(1) When the whole string vibrates in one vibration, it gives its lowest note which is called the fundamental note.

If the whole string be touched in the middle with a finger, a higher note is obtained, which practical musicians call the octave of the fundamental note.

(2) If the string be divided by touching it with a finger or a feather into two, three, four, &c. parts, higher and higher notes are obtained which form that which is called "En-harmonic" series.

Authors on Aryan Music.

मत्तंगमते तु-सूक्ष्मश्रैवातिसूक्ष्मश्च व्यक्तो-
ऽव्यक्तश्च कृत्रिमः=सूक्ष्मनादो गुहावासी
हृदये चातिसूक्ष्मकः &c. पञ्चानामपि सा-
मान्येन गीतोपयोगित्वे प्रति हृत्कंठ-
मूर्धस्थाने एव गीतोपयोगित्वमाह अत्र
गानार्हा इति ।

रा. वि. वि. १ आर्या ११.

एवं पंचसु त्रयाणां गानोपयोग्यता ।

रा. वि. आर्या १२-१३.

नादोऽतिसूक्ष्मः सूक्ष्मश्च पुष्टोऽपुष्टश्च
कृत्रिमः ॥

इति पञ्चाभिधां धत्ते पञ्चस्थानस्थितः
क्रमान् ॥ (५)

व्यवहारे त्वसौ त्रेधा हृदि मन्द्रोऽभिधीयते ।
कंठे मध्यो मूर्ध्नि तारो द्विगुणश्चोत्तरोत्तरः ॥७॥

सं. र. पान ३२.

मेरुच्छिष्टतुर्यतन्त्रीरवे सः = षड्जः
अभिव्यज्यते । अत्र तन्त्री शब्देन तदु-
द्भवो रवो लक्ष्यते ।

The whole vibrating length of the string resting on the two fixed bridges (मेरु) gives a note (षड्ज) which in English is called the fundamental note.

द्वाविंशस्थिः षड्जः द्विगुणसमः ।

रा. वि. वि. १ आर्या २१.

मध्यस्थानस्थः षड्जः - द्विगुणित-
षड्जः द्विगुणप्रायः

A note double of the funda-
mental is obtained, if the wire is
halved. [रागविबोध]

European Scientists.

The notes of this harmonic series are not notes taken at random. They are very agreeable to the ear in relation to the fundamental note, and have great importance as we shall see in the sequel in the theory of musical instruments.

Tones increase in Pitch in the inverse ratio of the length of the Wire.

But it may be noticed that (in human voice) the larynx rises for the production of high notes.

9. *Simple ratios of consonant notes.*

It may be established as one of the fundamental principles of our music that the ear can endure notes, be they simultaneous or successive, on this condition—viz.—*that they should bear simple ratios to each other in respect of the number of their vibrations per second*, that is to say, that the ratio of the number of vibrations per second of the notes should be expressed by low numbers.

Blaserna. Chp. 5 sec. 2.

Authors on Aryan Music.

नीचोच्चस्थानकृत एवेषां भेदो न रूपभेदः
इत्यर्थः

रा. वि. वि. १ आर्या २१. टीका.

अत्यन्तरभावी यः स्निग्धोऽनुरणनात्मकः
स्वतो रंजयति श्रोतुश्चित्तं सस्वर उच्यते.

सं. र. आर्या २६.

अधराधर तीव्रा स्तास्तज्जो नादः श्रुतिमर्तः ।
टीका—तंत्र्योऽधराधरास्तीव्रा उच्चोच्चध्वनयो
भवन्ति.

तन्त्रीतंतुस्वरो ज्ञेयस्तद्वैद्यव्यस्तमानतः ।
तंतुस्थौल्येऽपि विज्ञेयस्तंतुसौक्ष्म्येऽप्ययं
विधिः ॥ शेष लीलवती.

यथा शरीरे श्रुतयः उत्तरोत्तरोच्चाः उ-
त्पद्यन्ते तथा वीणायां.

अधराउच्चा उत्पद्यन्ते—इति स्वारस्यम् ।
(सं. र. प्र. अ. प्रकरण ३ श्लोक १३.)

वायुःसोपानपरंपराविव आरोहात् अत्र
हृत्कंठ मूर्धस्थानेषु मरुतावाताभि-
व्यक्तान्नादान् कुरुते=(विद्युत्पत्ति)

रा. वि. आर्या १३. टीका.

संवादि स्वरः Sanskrit writers call notes which bear simple ratios to each other संवादि स्वर and the following extracts will show the importance which has been given to these simple-ratio-bearing-notes (otherwise called संवादि स्वर) by the Aryan authors of music as a science, and by musical composers.

संवादिनां समाजो रंजनकारी भवेदिति
न्यायात् ॥

नितं निःशंकादिभिरिहापि संवादि
सान्निध्यम् ।
रा. वि. १८.

The word न्याय may be translated by the English word 'law.'
टीका—संवाद=एककार्यत्वं येषामस्ति
तौदृशानां समूहः (समाजः) सहावास्थितिः
इति यावत् रंजनकारी रंजको भवेत् इति
लोकप्रघातः ।

Sharangdeo also in his Sangit Ratnakar (संगतिरत्नाकर) defines consonant sounds and divides them into 4 classes.

सं. र. प्र. अ. प्रकरण ३ श्लोक ४९.

चतुर्विधाः स्वरा वार्दी संवादीच
विवाद्यापि ।
अनुवादीच वार्दीतु प्रयोगे बहुलःस्वरः ॥
सं. र. प्र. ४९.

10. Beats.

When two notes not exactly of the same pitch and bearing intricate ratios are sounded together (a new phenomenon is observed known by the name of beats) a sound is obtained of varying loudness, now strong and now feeble, and very marked jerks or shocks are perceived. These shocks are the beats &c. &c.

If one of the two notes be slightly altered unpleasant beats are heard and they "spoil the harmony."

Blaserna Chapt. V,
Sec. 4, 5 and 6.

The Aryan and Sanskrit authors also describe in similar terms the unpleasant effect produced on our ear by the combination of notes bearing intricate ratios, which notes go by the name. विवादिस्वर एकश्रुत्यंतरितौ (having a difference of only one Shrutee or a quarter or a third of a note) विवादिनौ वैरिणौ मिथोभवतः ।
(आर्या ३८ रा. वि. विवे.)

टीका—विवादिनं लक्षयति—× ×
संवादि अनुवादिजनितरागरक्तिविना-
शकत्वात् विवादिनौ भवतः । विवादिस्व-
यथा—ऋषभस्य गांधारः ॥

विवादि note as defined by Sharangdeo पृष्ठ ४३ श्लोक ४९ टीका.

विषदनाद्विवादि । विषदने नाम वाद्या-
दिभिः स्वरैरुत्पाद्यमानरक्तः विनाशकत्वं
(here रक्ति means harmony. रंजन
—pleasure &c. &c.)

11. Resultant notes or difference notes.

Blaserna in sec. 6 Chapter 5.

Whenever any two notes bearing simple ratios are combined, besides these two notes a low note is very clearly heard (i. e. when two notes making 200 and 250 vibrations per second are sounded, a third note corresponding to 50 vibrations per second is heard. This number is 4th part of 200 or the half of the half). This note is called the resultant or difference note. Its pitch or strength or the number of vibrations is equal to the difference between the two combined notes. This third note is agreeable to the ear, because it arises or is the result of two combined notes which bear simple ratios to each other. It, therefore, forms a consonant part of any one of the two notes combined and thus supports harmony.

"If then several notes be combined" observes Blaserna "it is not enough to select those which by themselves will give an agreeable harmony; it is necessary further to examine the resultant notes and to see how these will behave in relation to the combined notes."

After describing the Veenâ (a stringed instrument of the time of Nârada) the author of Râgavibodha in Arya 19 and in its commentary gives instructions as to how to tune the 4 strings on the said instrument.

अनुमंत्रणञ्जमहेनुमन्त्रे पं द्वितीयका तंत्री ।
मंद्रं संच तृतीया चतुर्थिका मध्यमं
मंद्रं ॥ ३९ ॥
रा. वि. वि. २.

If translated it is as follows:—

The first string should be so tuned as to give the fundamental note. The second to give its 5th, the 3rd to give the octave, and the 4th to give F, the fourth of the octave. Now supposing the fundamental note gives 24 vibrations per second, we find out the following vibrational values of the 4 notes combined.

C or षड्ज=24	} 12	Now if we find out the values of the resultant notes they are as noted in the margin.
G or पंचम=36		
C' or षड्ज=48		
F' or मध्यम=64		

European Scientists.

The discovery of these resultant notes was made towards the middle of the 18th century and is generally attributed to the celebrated violinist Tartini.

The next most simple ratio that can be imagined after unison is that of 1 to 2. This is the ratio called that of the octave.

3. From the foregoing comparison of the fundamental laws of the constitution of musical sound, adopted by modern scientists, and those observed by our old Sanskrit writers, it will be clear that in constructing their musical scale the Aryan authors proceeded on scientific lines. How from these laws the Diatonic scale of seven notes, or the स्वरसप्तक was formulated may be noted below. It may be stated that the rule of perfect concord and of harmonics was strictly observed in the construction of the musical scale. An explanation of the ordinary terminology in Sanskrit musical works would help towards understanding the subject: मेरु=fixed bridge; moveable fret=सारिका; शुद्धसंवाद=unison or the relation

Authors on Aryan Music.

