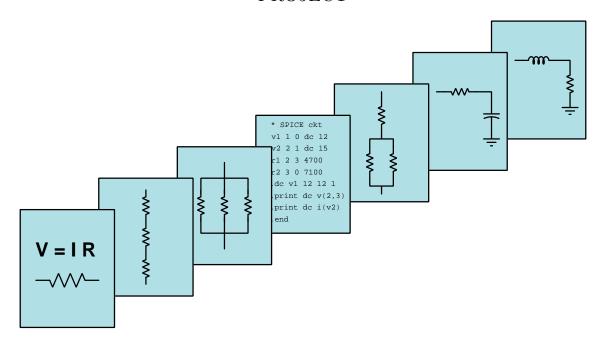
Modular Electronics Learning (ModEL) PROJECT



PHASOR DIAGRAMS

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Chapter 1

Introduction

1.1 Recommendations for students

AC circuit analysis is complicated by the fact that voltages and currents exist as waves rather than as static quantities, and therefore the relative phase shift of one waveform compared to another affects how those waveforms interact. Complex numbers work well as a mathematical tool to symbolically represent voltage and current and impedance quantities in AC circuits as phasors, but there exists a graphical method in which these complex quantities are represented by line segments ("vectors") having magnitude (length) and phase angle (direction). This module explores the concept of graphical phasors and diagrams comprised of them.

Important concepts related to phasor diagrams include **complex numbers**, **phase shift**, **vector addition**, **vector subtraction**, **rectangular form**, **polar form**, **Kirchhoff's Voltage Law**, **Kirchhoff's Current Law**, properties of **series** networks, properties of **parallel** networks, and **sources** versus **loads**.

Here are some good questions to ask of yourself while studying this subject:

- Choose any of the example phasor diagrams shown in the tutorial to associate the text's explanation with the graphical image.
- How does the "polar" form of a complex number relate to an AC voltage or current?
- How does the "rectangular" form of a complex number relate to an AC voltage or current?
- What does it mean when an AC source is labeled with polarity symbols or an arrow symbol?
- How are phasors stacked together to represent addition?
- How are phasors stacked together to represent subtraction?
- Which electrical quantity(ies) add in a series network?
- Which electrical quantity(ies) must be equal throughout a series network, and why?

- Which electrical quantity(ies) add in a parallel network?
- Which electrical quantity(ies) must be equal throughout a parallel network, and why?
- Explain how the directions of current arrows used to annotate schematic diagrams can be (and often are!) confused with the directions of vectors used to plot phasor diagrams.

1.2 Challenging concepts related to phasor diagrams

The following list cites concepts related to this module's topic that are easily misunderstood, along with suggestions for properly understanding them:

- Phasors representing AC amplitudes and phase shifts a powerful tool used for understanding the operation of AC circuits is the phasor diagram, consisting of arrows pointing in different directions: the length of each arrow representing the amplitude of some AC quantity (voltage, current, or impedance), and the angle of each arrow representing the shift in phase relative to the other arrows. By representing each AC quantity thusly, we may more easily calculate their relationships to one another, with the phasors showing us how to apply trigonometry (Pythagorean Theorem, sine, cosine, and tangent functions) to the various calculations. An analytical parallel to the graphic tool of phasor diagrams is complex numbers, where we represent each phasor (arrow) by a pair of numbers: either a magnitude and angle (polar notation), or by "real" and "imaginary" magnitudes (rectangular notation). Where phasor diagrams are helpful is in applications where their respective AC quantities add: the resultant of two or more phasors stacked tip-to-tail being the mathematical sum of the phasors. Complex numbers, on the other hand, may be added, subtracted, multiplied, and divided; the last two operations being difficult to graphically represent with arrows.
- Complex numbers in measurement complex numbers may be expressed in either rectangular or polar form, either one of these being perfectly valid. However, measurement instruments such as multimeters only provide the magnitude of the polar form of the voltage or current in question. For example, if a component's voltage is 4.8 Volts RMS ∠ 35° with the circuit's source voltage being the phase reference (0°), an voltmeter reading that voltage will simply register 4.8 Volts RMS. An oscilloscope simultaneously measuring that component voltage on one channel and the source voltage on another will show the 35° shift on the horizontal axis between the two waveforms.

The Case Tutorial chapter contains multiple sections showing phasor diagrams applied to example circuits.

1.3 Recommendations for instructors

This section lists realistic student learning outcomes supported by the content of the module as well as suggested means of assessing (measuring) student learning. The outcomes state what learners should be able to do, and the assessments are specific challenges to prove students have learned.