This very same principle has all along been strictly observed both by the celebrated *Rishi Nārada* (who is called the father of music) during the Vedic period and also by instrumentalists and composers of subsequent periods. × How the first two resultant notes form into the lower octave of the fundamental note $\frac{2}{3} = 12$ how the 3rd note viz: of 32 vibrational value forms into lower octave of $F'' = \frac{1}{2} = 32$ and how these 3 support the original 4 notes and how they thus contribute to the harmony of the whole instrument, may be more easily heard and enjoyed than described.

द्वाविंशतिस्थः षड्जः द्विगुणसप्तः पूर्वं षड्जिनः मध्यस्थानस्थः षड्जः ।
यथा पूर्वीकस्थापनया, मध्यषड्जेन-
सह मन्द्रषड्जस्य मेरुस्थस्य संवाद
(agreement complete) साशुद्धेति
विश्रयः । रा. वि. वि. १ आ. २१, २२.

between notes bearing the ratio of an octave; सुहृत्संवाद= perfect concord, ratio of 2 : 3, अनुवाद = imperfect concord, ratio of 4 : 5 or 5 : 6; विवाद = dissonance. They lay down that the rule of perfect concord should be observed strictly in forming musical scales. The lengths which will be given for the several notes in the Diatonic scale below, are those of the wire of the Diachord, whose length, I take to be 36 inches; each inch being further divided into 20 subdivisions, which I call lines. I also take 240 vibrations for the fundamental note सा. In the Diachord are two strings or wires, resting on two fixed bridges, one at each end. When experiments are to be made, we have to tune one string to give out a note which may be called the fundamental note. The other string is to be tuned so that it may be in full unison with the first. When the two strings are thus tuned, then the moveable bridge is to be moved about for producing the required notes. Its height must be such as to leave no distance whatsoever between the string and the bridge, yet not pressing the string upward. One of the strings is to be left free to vibrate on its whole length, giving the fundamental note, while the different notes required are to be produced on the other. On moving the bridge to the distance required for producing a note, the string is to be pressed very lightly to the edge of the bridge with the finger-nail, so as not to increase the tension in the least. Then the exact note will be produced on sounding the string. To get the exact note on the given length, it is necessary that there should not be any disturbing element such as increased tension caused by pressing the string downward to the bridge. This depends on the accuracy of the instrument.

How the positions and vibrations of the 7 notes of the Diatonic Scale and the octave, have been settled with mathematical precision is shown below.



The Seven Notes: स₁ (c₁) to स₂ (c₂).

Notes	(1) C	(2) D	(3) E ^a	(3) ^b E ^b	(4) F	(5) G	(6) A	(7) ^a B ^a	(7) ^b B ^b	(8) C ₂
	प	ध	नी	स ₁	री	ग	२८ $\frac{1}{2}$	२८ $\frac{1}{2}$	२८ $\frac{1}{2}$	२८ $\frac{1}{2}$
Vibrations	36	32	300	320	360	405	450	480	480	480
Ratios	1	9/8	5/4	4/3	3/2	2/3	1/2	1/2	1/2	2

स₁ (C₁) and स₂ (C₂).

१. मेरुदिलद्वयतुल्यतन्त्रीरवे सः षड्जः
अभिव्यज्यते.

(रागविबोध-वि. १ आर्या २१).

Rule (1) *The whole length of the wire between the two fixed bridges gives the fundamental note स¹ (c¹).*

Let the length of the wire be 36", the note produced be called स₁ (c₁) and let its vibrations be 240 per second.

२. मध्यस्थानस्थः षड्जः द्विगुणसम
(रा. वि.)

Rule (2) *The note produced on half the length is in value equal to स₁ (c₁) and in pitch or vibrations it is double the fundamental note (F. N.)*

The note produced on the length 18" is therefore स₁ or c₁ itself, but one octave higher. Let this note be called स₂ or c₂ to distinguish it from c₁ or स₁, the F. N.; then the vibrations of स₂ or c₂ are double i. e. 2 × 240 = 480 per second.

३. तन्त्रीतनुस्वरो ज्ञेयः तद्वैर्ध्वव्यस्तमानतः ।

(शेष लीलावती.)

Rule (3) *The pitch of a note or its vibrations are inversely proportional to the length of the wire.*

This rule is a legitimate inference from the above two rules. Rule (1) permits us to take any length for the Fundamental Note (F. N.) and according to Rule (2) if the length is halved the pitch is doubled, and if the length is doubled the pitch or the number of vibrations is halved. If therefore 1/3rd length is taken the pitch or the number of vibrations produced will be trebled. Or by generalization :

Rule (4) *The pitch varies inversely as the length and vice versa.*

The above four rules may therefore be put in the form of a simple Formula for convenience of working and ready reference.

Let V_n = Vibrations or pitch of the note on wire l_n inches long. uⁿ = The vibrations or pitch of स₁ (c₁) the F. N., here = 240

l = The length of the wire of the F. N, here = 36 Inches = 36".

Then :

$$V_n \times l_n = u \times l \dots \dots \dots (A)$$

$$V_n = u \times \frac{l}{l_n} \dots \dots \dots (B)$$

$$l_n = u \times \frac{l}{V_n} \dots \dots \dots (C)$$

therefore if V_n = 2u

$$l_n = \frac{l}{2} \dots \dots \dots (D)$$

म (F).

४. मध्यस्थानस्थः मध्यमः । (रा. वि.)

उभयोः षड्जयोर्मध्ये मध्यमं स्वरमाचरेत् ।

(संगीत-पारिजात.)

Rule (5) *The note म (For the fourth note) is produced at the middle of the Fundamental Note and its octave.*

The note म is therefore produced at half the length of स₁ (c₁) and स₂ (c₂) or at $\frac{1}{2}$ (36'' + 18'') = $\frac{1}{2}$ (54'') = 27''. In other words the note of the wire 27'' or 27'' inches of the executive part of the wire will give out the 4th note or म (F) and by Rule (4) formula (B) the pitch or vibrations of म (F) are equal to 320.

The formula (B) is :—

$$V_n = u \times \frac{l}{l_n}; \text{ Here } u = 240, l = 36 \text{ \& } l_n = 27$$

$$V_n = 240 \times \frac{36}{27} = 320 = \text{Vibrations of म}$$

And formula (C) is :—

$$l_n = u \times \frac{l}{V_n} \therefore l_n = 240 \times \frac{l}{320} = \frac{3}{4} l = \frac{3}{4} \times 36$$

or the length of म is $\frac{3}{4}$ of the length of the F. N. and the vibrations of म are $\frac{4}{3}$ of the F. N. and it may be laid down :—

Rule (6) *That the length of the wire of म (F) or the 4th note is $\frac{3}{4}$ of that of the Fundamental Note and the vibrations of म (F) are $\frac{4}{3}$ of the vibrations of the Fundamental Note स₁ (c₁).*

प (G).

५. त्रिभागात्मकवीणायां पंचमःस्वात्तद्विधे । (संगीत-परिजात.)

Rule (7) *The fifth or प (G) note is produced on $\frac{1}{3}$ or $\frac{2}{3}$ of whole length of the wire. The former note is one octave higher than the latter.*

The length of the wire is 36''. Therefore a length of 12'' or 24'' will give the fifth note प (G). But we want the length between 18'' and 36''—the two limits of the octave. Therefore the length 24'' is that which we require and it will give out the note प (G).

Let us apply the formulæ (B) and (C) to the case of प (G).

$$V_n = u \times \frac{l}{l_n} \dots \dots \dots (B)$$

Substitute the values $u = 240, l = 36$ and $l_n = 24$

$$\therefore V_n = 240 \times \frac{36}{24} = 360 = \text{Vibrations of प (G)}$$

$$= u \times \frac{36}{24} = \frac{3}{2} u$$

or the Vibrations of प (G) are $\frac{3}{2}$ of its स₁ or F. N.

and

$$l_n = u \frac{l}{V_n} \dots \dots \dots (C)$$

$$\therefore l_n = \frac{240}{360} \times l = \frac{2}{3} l = 24$$

or the length of प is $\frac{2}{3}$ of its स₁ (c₁) or F. N.

These facts may be noted down under Rule (8) below :—

Rule (8) *The length of the wire of प (G) or the fifth note is $\frac{2}{3}$ of that of स₁'s (c₁) wire and its vibrations or pitch is $\frac{3}{2}$ of that of स₁ (c₁).*

री (D) and ध (A).

६. स-प-स-मसुख्याः संवादिनः स्वराः एकसंभवाः प्रायः । (रा. वि.)

Rule (9) *In the interval of a given octave, स₁ (C₁) with प (G) and म (F) with स₂ (C₂) form perfect concords; it may be noted that स₁ (C₁) with म (F) and प (G) with स₂ (C₂), the inverted interval, form imperfect concords.*

This rule is very important and is made use of in finding out the lengths and vibrations of the other notes री, (D), ग (E), &c. &c.

According to Rule (1) any length may be said to give the fundamental note and its पंचम will be the 5th note from it. This पंचम or प will form a perfect concords with it.* This gives us the following consonant notes.

F. N. स₁ (c₁).

Consonant note प (A) or म (F).

स C₁

प G

री D

ध A

ग E

नी B

म F

स₂ C₂

प G

री₂ D₂

स₂ C₂

प₂ G² or प G

* As I proceed to show, ग₂ (E₂) is not a perfect pancham with प (A); nor is म₂ (F₂) with री (B).