• Outcome – Demonstrate effective technical reading and writing

<u>Assessment</u> – Students present their outlines of this module's instructional chapters (e.g. Case Tutorial, Tutorial, Historical References, etc.) ideally as an entry to a larger Journal document chronicling their learning. These outlines should exhibit good-faith effort at summarizing major concepts explained in the text.

<u>Assessment</u> – Students show how quantitative results were obtained by the author in the Tutorial chapter's examples.

• Outcome – Plot phasor diagrams expressing circuit quantities

<u>Assessment</u> – Sketch phasor diagrams expressing voltages in AC circuits; e.g. pose problems in the form of the "Three series voltage sources" Quantitative Reasoning question.

<u>Assessment</u> – Sketch phasor diagrams expressing currents in AC circuits; e.g. pose problems in the form of the "Three parallel current sources" Quantitative Reasoning question.

• Outcome – Identify errors made in a phasor diagram

<u>Assessment</u> – Identify errors in a phasor diagram provided by the instructor; e.g. pose problems in the form of the "Find the mistakes" Diagnostic Reasoning question.

ullet Outcome – Independent research

<u>Assessment</u> – Read and summarize in your own words reliable historical documents on the subject of applying complex numbers to AC circuit calculations. Recommended readings include books written by Charles Proteus Steinmetz.

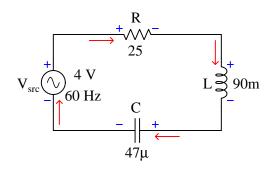
Chapter 2

Case Tutorial

The idea behind a *Case Tutorial* is to explore new concepts by way of example. In this chapter you will read less presentation of theory compared to other Tutorial chapters, but by close observation and comparison of the given examples be able to discern patterns and principles much the same way as a scientific experimenter. Hopefully you will find these cases illuminating, and a good supplement to text-based tutorials.

These examples also serve well as challenges following your reading of the other Tutorial(s) in this module – can you explain why the circuits behave as they do?

2.1 Example: series AC circuit with voltage source



 $Z_R = 25.0000 \ \Omega \ \angle \ 0^o$ $Z_L = 33.9292 \ \Omega \ \angle \ 90^o$

 $Z_C = 56.4379 \ \Omega \ \angle \ -90^o$

 $Z_{total} = 33.6399 \ \Omega \ \angle \ -41.9983^{o}$

 $I=118.906~\mathrm{mA} \ \angle\ 41.9983^o$

 $V_R = 2.97266 \text{ V} \angle 41.9983^o$

 $V_L = 4.0344 \text{ V} \angle 131.998^o$

 V_C = 6.71083 V \angle -48.0017^o

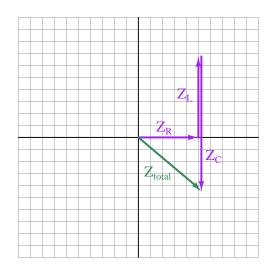
 $S=0.475626~\mathrm{VA}$

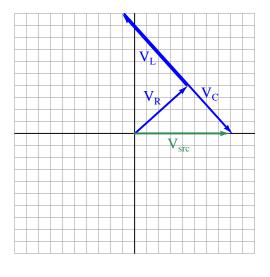
 $P=0.353468~\mathrm{W}$

 $Q=0.318245~\mathrm{VAR}$

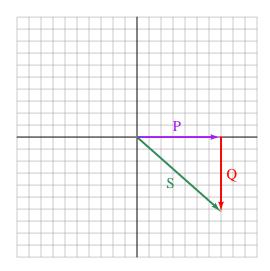
Power factor = 0.743165 leading

Phasor diagrams for impedances and voltages:

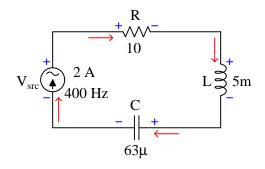




Phasor diagram for powers:



2.2 Example: series AC circuit with current source



 Z_R = 10.0000 Ω \angle 0^o

 $Z_L = 12.5664~\Omega~\angle~90^o$

 $Z_C = 6.31567 \ \Omega \ \angle \ -90^o$

 $Z_{total} = 11.7928~\Omega~\angle~32.0083^o$

 $V_{src} = 23.5857~\mathrm{V} \ \angle \ 32.0083^o$

 $V_R = 20 \text{ V} \angle 0^o$

 $V_L = 25.1327 \text{ V} \angle 90^o$

 $V_C = 12.6313 \text{ V} \angle -90^o$

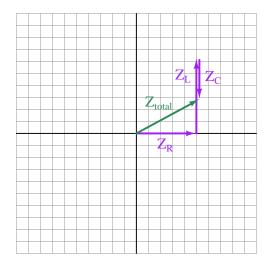
 $S=47.1714~\mathrm{VA}$

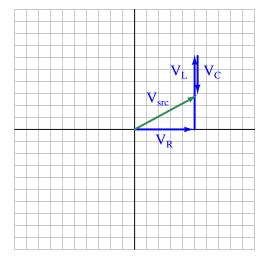
 $P=40~\mathrm{W}$

 $Q=25.0028~\mathrm{VAR}$

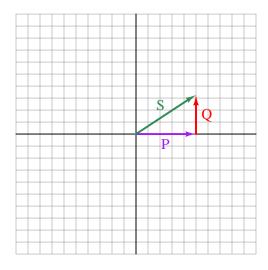
Power factor = 0.847972 lagging

Phasor diagrams for impedances and voltages:

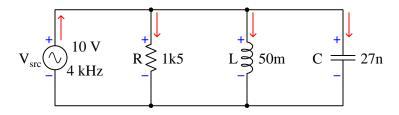




Phasor diagram for powers:



2.3 Example: parallel AC circuit with voltage source



 Z_R = 1500.00 Ω \angle 0^o

 $Z_L = 1256.64~\Omega~\angle~90^o$

 $Z_C = 1473.66 \ \Omega \ \angle \ -90^o$

 $Z_{total} = 1477.35 \ \Omega \ \angle \ 9.96994^{o}$

 $I_{src}=6.76889~\mathrm{mA}~\angle~-9.96994^o$

 $I_R=6.66667~\mathrm{mA}~\angle~0^o$

 $I_L = 7.95775~\mathrm{mA}~\angle~-90^o$

 $I_C = 6.78584~\mathrm{mA} \ \angle \ 90^o$

S = 0.0676889 VA

 $P = 0.0666667 \; \mathrm{W}$

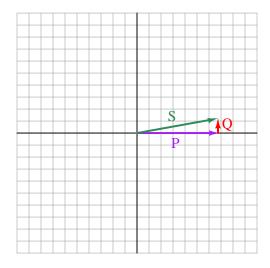
 $Q=0.0117191~\mathrm{VAR}$

Power factor = 0.984899 lagging

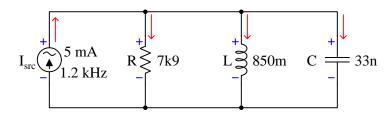
Phasor diagram for currents:



Phasor diagram for powers:



2.4 Example: parallel AC circuit with current source



 $Z_R = 7900.00 \ \Omega \ \angle \ 0^o$

 $Z_L = 6408.85~\Omega~\angle~90^o$

 $Z_C = 4019.06 \ \Omega \ \angle \ -90^o$

 $Z_{total} = 6371.73 \ \Omega \ \angle \ -36.24^o$

 V_{src} = 31.8587 V \angle -36.24^o

 $I_R = 4.03274~\mathrm{mA}~\angle~-36.24^o$

 $I_L = 4.97104 \text{ mA} \angle -126.24^o$

 $I_C = 7.92688~\mathrm{mA} \ \angle \ 53.76^o$

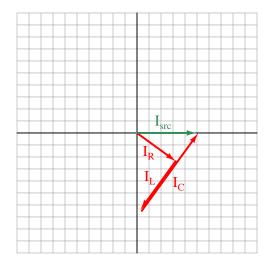
S = 0.159293 VA

 $P=0.128478~\mathrm{W}$

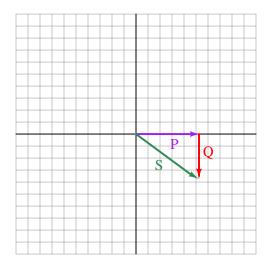
 $Q=0.0941691~\mathrm{VAR}$

Power factor = 0.806548 leading

Phasor diagram for currents:



Phasor diagram for powers:



Chapter 3

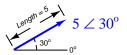
Tutorial

3.1 Graphically representing complex numbers

Phasor representation of AC quantities consists of using complex numbers for AC circuit quantities such as voltage and current. These complex numbers may be added and subtracted just as "normal" (called "real") numbers, and this allows us to apply principles such as Kirchhoff's Laws to AC circuit analysis. A disadvantage of complex numbers is that they are, well, complicated to mentally manipulate. Whereas 8+3=11 may be easy enough to compute without the aid of any calculating device, $(8 \angle 35^o) + (3 \angle -20^o) = 10.03 \angle 20.8^o$ is definitely not. For this reason I strongly encourage students use electronic calculators capable of performing complex-number arithmetic, as such a tool eliminates much of the tedium in AC circuit analysis and allows greater focus on principles rather than procedures.