Let us take ग (G) itself as the starting or fundamental note then its पंचम or fifth will be ञ D in the higher octave which may be called ञ₂ D₂. Apply the formula (B).

$$V_n = u \frac{l}{l_n}; \text{ Here } u = 360, l = 24 \text{ and } l_n = \frac{2}{3} \times 24; \therefore l_n = 16$$

Rule (7). Substituting the values of $u, l,$ and l_n

$$V_n = 360 \times \frac{24}{16} = 540.$$

540 are the vibrations of ञ₂ or ञ (D) in the 2nd octave. Therefore the vibrations of ञ in the first octave are $= \frac{1}{2} \times 540 = 270$ Vide Rule (2).

Formula (C) is—

$$l_n = u \times \frac{l}{V_n}; \text{ substituting } u = 240, l = 36 \text{ and}$$

$V_n = 270,$ we have

$$l_n = 240 \times \frac{36}{270} = 32. \text{ Hence—}$$

Rule (10) The length of ञ (D) is 32 inches and its vibrations are 270 or the length is $\frac{2}{3} l$ and vibrations $\frac{3}{2} u$.

घ (A).

Rule (11) The length of ञ is 32". If we take this as the starting note, then its पंचम is घ. Therefore the length of घ is $\frac{2}{3}$ of 32 = 21 $\frac{1}{3}$ by Rule (8) and its vibrations are $\frac{3}{2}$ of 270 = 405.

ग (E) and नि (B).

The length of घ (A) is 21 $\frac{1}{3}$ and its vibrations are 405. Let us take घ as the fundamental note (Rule 1); then ग² (E) or ग, धार in 2nd octave becomes its पंचम or the 5th note (Rule 9). Therefore its length is $= \frac{2}{3} \times 21\frac{1}{3}$ and vibrations $= \frac{3}{2} \times 405$; but these are for ग₂. Therefore according to Rule (2) The length of ग is $= 2 \times \frac{2}{3} \times 21\frac{1}{3}$

$$= 2 \times \frac{2}{3} \times \frac{46}{3} = \frac{256}{9} = 28\frac{4}{9}.$$

$$\text{and the vibrations of ग} = \frac{1}{2} \times \frac{3}{2} \times 405 = \frac{1215}{4} = 303\frac{3}{4}.$$

नि (B).

The length of ग is 28 $\frac{4}{9}$ and its vibrations 303 $\frac{3}{4}$ (Rule 12). If we take ग as the Fundamental note, then नि becomes

its पंचम or the fifth note. Therefore the length of नि $= \frac{2}{3} \times 28\frac{4}{9} = \frac{2}{3} \times \frac{256}{9} = \frac{512}{27} = 18\frac{8}{27}$ and the vibrations of नि $= \frac{3}{2} \times 303\frac{3}{4} = \frac{3}{2} \times \frac{1215}{4} \times 1 = \frac{3645}{8} = 455\frac{5}{8}.$

ग (E) and नि (B).

again

Rule (12) If the vibrations of ग (E) be taken at 300 (and there is a reason for doing so) in place of 303 $\frac{3}{4}$ as obtained in Rule (2) above, then

$$l_n = u \frac{l}{V_n} \dots \dots \dots (C); u = 240, l = 36 \text{ and } V_n = 300$$

$$\therefore l_n = \frac{240 \times 36}{300} = \frac{144}{5} = 28\frac{4}{5}$$

Hence the length of ग = 28 $\frac{4}{5}$ and its pitch = 300.

[The ग (E) obtained by the foregoing process has 303 $\frac{3}{4}$ vibrations and bears with the F_n Note a complicated ratio viz. 81 : 64. The ग (E) obtained as the fifth harmonic when reduced by two octaves has 300 vibrations and bears with the F_n Note the simple ratio of 5 : 4; and it sounds more consonant with it. It is clearly heard on the bass string (the fourth, giving सा or F. Note) of the Vina. Sanskrit writers have adopted this in preference to the other. They tested their notes by harmonics; the author of रागविबोध clearly lays down : मेरुगतस्वयंभुस्वरपंक्तिप्रामाण्येन । रा. वि. विवेक २ आर्या ३५ टीका.]

नि (B).

Rule (13) If ग (E) is taken as the fundamental note, then नि (B) becomes its पंचम the fifth in the same octave.

$$\therefore 300 \times \frac{3}{2} = 450 = \text{the vibrations of नि by Rule (8);}$$

$$\text{and the length is } \frac{2}{3} \times 28\frac{4}{5} = \frac{2}{3} \times \frac{144}{5} = \frac{288}{5} = 19\frac{3}{5} = 19\frac{1}{3}$$

$$\therefore \text{The vibrations of नि} = 450$$

$$\text{and the length of नि} = 19\frac{1}{3}.$$

Notes and Summary.

1. The lengths and vibrations of सा₁ (c₁) and सा₂ (c₂) are directly derived from Rules 1-2-3 which are based on the directions distinctly laid down in old Sanskrit works on Music—रागविबोध, संगीत-पारिजात and संगीत-रत्नाकर.

2. Rule 4 expresses in the form of formulae the results of the above rules. The formulae which are derived from formula A are given below for the convenience of ready reference.

$$\left. \begin{aligned} V_n \times l_n &= u \times l \dots\dots(A) \\ V_n &= u \frac{l}{l_n} \dots\dots (B) \\ l_n &= u \frac{l}{V_n} \dots\dots(C) \\ l_n &= \frac{1}{2} l \dots\dots(D) \end{aligned} \right\} \begin{array}{l} \text{where } V_n = \text{Vibrations of the length } l_n \\ \text{where } u = \text{Vibrations of length } l, \text{ which} \\ \text{are respectively 240 and } 36'' \end{array}$$

The rules are not discoveries of new truths in the science of the theory of Music. But they prove that these truths were known to Sanskrit writers on Music several centuries ago.

3. Rule (5) gives the length of ऋ (F) the 4th note as prescribed by रागविबोध. Rule (6) notes down the length and vibrational value of ऋ (F) as worked out from the rules.

4. Rule (7) determines the position of ऋ (G), the 5th note, its length on the diachord and its vibrations. Rule (8) notes down the length and vibrations of ऋ (G) the fifth note in general in any octave.

The positions, length and vibrations of स₁ (c₁), ऋ (F), ऋ (G) and स₂ (c₂), the 4 principal notes which have consonance of the first order, are thus marked down, worked out and settled. It now remains to find out the same of the remaining notes viz. री (D), ग (E), ध (A) and नि (B). This is done by the rule of संवादित्व of the 5th note ऋ (G) which may be called the rule of perfect concord.

5. Rule (9) describes in full the rule of perfect concord and how it may be used in finding out satisfactorily every thing required to be known of the remaining 4 notes—री, ग, ध and नि.

6. Rules (10) and (11) show how the lengths and vibrations of री and ध may be found from those of ऋ (G) by applying the rule of perfect concord.

7. Rule (12) and (13) show how the lengths of ग (E) and नि (B) are determined, the first by imperfect concord with स₁ (C₁) and the second by perfect concord with ग (E).

8. The lengths and vibrational values of all the notes in an octave are thus found out, by means of rules distinctly laid down in old Sanskrit works on Hindu Music such as रागविबोध, संगीत-पारिजात and संगीत-रत्नाकर.

9. I give below Table A, the Diatonic Major Scale तीव्र स्वर सप्तक showing the number of Shrutees assigned to each note,† the number of vibrations, lengths of wire of the Diachord, the number of Mr. Ellis' cents,* the musical intervals between any two consecutive notes of the scale, the ratios of each note with the fundamental note, and the English names of the intervals and notes :—

10. Now on looking at this table it will be seen that there are three kinds of musical intervals viz. 8:9, 9:10 and 15:16. In the scale the interval 8:9 occurs three times, 9:10 occurs twice and 15:16 occurs twice. The seven intervals form two trichords : the intervals between स and रि, रि and ग, and ग and ऋ forming the first trichord ; while those between ऋ and ध, ध and नि, and नि and सं, forming the second trichord. Each interval of the first trichord exactly allies with the corresponding interval of the second trichord. The interval between ऋ and ऋ (8:9) stands as a neutral zone between the two trichords. It is interesting to see that these intervals are evenly distributed. The interval between स and रि (8:9) which is the largest, occurs between ऋ and ध of the second trichord. The smaller interval between रि and ग (9:10) of the first trichord also lies between ऋ and नि of the second trichord. The smallest interval 15:16, which lies between ग and ऋ also appears between नि and सं (octave) of the second trichord. The total of Mr. Ellis' cents for these intervals is 1200.

11. Similarly we might note with interest the Diatonic Minor Scale (क्रोमल स्वर सप्तक,) shown in Table B given below. It consists of eight notes including the upper Octave, like the Major Scale तीव्र

† The assignment of Shrutees in Column 2, to the different notes is based on the following Aryā (आर्या) in रागविबोध (विवेक १. आ. २१):—

ऋषभस्तृतीयसार्या गःपंचम्यां नवम्यां मः ।
पस्तु त्रयोदशीस्थः षोडशी, अष्टादशी च ध, नी ॥
द्वाविंशीस्थः षड्जो द्विगुणसमः पूर्वषड्जैः ॥

For the explanation of the word श्रुति, I would draw the attention of the reader to Paragraphs 17 and 20.

° By dividing the interval between the fundamental note of value one (1) and its octave of double the value i.e. two (2), into 1200 cents, according to his method, Mr. Ellis has devised a system for measuring the various intervals. This system, into the details of which we need not go at present, he used for testing the scales of the world. It would be gratifying to learn that the Hindu Musical scale stands this test of cents admirably.