A practical way to make phasors seem less abstract is to represent them graphically as *vectors* on a two-dimensional diagram. A "vector" is a line segment with an arrowhead at one end, representing any quantity that has a magnitude (vector length) and angle (vector direction). The following example shows a vector with a magnitude of five (5) and a direction of 30 degrees counter-clockwise from horizontal-right:

A vector has both magnitude and direction



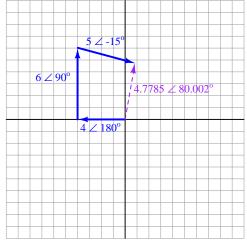
Vectors are often applied in mechanics to represent forces and motion, since these physical quantities both have magnitude and direction in three-dimensional space. For our purposes in analyzing AC circuits, though, we use vectors to represent AC voltages, currents, impedances, and other quantities on the complex-number plane where the horizontal axis represents real numbers and the vertical axis imaginary numbers. In fact, the word "phasor" is actually a portmanteau of "phase" and "vector", which simply means that the angle of any phasor represents a phase shift between two sinusoidal waveforms rather than an angular displacement in space as is the case with most vectors in physics. In order to minimize confusion, we will refer to any rectangular- or polar-form mathematical expression of an AC circuit quantity as a "phasor", and reserve the word "vector" for the arrow symbol used to graphically illustrate a phasor quantity.

3.2 Phasor diagrams and vector addition

Vector diagrams are a graphical aid to understanding the addition and subtraction of quantities having magnitude and direction. In physics, a common application of vector diagrams is to show the summation of multiple forces acting on an object (called a "force-body diagram"). In AC circuit analysis we may do a similar thing, using vectors to represent any additive or subtractive electrical quantities, in which case we refer to this special type of vector diagram as a phasor diagram.

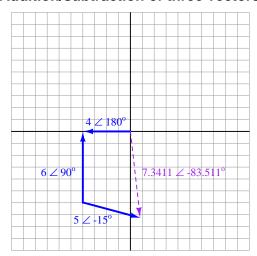
Addition of vectors consists of stacking them end-to-end with the tip of one vector touching the tail of the next, the resulting sum being the vector stretching from the starting point (the first vector's tail) to the ending point (the last vector's tip). Subtraction of vectors consists of stacking them either tip-to-tip or tail-to-tail. We will explore addition and subtraction examples using phasor diagrams:

Addition of three vectors



 $(4 \angle 180^{\circ}) + (6 \angle 90^{\circ}) + (5 \angle -15^{\circ}) = 4.7785 \angle 80.002^{\circ}$

Addition/subtraction of three vectors



 $(4 \angle 180^{\circ}) - (6 \angle 90^{\circ}) + (5 \angle -15^{\circ}) = 7.3411 \angle -83.511^{\circ}$

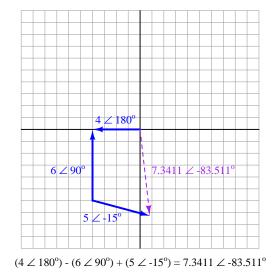
In the left-hand example we see the first vector plotted with its tail at the graph's origin (center). The second vector's tail starts at the tip of the first vector, the tip of that second vector marking the starting point for the tail of the third vector, in the order of the written mathematical sum shown below the graph. The resultant vector (sum) is simply the distance and angle from the first vector's tail (at the origin of the graph) to the last vector's tip. Vector addition, as you can see, is quite simple. In the absence of an electronic calculator capable of performing complex-number arithmetic, you can also see how it would be possible to approximate this sum simply by carfully sketching the three vectors and then measuring the resultant using a ruler and protractor.

In the right-hand example we see the same three vectors, but this time the middle term is subtracted from the other two rather than being added to them. This is why the tip of the first vector touches the tip of the second rather than the tail of the second. Likewise, the tail of the second vector touches the tail of the third vector for the same reason: the middle vector's term is subtractive while the first and last terms are additive to the resultant. Again, the resultant is

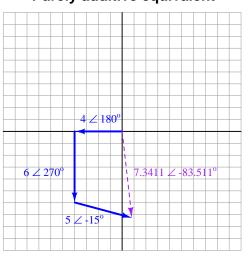
nothing more than the distance and direction from the starting point to the ending point, and could be estimated by careful plotting and measurement on graph paper.