स्वर सप्तक. It will be seen that in place of major second ती. ग., major third ती. ग., major sixth ती. ध. and major seventh ती. नि. are inserted four corresponding flat notes or कौमल स्वराः. It is very interesting to note that the seven musical intervals are the same as those of the major Scale, but are differently distributed. So also are the ratios of each note with the fundamental note. The total of cents assigned to these intervals also comes to 1200. There are different modes (राग) and modulations (रागिणी) which are sung in the notes of this Diatonic Minor Scale.

12. It will be seen from the Diatonic Major Scale (Table A) that the smallest interval is 15:16 that between ग and म, and नि and स and this interval is used in forming our Chromatic Scale of twelve notes. Perhaps here a question may be asked as to why the particular interval of 15:16 is used in formulating the chromatic scale of twelve notes. To this question the simple answer is as follows. When we look at the seven musical intervals of the Diatonic Major Scale we find that out of these seven, five are large intervals and two are the smallest viz. those of 15:16 between ग and म, and नि and स. Sanskrit writers have termed the musical Scale as "a ladder"—सोपानपरंपरा (संगितरत्नाकर प्रकरण ३, श्लोक १३). They have formed out of this Diatonic Major Scale of seven notes a Chromatic Scale of twelve notes, by putting four more smaller notes or steps. They have also styled म, the fourth note or step of the Diatonic Scale, as कौमल; this is the smallest step of the musical ladder. Now it is evident that in introducing minor notes the smaller ratios or intervals will have to be utilized. Thus we get a method for developing our Scale by introducing minor notes.

13. Proceeding thus, while forming our Chromatic Scale of twelve notes, the smallest interval 15:16 is introduced between the four notes of the Diatonic Scale having larger intervals viz. 8:9 and 9:10. The interval between स and ती. रि. is 8:9. This is the biggest step. An interval of 15:16 is introduced between these two notes. Thus we obtain a third note called को. रि. with 256 vibrations, स being of 240 vibrations. Now स stands to को. रि. in the ratio of 15:16 and को. रि. stands to ती. रि. in the ratio of 128:135. Assigning Mr. Ellis' cents to these intervals, we get for 15:16, 112 cents and for 128:135, 92 cents. The larger interval of 8:9 having

204 cents is thus split up into two smaller ones of 92 and 112 cents respectively, making a total of 204 cents. The same ratio 15:16 is again introduced in the second half of the scale between म and ध. And the results are similar. In this manner we have got को. रि. and its corresponding संवादि note (consonant) in the second half viz. को. ध. Again similarly we divide the larger interval of 9:10 as before by the introduction of a smaller one of 15:16. Thus we get को. ग. of 288 vibrations, ती. ग. being of 300 vibrations. The interval between ती. रि. and को. ग. becomes 15:16, and has 112 cents; and that between को. ग. and ती. ग. becomes 24:25 and has 70 cents. These two smaller intervals make up the 182 cents which was the number for the second larger interval of 9:10. Similarly we have introduced को. नि. between ती. धे. and ती. नि., with 432 vibrations and having a ratio of 15:16 with 112 cents. The interval between को. नि. and ती. नि. is 24:25 with 70 cents. Thus we have in place of the seven notes of the Diatonic Scale, or eight including the upper octave, the following twelve notes of the Chromatic Scale viz. 1 स + 2 रि + 2 ग + 1 म + 1 प + 2 ध + 2 नि + 1 स = 12. Between म and प which with स form the backbone of our scale, we insert a note called ती. म. This note is the 5th harmonic of ऋ and therefore forms अनुवाद with it. स and प are kept fixed and unchangeable. [षड्जपञ्चमयोरविकृतत्वात् । विदे रा. वि. वि. ३ आर्षा < टीका.] Now by inserting smaller intervals of 15:16 between the larger ones of 8:9 and 9:10, we have introduced four कौमल or flat notes into the two trichords or halves of the scale, two in each; making in all eleven intervals for 12 notes. In order to show that these intervals are just and mathematical, Mr. Ellis' cents are given, and each interval is given its English name. The total of these cents for the various intervals is 1200. These are the very notes of the Chromatic Scale of twelve notes which we actually sing and play. It is to be noted here that the twelve frets which are fixed on the Sitar (सतार) as अचल थाद, are intended to give out the twelve notes of this Chromatic Scale and not any other. The foregoing results are given in Table C.

TABLE A.

तंत्रि स्वरांचे स्वर—सप्तक (वरील षड्ज धरून आठ स्वरांचे). Indian Diatonic Major Scale.

1	2	3	4	5	6	7	8	9	10	11
Serial No.	Shrutees.	Names of Notes.	Vibrations.	Musical Interval.	Its name.	Ellis' cents.	Ratio of each note with the Fundamental Note.	Its name.	Ellis' cents.	Vibrating length of wire required for each Note.
1	0	षड्ज or C	240	8 : 9	Major 2nd	204	8 : 9	Major 2nd; 9th Harmonic ...	204	36
2	3	ऋषभ or D	270							
3	5	गांधार or E	300	9 : 10	Minor 2nd	182	4 : 5	Just Major 3rd; 5th Harmonic ...	386	32
4	9	मध्यम or F	320	15 : 16	Diatonic Semitone	112	3 : 4	Just and Pythagorean fourth ...	498	28-16 lines
5	13	पंचम or G	360	8 : 9	Major 2nd	204	2 : 3	Just and Pyth. Fifth 3rd Harmonic...	702	27
6	16	धैवत or A	405	8 : 9	Major 2nd	204	16 : 27	Pythagorean major 6th; 27th Harmonic.	906	24
7	18	निषाद or B	450	9 : 10	Minor 2nd	182	8 : 15	Just major 7th; 15th Harmonic ...	1088	21-6 $\frac{2}{3}$ lines
8	22	षड्ज or C'	480	15 : 16	Diatonic semitone	112	1 : 2	Octave ...	1200	19-4 lines
						1200				18

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TABLE B.

कोमल स्वरांचे स्वर—सप्तक (वरील षड्ज धरून आठ स्वरांचे) भैरवी धादाचे. Indian Diatonic Minor Scale of 5 flat notes or 8 notes including the Fundamental, note the Fifth and Octave.

1	2	3	4	5	6	7	8	9	10	11
Serial No.	Names of Notes.	Vibrations.	Musical Interval.	Its name.	Ellis' cents.	Ratio of each note with the Fundamental Note.	Its name.	Ellis' cents.	Vibrating length of wire required for each Note	Remarks.
1	षड्ज or C.	240	15 : 16	Diatonic semitone.	112	15 : 16	Diatonic semitone.	112	36	33-15
2	को. ऋषभ or D flat.	256								
3	को. गांधार or E fl.	288	8 : 9	Major 2nd.	204	5 : 6	Just Minor 3rd	316	30-0	
4	को. मध्यम or F.	320	9 : 10	Minor 2nd.	182	3 : 4	Just fourth.	498	27-0	
5	को. पंचम or G.	360	8 : 9	Major 2nd.	204	2 : 3	Just fifth.	702	24-0	
6	को. धैवत or A fl.	384	15 : 16	Diatonic semitone.	112	5 : 8	Just minor 6th.	814	22-10	
7	को. निषाद or B fl.	432	8 : 9	Major 2nd.	204	5 : 9	Just Minor 7th.	1018	20-0	
8	षड्ज or C'.	480	9 : 10	Minor 2nd.	182	1 : 2	(Sometimes called accute.) Octave.	1200	18-0	
					1200					

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TABLE C.

1	2	3	4	5	6	7	8	9	10	11
Serial No.	Names of Notes.	Vibrations.	Musical Interval.	Its name.	Ellis' cents.	Ratio of each note with the Fundamental Note.	Its name.	Ellis' cents.	Vibrating length of wire required for each Note.	Remarks.
1	षड्ज or C ...	240	15 : 16	Diatonic semi-tone.	112	15 : 16	Diatonic semi-tone.	112	Inches—lines	
2	को. ऋषभ D fl. ...	256		Small Limma.	92					
3	ऋषभ or D ...	270	128 : 135	Diatonic semi-tone.	112	8 : 9	Major 2nd: 9th Harm.	204	33—15 32—0	
4	को. गंधार E fl. ...	288		Small Semitone.	70					
5	गंधार or E ...	300	15 : 16	Diatonic semi-tone.	112	5 : 6	Just minor 3rd	316	30—0	
6	को. मध्यम or F fl. ...	320		Small Limma.	72					
7	ती. मध्यम or F. ...	337½	128 : 135	Diatonic semi-tone.	112	4 : 5	Just major 3rd 5th Harm.	386	28—16	
8	पंचम or G ...	360		Small Limma.	72					
9	को. धैवत or A fl. ...	384	15 : 16	Diatonic semi-tone.	112	32 : 45	Just tri-tone: 45th Harm.	590	24—0	
10	धैवत or A ...	405		Small Limma.	92					
11	को. निषाद or B fl. ...	432	128 : 135	Diatonic semi-tone.	112	2 : 3	Just fifth.	702	22—10	
12	निषाद or B ...	450		Small semitone.	70					
13	षड्ज or C' ...	480	15 : 16	Diatonic semi-tone.	112	8 : 15	Just Major 7th: 15th Harm.	1018	20—0	
					1200	1 : 2*	Octave.	1088	19—4	
								1200	18—0	

The English names of the musical intervals in Col. 5 and of the ratios in Col. 8 are taken from the table of Harmonics on page 22 and the table of musical intervals on pages 453-56 of Helmholtz's "Sensations of Tones."