A bit of careful observation and consideration reveals how it is possible to re-write the addition/subtraction example as pure addition. All we need to do is express the second term in such a way that it represents the same quantity when added as it did before when subtracted. Here are two diagrams, on the left showing the same addition/subtraction example as on the previous page, and on the right showing the purely-additive version of the same:

Addition/subtraction of three vectors



Purely additive equivalent



 $(4 \angle 180^{\circ}) + (6 \angle 270^{\circ}) + (5 \angle -15^{\circ}) = 7.3411 \angle -83.511^{\circ}$

The alteration we made to the middle term was to add 180 degrees of rotation to the vector so that it pointed in the opposite direction as before. Now, with that vector being $6 \angle 270^o$ instead of $6 \angle 90^o$ we may add it to the two other terms rather than subtract it, and get the same result¹.

¹In case you were wondering, 6 \angle 270° is the same as 6 \angle −90°, but I chose to write the modified vector angle as 270 degrees rather than −90 degrees in order to avoid triggering a common misconception that reversing the sign of a vector's angle always reverses the vector's direction. The truth is, reversing the sign of a vector's angle turns it into its mirror-image about the horizontal axis, which only reverses its direction in the special case of +90° or −90°.

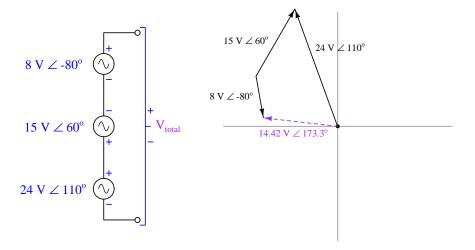
3.3 Appropriate uses for phasor diagrams

All of this shows us how the basic concept of vector addition and subtraction works, which by extension means we may do the same with all additive or subtractive *phasor* quantities in AC circuits. Even if we have the computational tools necessary to perform complex-number arithmetic, sketching a phasor diagram for any sum is a way to confirm to ourselves that the mathematical result we computed is indeed correct.

Again, it is important to stress that phasor diagrams are fundamentally additive and subtractive in nature, which means their use in AC circuit analysis is limited to quantities we happen to know either add or subtract. This means phasor diagrams apply to voltage and impedances in series AC networks, and to currents in parallel AC networks. Therefore it is always important to check your work against your knowledge of circuit fundamentals – that voltages and impedances add in series, and that currents add in parallel – when sketching or interpreting phasor diagrams.

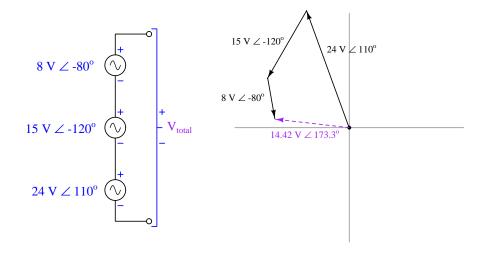
3.4 Series network phasor diagrams

Let us now sketch a phasor diagram for a network of three AC voltage sources connected in series. We know from Kirchhoff's Voltage Law that the total voltage of a series network is equal to the algebraic sum of the individual voltages, so all we need to do is pay attention to the polarities of these sources (as if they were DC) to determine whether they will add or subtract from each other, then stack the vectors end-to-end on that basis starting at the origin (center point) of the diagram:



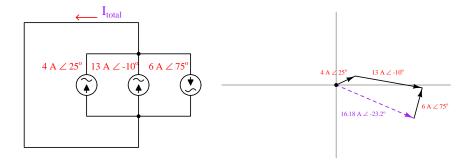
Notice how the 15 Volt vector meets tip-to-tip with the 24 Volt vector because those two voltage sources are connected series-opposing in the circuit (i.e. the + of one source connecting to the + of the other). Note also how the 15 Volt vector meets tail-to-tail with the 8 Volt vector because those two sources are also connected series-opposing (the - of one source connecting to the - of the other). The resultant (sum) begins at the origin and ends at the last vector.

If the concept of phasor subtraction is too confusing, know that you can re-annotate the middle voltage source (i.e. reverse its polarity and shift its phase angle by 180°) and re-draw the phasor diagram to show everything adding with nothing subtracting:



3.5 Parallel network phasor diagrams

Of course, phasor diagrams work just as well² to plot additive AC currents as they do to plot additive AC voltages. Here we will calculate total current for three parallel-connected AC current sources, knowing from Kirchhoff's Current Law that I_{total} must be the sum of the three source currents:



Note how the 6 Ampere vector meets tip-to-tip with the 13 Ampere vector because those two current sources are connected in parallel-opposing fashion. The 4 Ampere and 13 Ampere vectors meet tip-to-tail because they aid each other. As usual, the resultant (sum) begins at the origin and ends at the last vector. If we wish to avoid subtraction and instead use only addition, we could reverse the direction of the 6 Ampere source's current arrow in the schematic diagram and shift its phasor's angle by 180^o (making it 6 A \angle -105^o or 6 A \angle 255^o), then stack all three vectors tip-to-tail to achieve the same resultant, much like what was demonstrated in the previous (voltage) example.

 $^{^2}$ Phasor diagrams actually work well for any additive phasor quantities: voltages and impedances in series, currents and admittances in parallel, etc.

3.6 Vector arrows versus current arrows

A very important point to note, and a common source of confusion among students new to phasor diagrams, is that the arrows showing direction of current in the schematic diagram are *not* vectors, but represent something entirely different. Current arrows in a schematic diagram represent the direction of positive charge carrier motion (conventional flow notation) at the 0^o point in time for that quantity's cosine wave – in other words, this is the direction charge carriers will be moving through the circuit when *that* wave is at its positive peak. A phasor, on the other hand, represents the state of that waveform in the complex-number plane at the instant in time when the *reference* quantity is at *its* 0^o point (positive peak). Current arrow direction is mostly at the discretion³ of whoever sketched the circuit diagram, but phasor direction is standardized with 0^o pointed to the right, 90^o pointed up, 180^o pointed to the left, and -90^o (or 270^o) pointed down.

Current arrows drawn in a schematic diagram simply tell us whether their associated phasors will add or subtract. The 4 Ampere and 13 Ampere sources in the previous schematic added because their respective currents merged in the same direction, whereas the 6 Ampere source subtracted from the other two because its current arrow pointed in the opposite direction on the schematic. Once we determine the add/subtract relationships from the schematic diagram, we use that information to stack the vectors properly in the phasor diagram. Do not make the mistake of thinking that the direction of current flow in the circuit schematic is somehow the same as the direction each current's vector will point in the phasor diagram – these two sets of arrows are related to each other, but not synonymous.

 $^{^3}$ To illustrate this principle, imagine if I had sketched the schematic diagram so that the current source terminals were arranged horizontally instead of vertically, with the 4 Ampere and 13 Ampere source currents pointing to the right instead of up and the 6 Ampere source current pointed left instead of down. This re-orientation of the schematic diagram would have no effect whatsoever on the phasor diagram, where each vector is pointing in the direction specified by the angle quantity of the polar-form complex number (e.g. the 13 A \angle -10° vector is pointed 10 degrees below horizontal).

Chapter 4

Questions

This learning module, along with all others in the ModEL collection, is designed to be used in an inverted instructional environment where students independently read¹ the tutorials and attempt to answer questions on their own *prior* to the instructor's interaction with them. In place of lecture², the instructor engages with students in Socratic-style dialogue, probing and challenging their understanding of the subject matter through inquiry.

Answers are not provided for questions within this chapter, and this is by design. Solved problems may be found in the Tutorial and Derivation chapters, instead. The goal here is *independence*, and this requires students to be challenged in ways where others cannot think for them. Remember that you always have the tools of *experimentation* and *computer simulation* (e.g. SPICE) to explore concepts!

The following lists contain ideas for Socratic-style questions and challenges. Upon inspection, one will notice a strong theme of *metacognition* within these statements: they are designed to foster a regular habit of examining one's own thoughts as a means toward clearer thinking. As such these sample questions are useful both for instructor-led discussions as well as for self-study.

¹Technical reading is an essential academic skill for any technical practitioner to possess for the simple reason that the most comprehensive, accurate, and useful information to be found for developing technical competence is in textual form. Technical careers in general are characterized by the need for continuous learning to remain current with standards and technology, and therefore any technical practitioner who cannot read well is handicapped in their professional development. An excellent resource for educators on improving students' reading prowess through intentional effort and strategy is the book textitReading For Understanding – How Reading Apprenticeship Improves Disciplinary Learning in Secondary and College Classrooms by Ruth Schoenbach, Cynthia Greenleaf, and Lynn Murphy.