TABLE D
(Referred to at page 3)

Table D cont.

Indian Chromatic Scale of twenty-two

1	2	3	4	5	6	7	8	9	10	11	
No.	Name and kind of Shrutees. श्रुतिनाम, जाति.	Name of notes.	Vibrations	Musical interval lying between each pair of notes.	Its name.	Ellis' cents assigned to each interval	Ratio of each note with the Fundamental Note.	Its name.	Ellis' cents assigned.	Vibrating length of wire required for each note.	No.
(0)	छंदोवती, मध्या.	ष or C.	240	24 : 25	Small semitone.	70				Inches. Lines.	
(1)	इयावती, करुणा.	अ. को. क. Dff.	250	125 : 128	Great Disis.	42	24 : 25	Small semitone.	70	36-0	(13)
(2)	ईजनी, मध्या.	को. क. Df.	256	24 : 25	Small semitone.	70	15 : 16	Diatonic or Just semitone.	112	34-11½	(14)
(3)	रतिका, वृद्ध.	म. क. D.	266½	80 : 81	Comma of Didymus.	22	9 : 10	Minor second.	182	33-15	(15)
(4)	रौद्री, वीसा.	ती. क. Ds.	270	243 : 256	Pyth. Lihma.	90	8 : 9	Major second: 9 Harm.	204	32-0	(16)
(5)	क्रोधा, आयता.	अ. को. गं. Eff.	284½	80 : 81	Comma of Didymus.	22	27 : 32	Pyth. Minor Third.	294	30-7½	(17)
(6)	बज्रिका, वीसा.	को. गं. Ef.	288	24 : 25	Small semitone.	70	5 : 6	Just Minor Third.	316	30-0	(18)
(7)	प्रसारिणी, आयता.	ती. गं. Es.	300	80 : 81	Comma of Didymus.	22	4 : 5	Just Major Third: 5 Harm.	386	28-16	(19)
(8)	मीती, वृद्ध.	त. ती. गं. Ess.	303½	27 : 28	Septimal Comma.	63	64 : 81	Pyth. Major Third.	408	28-0	(20)
(9)	मार्जनी, मध्या.	अ. को. म. Fff.	315	63 : 64	Septimal Comma.	27	16 : 21	21st Harm., Sub F.	471	27-8½	(21)
(10)	सिती, वृद्ध.	को. म. Ff.	320	128 : 135	Small Lihma.	92	3 : 4	Just and Pyth. Fourth.	498	27-0	(22)
(11)	रक्ता, मध्या.	ती. म. Fs.	337½	125 : 128	Gr.	42	32 : 45	Pluperfect Fourth. 45 Harm.	590	25-12	
(12)	संहीपनी, आयता.	त. ती. म. Fss.	345½	24 : 25	Small semitone.	70	25 : 36	Acute dimi. Fifth.	632	25-0	
(13)	आलापिनी, करुणा.	पं. G.	360			702	2 : 3	Fifth. Just and Pyth.	702	24-0	

Note:—The Sanskrit writers have assigned names to each one of the twenty-two Shrutees, indicating the particular emotion, (or रस) effected by the particular note. As the twenty-two notes for the twenty-two Shrutees have now been fixed in the above Table, it is easy to assign the names. It will be seen that along with the musical consonance in the notes, there is also a correspondence between the emotions effected by them. Experts like Prof. Abdul Kareem can actually sing these twenty-two notes, for several modes and modules.

The following notes are also used by experts, अ. को. गं. of 281½ vibrations which is major third from ती. नि., and it has its corresponding अ. को. नि. of 421½ vibrations which is fifth above it; त. ती. म. of 341½ vibrations which is fourth from को. र. These notes are used by some experts for some Rāgās. Twenty-two Shrutees are given by Kandhari as sung by Rahimatkhan and Bhayasaheb Joshi; the Dagari and the Nohari as sung by Professor Alladhia and Gokhale brothers (who both are in the service of the Government of Bombay) and the several notes as well as the notes themselves used in several Modes and Modules.

Two Notes, or the Shrutee Scale.

1	2	3	4	5	6	7	8	9	10
Name and kind of Shrutees. श्रुतिनाम, जाति.	Name of notes.	Vibrations	Musical interval lying between each pair of Notes-	Its Name.	Ellis' cents assigned to each interval	Ratio of each note with the Fundamental Note.	Its name.	Ellis' cents assigned.	Vibrating length of wire required for each note.
(13) आलापिनी, करुणा.	पंचम.	360	24 : 25	Small semitone.	70	2 : 3	Just Fifth: 3rd Harm.	702	Inches, Lines. 24—0
(14) मंदंती, करुणा.	अ. को. धे. Aff.	375		125 : 128	Great Dissis.			42	16 : 25
(15) रोहिणी, आयता.	को. धे. Af.	384	24 : 25		Small semitone.	70	5 : 8	Just Minor 6th.	
(16) रम्या, मध्या.	म. धे. A.	400		80 : 81	Comma of Didymus.	22			3 : 5
(17) उषा, वीसा.	ती. धे. As.	405	243 : 256		Pyth. Limma.	90	16 : 27	Pyth. Major 6th: 27 Harm.	
(18) क्षोभिनी, मध्या.	अ. को. नि. Bff.	426 $\frac{3}{4}$		80 : 81	Comma of Didymus.	22			9 : 16
(19) तीव्रा, वीसा.	को. नि. Bf.	432	24 : 25		Small Limma.	70	5 : 9	Acute Minor 7th.	
(20) कुसुवती, आयता.	ती. नि. B.	450		80 : 81	Comma of Didymus.	22			8 : 15
(21) मंसा, वृद्ध.	त. ती. नि. Bs.	455 $\frac{1}{2}$	243 : 256		Pyth. Limma.	90	128 : 243	Pyth. Major 7th.	
(22) छंदोवती, मध्या.	ष. C'.	480		Total carried from ष to ष ...	702	1 : 2			Octave.
			Total from ष to ष.	498	Grand Total... 1200				

* European system tempers the fifth; while in Hindu Music Fifth or ष is kept unchanged (अविच्छिन्न), as the backbone of the Scale.

vibrations which is fifth above अ. को. गं. (281 $\frac{1}{2}$ vibr.); अ. को. म. of 307 $\frac{1}{5}$ vibrations, which is minor third of को. रि, and it has its corresponding त. ती. are generally accepted by almost all the systems of Indian Music. There are several systems in vogue, e. g. the Goburhari, as sung by Abdul Kareem, the vice of the Kolhapur Durbar) and several systems in the Karnatic. All these systems accept the Shrutees, though their several advocates differ as to the combination

Now when we look at the intervallic Scale of twelve notes (Table smaller than 15 : 16 which we in its appearance twice, and that is looked, because it is an interval lying of the musical scale viz. को. गं. and ष. Therefore this interval has been ant and the most suitable interval for giving a still finer scale. The same is used above for the Chromatic scale in developing the scale of twenty-two in रागविबोध. For purposes of the twenty-two Shrutee scale is given below of wire of the Diachord, Mr. Ellis' cents' (as called by Mr. Ellis), and

From this table it will be seen that 24 : 25 having 70 cents, is put 256 (256 vib.), another note called the simple ratio of 24:25 and has 70 cents. In the same way a third note is put 27 (27 vib.). Similarly two संवादि (concord) notes are put here that these notes अ. को. ष. of the scale, and अ. को. ध. को. ष. called by सोमनाथ author of रागविबोध by him. [Vide. श्रुति Table in Music Page 16.] In the same way अ. को. ष. and त. ती. नि. नि. have been already stated that like स. ष. is also used; and the two are to form the backbone of the scale. Therefore the Aryan parts and assigned notes which are combinations of स and नोत of ष [vide श्रुति Table] notes are अ. को. म., को. म, ती. म, ष. of 24:25, 128:135, and 125:128 respectively, making up a total

9. Now when we look at the intervals newly obtained in our Chromatic Scale of twelve notes (Table C), we find that another interval smaller than 15 : 16 which we get in the Diatonic Scale, puts in its appearance twice, and that is 24 : 25. It must not be overlooked, because it is an interval lying between two consecutive notes of the musical scale viz. को. ग. and ती. ग. which form part of harmonics. Therefore this interval has been considered as an important and the most suitable interval to be put in for the purpose of evolving a still finer scale. The same process which has been described above for the Chromatic scale of twelve notes, has been followed in developing the scale of twenty-two notes or श्रुति scale as defined in रागविबोध. For purposes of easy reference, Table D of the twenty-two Shrutee scale is given below, with the musical intervals, lengths of wire of the Diachord, Mr. Ellis' cents number of Shrutees or 'degrees' (as called by Mr. Ellis), and names of the note etc.