²Lecture is popular as a teaching method because it is easy to implement: any reasonably articulate subject matter expert can talk to students, even with little preparation. However, it is also quite problematic. A good lecture always makes complicated concepts seem easier than they are, which is bad for students because it instills a false sense of confidence in their own understanding; reading and re-articulation requires more cognitive effort and serves to verify comprehension. A culture of teaching-by-lecture fosters a debilitating dependence upon direct personal instruction, whereas the challenges of modern life demand independent and critical thought made possible only by gathering information and perspectives from afar. Information presented in a lecture is ephemeral, easily lost to failures of memory and dictation; text is forever, and may be referenced at any time.

GENERAL CHALLENGES FOLLOWING TUTORIAL READING

- <u>Summarize</u> as much of the text as you can in one paragraph of your own words. A helpful strategy is to explain ideas as you would for an <u>intelligent child</u>: as simple as you can without compromising too much accuracy.
- <u>Simplify</u> a particular section of the text, for example a paragraph or even a single sentence, so as to capture the same fundamental idea in fewer words.
- Where did the text <u>make the most sense</u> to you? What was it about the text's presentation that made it clear?
- Identify where it might be easy for someone to <u>misunderstand the text</u>, and explain why you think it could be confusing.
- Identify any <u>new concept(s)</u> presented in the text, and explain in your own words.
- Identify any <u>familiar concept(s)</u> such as physical laws or principles applied or referenced in the text.
- Devise a <u>proof of concept</u> experiment demonstrating an important principle, physical law, or technical innovation represented in the text.
- Devise an experiment to <u>disprove</u> a plausible misconception.
- Did the text reveal any <u>misconceptions</u> you might have harbored? If so, describe the misconception(s) and the reason(s) why you now know them to be incorrect.
- Describe any useful <u>problem-solving strategies</u> applied in the text.
- <u>Devise a question</u> of your own to challenge a reader's comprehension of the text.

GENERAL FOLLOW-UP CHALLENGES FOR ASSIGNED PROBLEMS

- Identify where any <u>fundamental laws or principles</u> apply to the solution of this problem, especially before applying any mathematical techniques.
- Devise a <u>thought experiment</u> to explore the characteristics of the problem scenario, applying known laws and principles to mentally model its behavior.
- Describe in detail your own <u>strategy</u> for solving this problem. How did you identify and organized the given information? Did you sketch any diagrams to help frame the problem?
- Is there more than one way to solve this problem? Which method seems best to you?
- Show the work you did in solving this problem, even if the solution is incomplete or incorrect.
- What would you say was the most challenging part of this problem, and why was it so?
- Was any important information missing from the problem which you had to research or recall?
- Was there any <u>extraneous</u> information presented within this problem? If so, what was it and why did it not matter?
- Examine someone else's solution to identify where they applied fundamental laws or principles.
- <u>Simplify</u> the problem from its given form and show how to solve this simpler version of it. Examples include eliminating certain variables or conditions, altering values to simpler (usually whole) numbers, applying a <u>limiting case</u> (i.e. altering a variable to some extreme or ultimate value).
- For quantitative problems, identify the <u>real-world meaning</u> of all intermediate calculations: their units of measurement, where they fit into the scenario at hand. Annotate any diagrams or illustrations with these calculated values.
- For quantitative problems, try approaching it <u>qualitatively</u> instead, thinking in terms of "increase" and "decrease" rather than definite values.
- For qualitative problems, try approaching it <u>quantitatively</u> instead, proposing simple numerical values for the variables.
- Were there any <u>assumptions</u> you made while solving this problem? Would your solution change if one of those assumptions were altered?
- Identify where it would be easy for someone to go astray in attempting to solve this problem.
- Formulate your own problem based on what you learned solving this one.

General follow-up challenges for experiments or projects

- In what way(s) was this experiment or project <u>easy to complete?</u>
- Identify some of the <u>challenges you faced</u> in completing this experiment or project.

- Show how thorough documentation assisted in the completion of this experiment or project.
- Which <u>fundamental laws or principles</u> are key to this system's function?
- Identify any way(s) in which one might obtain <u>false or otherwise misleading measurements</u> from test equipment in this system.
- What will happen if (component X) fails (open/shorted/etc.)?
- What would have to occur to make this system <u>unsafe</u>?

4.1 Conceptual reasoning

These questions are designed to stimulate your analytic and synthetic thinking³. In a Socratic discussion with your instructor, the goal is for these questions to prompt an extended dialogue where assumptions are revealed, conclusions are tested, and understanding is sharpened. Your instructor may also pose additional questions based on those assigned, in order to further probe and refine your conceptual understanding.