10. From this table it will be seen that when the smaller interval of 24 : 25 having 70 cents, is put in between स (240 vib.) and को. रि (256 vib.), another note called अ. को. रि (250 vib.), bearing the simple ratio of 24:25 and having 70 cents makes its appearance. In the same way a third म. रि (266 $\frac{2}{3}$ vib.) appears between को. रि and ती. रि. Similarly two संवादि (consonant) notes are introduced in the second half of the scale viz. अ. को. ध and म. ध. It is to be clearly noted here that these notes अ. को. रि, को. रि, and म. रि, in the first half of the scale, and अ. को. ध, को. ध, and म. ध in the second half are called by सोमनाथ author of रागविबोध as विकृत स्वराः, and are recognised by him. [Vide श्रुति Table in Mr. Banhatti's बालसंगीतबोध, Pt. III, Page 16.] In the same way अ. को. ग. and त. ती. ग and the corresponding अ. को. नि and त. ती. नि have been introduced newly. It is already stated that like स, प is also to be kept unchanged (अविकृत); and the two are to form the back-bone of the scale. The interval between म and प which is the largest viz. 8:9, cannot therefore be neglected. Therefore the Aryan authors divided the same into four parts and assigned notes which are considered as विकृती or modifications of म and नो of प [vide श्रुति Table in Mr. Banhatti's book.] These notes are अ. को. म., को. म, ती. म, and त. ती. म, having th intervals of 24:25, 128:135, and 125:128 respectively, with 70, 92, 42 cents respectively, making up a total of 204 cents. which are

assigned to the higher interval of 8:9 lying between म and प. In this manner we have got 1 स + 4 रि + 4 ग + 4 म + 1 प + 4 ध + 4 नि + 1 सं (upper), making up a total of 23 notes including the octave. These results are given in the following Table D.

11. All the lengths given for the notes in these tables are those of the wire of the Diachord and they must not be confounded with lengths of strings of playing instruments, such as Been, Satar etc. The difference between the instrument fixing a scale like a Diachord and a playing instrument consists in this, that in the playing instrument the height of the strings or wires above the frets necessarily varies from one to five millimetres, as has been shown by Mr. Ellis in his examination of several वीणाs and the श्रुतिवीणा of Tanjore sent to him by Cap. Day. Unless we leave some margin for height, an instrumental player cannot move the fingers from the different frets freely and with ease; and he cannot produce increased tension in order to have different shades, and मेंड (mends) and घसित (ghasits) required for different modes (राग) and modulets (रागिणी). But it is to be observed that when the player puts pressure on the string when bringing it down to the fret, the increased tension due to the pressure must per force increase the pitch. But in preparing an instrument of scale, which is in other words a Diachord, we must not leave any height whatsoever between the speaking string and the moving bridge. Now when we have prepared the above scale, we are to note down the different speaking lengths of the different notes, on the wire of the Diachord. When an instrument player wishes to set the frets to the instrument to a particular scale, he must keep this Diachord by his side; and taking into account the tension caused by the pressure of his finger on the string, he must see whether the note on the playing instrument tallies exactly with that given by the Diachord. He must also while practising attend to the Diachord, and not the playing instrument; because the latter is likely to misguide him. So also while producing different विकृत स्वरास or modified notes by मेंड (मेंड) on the same fret on his playing instruments, he must not deflect the string indiscriminately. He should

deflect it only to such an extent as will give him the exact note required, which will tally accurately with that given out in the Diachord. This can be attained only by long and patient study. Even gifted specialists like the late Bande Ali and his disciples Chunna and Murad, Barkhat Ulla, Haidur Bux, Antubua Sadhale and Vishnupant Joshi (Pakhwajis) required years of constant practice to train their ears and fingers to get the exact notes with ease. The Diachord is the exact standard of measurement for accurately determining the musical scale; in other words it affords us a means to measure musical notes, just as we have the rain gauge, the thermometer, the barometer etc. But the playing instrument, unless it is played upon by a specialist, is not the standard by which the musical scale can be accurately gauged, as the skill of the player must be taken into account. The Sanskrit authors clearly intended this, as they distinctly state the exact divisions of the length of the wire, for producing the different notes viz. स, सं, प, and म. They do not obviously intend that there should be any height whatsoever between the speaking string and the moving fret. Had this been the case, then the laws laid down by (given above) would have given incorrect results. They intended the construction of the musical scale.

12. After having thus obtained these scales, let us now consider the Shruti problem. Among notable recent writers who have attempted to solve the question, may be mentioned Mr. Bhavanrao Pingale, Mr. Balawant Trimbak Sahasrabuddhe, and Raja Surendra Mohun Tagore. I will consider the methods of Messrs. Pingale and Sahasrabuddhe, first; and then examine the Raja's method. They have taken it for granted that like vibration a "Shrutee" was the "unit" of measurement of the long interval lying between a fundamental note and its octave and that 22 Shrutis = 3 subdivisions of equal value. This is not the case. A Shrutee is a sub-division of a note, may be a quarter or a third of a note, etc. &c., according to the position it occupies in the interval between any two consecutive notes.

13. For the purpose of comparing the Shrutee Scale with the exact Scale (स्वर समक) they divided the entire length of the executive part of the wire into 44 units. I quote Mr. Sahasrabuddhe. "If a

monochord" says Mr. Sahasrabuddhe "be taken and a space equal to 44 units be measured and the bridge shifted to this point, the string when struck will yield a note; if we start with this note as the tonic or keynote and run through the *gamut* by shifting the bridge (the Sanskrit writers affirm) the following facts will be observed. Sa will be produced at the distance of 44, Ri at 40, Ga at 37, Ma at 35, Pa at 31, Dha at 27, Ni at 24 and Sa again at 22, but the latter Sa will be twice as intense as the former."

तेषां श्रुतयः क्रमतो वेदा रामा दृशौ तथाश्चुधयः ।
निगमा दहनाः पक्षावेवं द्वाविंशतिः सर्वाः ॥ १६ ॥
तुर्यायां सप्तम्यां तासु नवम्यां श्रुतौ त्रयोदश्याम् ।
सप्तदशीविंशीद्वाविंशीषु च ते स्फुटाः क्रमतः ॥ १७ ॥
× × × ×
द्वाविंशीस्थः षडङ्गो द्विगुणसमः पूर्वषड्जेन ॥ २१ ॥

रागविबोध.

Mr. Sahasrabuddhe has based the above theory on the wrong interpretation and application of Aryas 16 & 17 and the latter part of Arya 21 of रागविबोध quoted above.

Exact Hindu Scale—C D E F G A B C
24, 27, 30, 32, 36, 40½, 45, 48.

Mr. Sahasrabuddhe's—Sá Ri Ga Ma Pa Dha Ni Sá
22, 26, 29, 31, 35, 39, 42, 44.

And now when actual comparison is made by finding the ratios of the fundamental note with each of the successive 7 notes of the Shrutee scale thus wrongly demonstrated, we find none of the notes (except the octave) bears those simple ratios which our Hindu Scale as well as the European exact scale bear. This is quite plain from the following comparative table.

Shruti scale as explained
by Mr. Sahasrabuddhe.

सा = $\frac{22}{22}$
रि = $\frac{26}{22}$
ग = $\frac{29}{22}$
म = $\frac{31}{22}$
प = $\frac{35}{22}$
ध = $\frac{39}{22}$
नि = $\frac{42}{22}$
सा' = $\frac{44}{22}$

The Hindu Exact
Scale.

C = 24 = 1
D = $\frac{27}{24} = \frac{3}{4}$
E = $\frac{30}{24} = \frac{5}{4}$
F = $\frac{32}{24} = \frac{4}{3}$
G = $\frac{36}{24} = \frac{3}{2}$
A = $\frac{40\frac{1}{2}}{24} = \frac{27}{16}$
B = $\frac{45}{24} = \frac{15}{8}$
C' = $\frac{48}{24} = 2$

It is well-known that notes increase in pitch in the inverse ratio of the length of the wire. And applying this law, we easily determine the several lengths of the executive part of the wire which, when sounded, will give the 7 notes of both the Shruti Scale (Mr. Sahasrabuddhe's) and the exact Scale. These lengths are:—

Shrutee scale as explained by
Mr. Sahasrabuddhe.
सा = the whole length

रि = $\frac{22}{26}$
ग = $\frac{22}{29}$
म = $\frac{22}{31}$
प = $\frac{22}{35}$
ध = $\frac{22}{39}$
नि = $\frac{22}{42}$ or $\frac{11}{21}$
सा' = $\frac{22}{44}$ or $\frac{1}{2}$

Exact Hindu
Scale. (Table A)
C = the whole length

D = $\frac{3}{4}$
E = $\frac{4}{3}$
F = $\frac{3}{4}$
G = $\frac{2}{3}$
A = $\frac{16}{27}$
B = $\frac{8}{15}$
C' = $\frac{1}{2}$

It will be found that each one of the intermediate notes of the Shrutee Scale as explained above bears a complicated and rather higher ratio with the fundamental note and that none of the lengths shewn on the left side gives out notes which are obtained in the स्वर-सन्नक (Table A) and which we *actually sing and play*. But the fact is otherwise. Our artistes actually sing and play notes which bear simple ratios with the fundamental note.

14. Mr. Chinna Swami Mudliar M. A. of Southern India, wrote a large volume entitled "Oriental Music," but has left untouched the question of श्रुति or Shrutees as being a very complicated and intricate one. How the labours of Messrs. Pingale and Sahasrabuddhe, were not productive of successful solution, I have already shown above. Raja Surendra Mohan Tagore also attempted to determine the position of the twenty-two Shrutees. He divided the whole speaking length of the wire into two halves, the whole length giving the स or fundamental note and the half giving the स', the octave; both these notes are correct. Again he divided the first half into two equal parts, each being one-fourth of the whole length. The first quarter (of the wire) he subdivided into nine equal parts calling each part a Shrutee. At the end of the ninth part is sounded a note म (at $\frac{1}{4}$ of the wire) which is correct. In the next quarter

of the wire he made thirteen equal subdivisions, each being also called a Shrutee. Thus in all he got the twenty-two Shrutees. Let us now see whether according to the Raja's apportionment we get the other notes correctly. Now there are three Shrutees for *सी. रि.* of the Diatonic Major Scale. (Vide. *रगविबोध आर्या* २० and २२). According to Raja Surendra Mohan Tagore's division, three Shrutees would mean three parts out of the nine equal parts in the first quarter of the whole speaking length of the wire; the length of these three parts would come to $\frac{1}{3}$ part of the whole wire ($\frac{1}{4}$ wire divided into 9 parts, each part = $\frac{1}{4} \times \frac{1}{9} = \frac{1}{36}$; three such parts would mean = $\frac{3}{36} \times 3 = \frac{1}{4}$ part of the whole length). Thus the *सी. रि.* will be produced, on the $\frac{1}{4}$ part of the whole wire, according to Raja Surendra Mohan Tagore's method; *i. e.* *सी. रि.* will be produced on a length of 33 ($= \frac{3}{4} \times \frac{1}{3} = 33$) inches. But as we have seen, the musical interval between *सा* and *सी. रि.* is 8 : 9; the pitch of *सी. रि.* is $\frac{8}{9}$ of *सा*; so if we inverse this ratio of pitch, we get the length required. [$36 \times \frac{9}{8} = 32$ inches]. Thus we get 32 inches as the length for *सी. रि.* Consequently Raja Surendra Mohan Tagore's *सी. रि.* is flatter or *क्रोमल* than the just Major Second which we actually sing and play; the interval also is smaller than the correct one. Similarly incorrect results might be obtained for the other notes, by following Raja Surendra Mohan Tagore's method.

15. I now proceed to show how Cap. Day and Mr. A. J. Ellis, in their attempts to find out the positions of the twenty-two Shrutees, were not successful, perhaps misguided, partly by the erroneous information of recent publications and partly by the assumption that the Hindu writers have followed or are inclined to follow the equal 'temperament' system of Europe in developing their Chromatic Scales. The lines on which Mr. Ellis tried to solve the question of the Shrutees may be seen from the following extract from his paper read before the Royal Society of Arts in 1885. Cap. Day also was similarly misled, and he follows Mr. Ellis' division. Mr. Ellis follows the lines suggested by Raja Surendra Mohan Tagore, whose methods I have already referred to. In his paper Mr. Ellis says:—

"Now we do not know precisely what a degree is. And hence any representation of these differences with exactness is impossible. But we may obtain a tolerably approximate notion thus: suppose the fixed notes to have been those already described in the old C.

Scale, so that C to D, F to G, and G to A, have each 204 cents, and a degree of such an interval should be a quarter of that amount, or 51 cents. The interval D to E, or A to B, has only 182 cents, and but only 3 degrees, so that each degree has $60\frac{2}{3}$ cents. Finally, the interval E to F, or B to C, has 112 cents, and only 2 degrees, hence one of these degrees has 56 cents. The modern Bengali division gets over the difficulty thus: The C string is divided in half, giving the Octave; the half nearest the nut is again halved giving the fourth, F. The part between the nut and F is divided into 9 equal parts, each giving a degree; and the other part from F to the Octave, is divided into 13 equal parts, each giving a degree. From these indications it is possible to calculate the value of each degree and assign the notes. In the following table I give the number of degrees and the calculation of their value on both plans, old and new, with the names of the 19 Indian notes assuming that pitch varies inversely as the length of the string as shown by the position of F and the Octave and that any errors thus arising have been corrected by ear:—

Indian Chromatic Scales.

Degrees ...	1	2	3	4	5	6	7	8
Notes ...	C	Dffl	Dfl	-	D	Efl	Efl	E
Old ...	0	51	102	153	204	264 $\frac{2}{3}$	325 $\frac{1}{3}$	386
New ...	0	49	90	15	204	316	259	374
Degrees ...	9	10	11	12	13	14	15	16
Notes ...	Esh	F	-	Fsh	Fssh	G	Afl	Afl
Old ...	442	498	549	600	651	702	753	804
New ...	435	498	543	589	637	685	736	787
Degrees ...	16	17	18	19	20	21	22	
Notes ...	Afl	...	A	Bffl	Bfl	B	Bsh	
Old ...	804	855	906	966 $\frac{2}{3}$	1027 $\frac{1}{3}$	1088	1144	
New ...	787	841	896	952	1011	1070	1135	

The only values agreeing in each are C, D, F, while new Ffl is the just Minor Third, a mere accident. The 9 degrees from C to F vary from 49 to 63 cents and then there is a sudden break, after which the 13 degrees from F to the Octave vary from 45 to 65 cents. This is the first intelligible presentment of the Indian scale which I have been able to effect. It will be seen that C, Dffl, D, Efl, E, F, Fsh, G, Afl, A, Bfl, B are represented pretty well by our equally tempered notes, but that the 7 intermediate notes Dffl, Efl, Esh, could only be

tempered on the Quarter-tone system used in Syria. Hence, in the usual transcription, these 7 notes are indentified with some of the others, possibly Dfl with Dfl (not with C), Effl with Ffl (not with D), Esh with F (as usual), Fssh with Fsh (not with G), Affl with Afl (not with G), Bfl with Bfl (not with A), and Bsh with C (as usual). These comparisons necessarily injure the original character of the music, and give it a harmonisable appearance which is entirely foreign to Indian music."

16. But our method of dividing a whole tone either of 204 or 182 or 112 cents into four, three or two tones as the case may be, is not to make equal divisions, as has been supposed and done by Mr. Ellis; but the divisions are to be made in accordance with the intervals lying between two consecutive notes. For instance the interval between स and ती. रि, the first and second note of our Major Diatonic Scale is 8:9 with 204 cents. Now suppose we want to divide this greater interval into two smaller ones or tones. Then we introduce between स and ती. रि, a third note called को. रि, or D flat, which bears to the fundamental note स the ratio of 15:16, because this same ratio or musical interval already lies between the third and fourth note ग and ग, or between the seventh and eighth note, नि and सं, of our Major Diatonic Scale. This done, the three notes स, को. रि, and ती. रि. will have the following two musical intervals lying between them. If स has 240 vibrations in a second of time, ती. रि. has 270 vibrations, the interval being 8:9. When को. रि. with 256 vibrations is introduced between the two notes, then the three notes सा (240 vib.), को. रि. (256) and ती. रि. (270 vib.) stand to one another in the ratio of 15:16, and 128:135; having 112 and 92 cents respectively, in all making up 204 cents. But this has not been done by Mr. Ellis. He has divided the whole tone of 204 cents into four equal parts and has assigned 51 cents to each part. This is evidently incorrect and these notes obtained by equal divisions are not actually sung in practice. Similarly are obtained wrong results for other notes also.

17. Again in assigning each subdivision to a Shrutee or "degree" of the twenty-two cycle, a wrong start is generally made by some writers; because the first Shrutee or degree (though it begins from the (0) on which स is marked) is to be marked where the first

Shruti ends and not where it begins. According to the rule given in रागाविबोध of tuning strings and placing the twenty-two frets, each indicating a Shrutee, the first fret or Shruti or "degree" is to be placed after the zero (0) or the fixed bridge on which the whole length of the wire or the vibrating length rests, and when sounded gives the fundamental note. Accordingly the correct and proper way of assigning or marking shrutees is that noted in the Table D; and is different from that adopted by Mr. Ellis. By this process, the figure (0) comes on स or C, the first Shrutee on the second note, and the twenty-second Shrutee exactly comes on the octave स, giving 1200 cents. And according to Mr. Ellis, the twenty-second Shrutee comes on त. ती. नि. or B sharp, having 1135 cents only.

18. Similarly Mr. Ellis made another experiment. He heard Raja Ram Pal Singh playing on his सतार (Satar)—a playing instrument, at four different settings. With the aid of a tuning fork, and assisted by Mr. Hipkins, a noted musician, he observed and took down cents for each note of the Diatonic Scale at each setting and got the following results.

Scales set by Raja Ram Pal Singh.

First and Fourth setting:—								
Obs. 1st.....	0	183	342	533	685	871	1074	1230
„ 4th	0	174	350	477	697	908	1070	1181
New	0	204	374	498	685	896	1070	1200
Notes.....	C	D	E	F	G	A	B	C
Second setting:—								
Obs.	0	183	271	534	686	872	983	1232
New	0	204	259	498	685	896	1011	1200
Notes.....	C	D	Efl	F	G	A	Bfl	c
Third setting:—								
Obs.	0	111	314	534	686	828	1017	1198
New	0	99	316	498	685	787	1011	1200
Notes.....	C	Dfl	Efl	F	G	Afl	Bfl	c
Fifth setting:—								
Obs.	0	90	366	490	707	781	1080	1087
New	0	99	374	498	685	787	1070	1200
Notes.....	C	Dfl	E	F	G	Afl	B	c

These results when compared with the cents, put in my Diatonic Major table will show that the cents obtained by Mr. Ellis have not

been correct ones. The observations noted in the first line of the first setting do not tally with those of the second setting, nor those of the third setting with those of the fourth setting. Even the cents observed for the Octave (स) differ for all the four settings. But there is no wonder that such varying results were obtained. Because Mr. Ellis himself says that the setting of the frets was a "pure matter of ear and memory"; and "the frets were moved somewhat hastily and perhaps were not arranged with the accuracy that would have been attained by a professional musician."

19. I may state in brief that attempts were made in three directions or ways to solve the question of Shruttees. Messrs. Pingale and Sahasrabudde among others tried to solve the question by dividing the whole speaking length of the wire into forty-four (44) equal units, and then trying to assign the positions of the twenty-two Shruttees. The faults of their method have been explained above. Raja Surendra Mohun Tagore divided the string into two equal parts, which again were subdivided into equal parts, each containing a varying number of equal units which he designated as the Shruttees I have already shown the erroneous nature of this method. Mr. A. J. Ellis divided each interval into as many *equal* parts as there were Shruttees *e. g.* 4, 3, or 2. I have shown above how this method too does not give a satisfactory solution. The reasons as to why Mr. Ellis could not get satisfactory results in all his experiments were: first, as he admits, the original treatises on Hindu Music were not accessible to him. Secondly, the experiments were made on fretted instruments. In these instruments, the pressing of the wire or string down to the fret increases the tension, thereby increasing the pitch. The height of strings above the frets in different instruments varies largely, say from 4 to 6 millimetres. Again in playing the same notes on different occasions, the same performer is likely to commit mistakes on account of defect of ear or want of proficiency. And, as is admitted by Mr. Ellis himself, "it is exceedingly difficult to determine the minute differences of pitch between notes with qualities of tones so different as those of plucked strings and tuning forks."

20. Now it may be asked that the श्रुतिस (Shruttees) in the table of 22 Chromatic notes or the Shruttee Scale (Table D) do not apparently correspond to those assigned for each of the 7 notes

in the Diatonic Major Scale. This point is cleared thus. As explained by Sanskrit writers a Shruttee is any audible musical note given by plucking the wire against the bridge; or to speak in terms of the scientist of the West, Shruttee is the smallest musical interval, lying between any two consecutive notes of the musical scale. I may make myself clear by giving an example. The musical interval between स and ती. रि. of the Diatonic Major Scale (of eight notes including the octave) is 8:9. This interval was first divided into three smaller ones, each being called a Shruttee. The author of रागविबोध first laid down that that ती. रि. has three Shruttees, But for developing this Diatonic scale into the Chromatic scale of twelve or twenty-two notes, it was also laid down that स and प are to be kept unchanged (अविकृत). Therefore the eight Shruttees of स and प (four for each) had to be distributed among the other notes, after retaining one for each (one for स and one for प). Thus to distribute the remaining six Shruttees among the other notes, it was necessary to divide the interval 8:9 between स and ती. रि. into four विकृत स्वरस, each called a Shruttee. Under these circumstances it will be easily seen that a Shruttee is not a *unit* of measurement, as has been supposed to be the case by several writers; but it is an interval lying between any two consecutive notes, and as such is liable to be subdivided into as many smaller intervals as there may be विकृत स्वरस, or modifications of tones. Shruttees may be more than twenty-two also, this number being the one generally accepted, some Sanskrit authors recognising 42, some 66 and some saying that they are innumerable.

21. It will thus be seen that in forming the Chromatic Scale of twenty-two Shruttees, the same method of introducing smaller ratios or intervals is observed, as that pursued in forming the scale of twelve notes. The rule of perfect concord on which Sanskrit writers put so much emphasis, has been strictly observed in all the scales. It will also be clear how the Chromatic scale of twelve notes has been formed out of the Diatonic scale of seven notes, and how the scale of 22 notes or the Shruttee scale has been worked out from that of twelve notes. I have already explained the methods which the Sanskrit writers have adopted for evolving higher and finer scales. It is to be noted that these scales which are worked

out strictly on the lines laid down by our Sanskrit authors are constructed on a thoroughly scientific basis ; and they fully (through their intervals) satisfy the test of the system of cents adopted by Mr. A. J. Ellis. The theory of the स्वरसप्तक or Diatonic Major scale has already been propounded above. From all this it will be evident that the Sanskrit writers were fully cognisant of the laws of the constitution of musical sound, which have been approved of by modern science ; that they worked out their scales not “ arbitrarily ” but on definite and regular fixed laws ; and that in formulating their scales they were led not by “ artificial ” ideas, and were guided not by “ capricious ” suppositions, but proceeded on precise rules and principles.

22. By means of the Diachord and these tables which have been worked out from Sanskrit writers, the Musical Scale can be determined with mathematical precision. The Diachord with its moving bridge gives us an accurate means of determining the several notes correctly ; and the notes of the instrumentalist or vocalist can be tested by referring them to those produced on the Diachord. Like the tuning forks of the West which are used for testing the correctness of the notes, the Diachord with its moving bridge serves us the same purpose. The ear, which at present chiefly guides the musician—instrumentalist or vocalist—is not always an infallible test of the correctness and justness of the notes ; it is liable to vary in its capacity of judgment. Hence the great importance of the Diachord.

23. The experiments which I made with the Diachord, were conducted with the assistance of Prof. Abdul Kareem, an expert professional vocalist of renown. The results of the experiments which I have been making for the last few years, have been verified by him. And it is no small satisfaction to me, and I believe, as well as to the public, that the results of my study of the theory of the Hindu Musical Scale as propounded by the old Sanskrit writers have been approved of and amply corroborated by eminent professional artistes like Prof. Abdul Kareem. It might be stated here that but for the kind help and open-hearted assistance of the Professor, I should not have been able to lay these few ideas before the public. I cannot but here express my heartfelt obligations to the works of modern

Indian writers like Messrs. Kunte, Pingale, Sahasrabudde, Bhatti, Chinna Swami Mudliar, and Raja Surendra Mohun Tagore among others; and also to the works of European writers like Sir William Jones, Capt. Day, Messrs. Bosanquet and A. J. Ellis, for the valuable light of information and criticism which they throw upon the subject. To the study of Hindu Music which these writers made and to their labours for regenerating and encouraging this Art of Arts, I humbly and respectfully add my share, infinitesimally small though it is. As endeavours in this direction are carried and pursued further, it is quite possible that more light will be thrown on the subject ; and perhaps the results which I have obtained at present might undergo modification. I stand open to correction.

24. I cannot conclude without making an appeal to the public in the interests of this Art of Music. At present, broadly speaking, the Art is confined to two classes, professional Musicians—Vocalists or Instrumentalists—and the operatic (संगीत) stage. And if the excellence of the Art is to be found anywhere, it must be admitted to exist among the Professional Musicians only. All credit is due to them, because in spite of the absence of material encouragement in recent times, they alone have still preserved and protected this ancient and richly developed Art from total extinction. Our Hindoo religion, which is so comprehensive in its relation to life as to hardly leave any subject outside the sphere of its influence, has done not a little, in fact it has done the utmost, by means of the numerous rites and ceremonials which embody music as a part of their programme, to preserve, cultivate and develop this Art. The great stimulus which Institutions like the Gayan Samaj of Poona and other centres, and the Gandharva Maha Vidyalaya of Lahore (the Academy of Indian Music, conducted by Pandit Vishnu Digamber Paluskar), have given to the study of this Art by creating a wide interest among the people, must be candidly acknowledged. All these attempts are surely commendable, but looking to the steady and slow decline of this Art in recent times, it must be recognised that they are insufficient for the purpose in view. The blind imitation of the Westerns which was the besetting sin of our educated people about 50 years ago, has had its evil effects on Music also as on other spheres of activity. No other

institution succumbed to the passion so completely as our Dramatic Stage. The harmonium and piano of the West soon took the place of the Veenâ, Bin and the Sarangi and the musical precision and rich melody of old soon gave place to imperfect and graceless music. Instruments of the harmonium family with fixed keys which reign supreme at present on our stage, are based on the *European Temperate Scale*, which is admitted by European musicians themselves to be a defective scale. As observed by Professor Blaserna, "it is an incorrect scale. It has destroyed many delicacies and has given to music, founded on simple and exact laws, a character of almost coarse approximation." These are instruments with fixed keys, they restrict a musician by compelling him to choose a note out of a fixed scale, and that too arranged on an *approximation to natural tones*. Again the notes on the piano or harmonium die away rapidly and do not give rise to overtones which are the essentials of rich and good music. Aroha (ascent), Avaroha (descent), Murchchhana (a quarter-tone), Mends, or Ghasits—all these are necessary for the proper execution of a Raga or Ragini; and in the very nature of things, they cannot be had on the harmonium or piano. Yet our musical pieces which are composed in accordance with the rules of Indian Music, are sung on the stage in accompaniment with these instruments! For example, the singer of दूरवारी कानडा (a Raga), obtains on the harmonium not the counterpart of his Raga, but quite a different tune; and the result is the creation of imperfect music and ludicrous incongruity. And yet, it is this incongruity which is enacted and tolerated on our dramatic stage, night after night! As Professor Blaserna rightly observes, "music founded on the temperate scale must be considered as imperfect music and far below our musical sensibility and aspirations. That it is endured and even thought beautiful only shews that our ears have been systematically falsified from infancy."* How truly do these remarks hold good in our case, may

* Hon. Mr. Muir Mackenzie explained to me that vocal music and music on instruments of the violin family is sung and played in the exact scale by connoisseurs only in Europe. But I would add that the *tempered* scale has been adopted in Europe to suit the exigencies of instruments with fixed keys. Its advantages for the European system which is dependent on transposition and unlimited modulation from one key to another are felt to far outweigh its disadvantages, and there is very little probability of a return being made to the natural scale in the near future in Europe. At the same time Indian Music which is not dependent on extensive modulation has no need whatever for a tempered scale.