Questions that follow are presented to challenge and probe your understanding of various concepts presented in the tutorial. These questions are intended to serve as a guide for the Socratic dialogue between yourself and the instructor. Your instructor's task is to ensure you have a sound grasp of these concepts, and the questions contained in this document are merely a means to this end. Your instructor may, at his or her discretion, alter or substitute questions for the benefit of tailoring the discussion to each student's needs. The only absolute requirement is that each student is challenged and assessed at a level equal to or greater than that represented by the documented questions.

It is far more important that you convey your reasoning than it is to simply convey a correct answer. For this reason, you should refrain from researching other information sources to answer questions. What matters here is that you are doing the thinking. If the answer is incorrect, your instructor will work with you to correct it through proper reasoning. A correct answer without an adequate explanation of how you derived that answer is unacceptable, as it does not aid the learning or assessment process.

You will note a conspicuous lack of answers given for these conceptual questions. Unlike standard textbooks where answers to every other question are given somewhere toward the back of the book, here in these learning modules students must rely on other means to check their work. The best way by far is to debate the answers with fellow students and also with the instructor during the Socratic dialogue sessions intended to be used with these learning modules. Reasoning through challenging questions with other people is an excellent tool for developing strong reasoning skills.

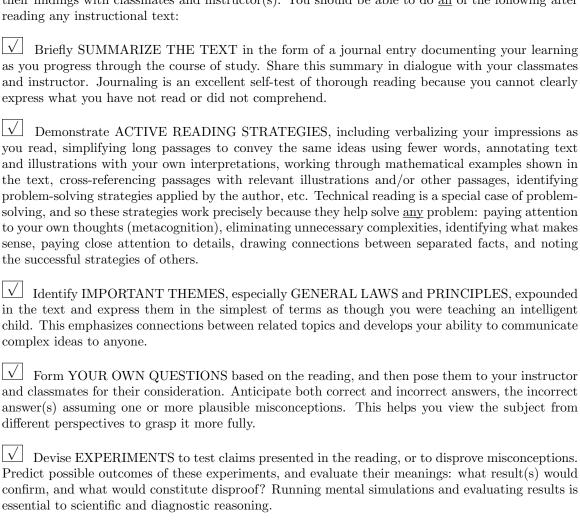
Another means of checking your conceptual answers, where applicable, is to use circuit simulation software to explore the effects of changes made to circuits. For example, if one of these conceptual questions challenges you to predict the effects of altering some component parameter in a circuit, you may check the validity of your work by simulating that same parameter change within software and seeing if the results agree.

³ Analytical thinking involves the "disassembly" of an idea into its constituent parts, analogous to dissection. Synthetic thinking involves the "assembly" of a new idea comprised of multiple concepts, analogous to construction. Both activities are high-level cognitive skills, extremely important for effective problem-solving, necessitating frequent challenge and regular practice to fully develop.

4.1.1 Reading outline and reflections

"Reading maketh a full man; conference a ready man; and writing an exact man" - Francis Bacon

Francis Bacon's advice is a blueprint for effective education: <u>reading</u> provides the learner with knowledge, <u>writing</u> focuses the learner's thoughts, and <u>critical dialogue</u> equips the learner to confidently communicate and apply their learning. Independent acquisition and application of knowledge is a powerful skill, well worth the effort to cultivate. To this end, students should read these educational resources closely, journal their own reflections on the reading, and discuss in detail their findings with classmates and instructor(s). You should be able to do <u>all</u> of the following after reading any instructional text:



Specifically identify any points you found CONFUSING. The reason for doing this is to help diagnose misconceptions and overcome barriers to learning.

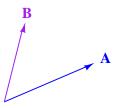
4.1.2 Foundational concepts

Correct analysis and diagnosis of electric circuits begins with a proper understanding of some basic concepts. The following is a list of some important concepts referenced in this module's full tutorial. Define each of them in your own words, and be prepared to illustrate each of these concepts with a description of a practical example and/or a live demonstration.

Polarity
Phasor
Vector
Phase angle
Complex numbers
Kirchhoff's Voltage Law
Kirchhoff's Current Law

4.1.3 Leading and lagging phasors

In this phasor diagram, determine which phasor (phase-vector) is *leading* and which is *lagging* the other:

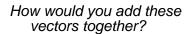


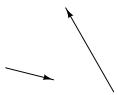
Challenges

• Using a protractor, estimate the amount of phase shift between these two phasors.

4.1.4 Adding two vectors

What does it mean to add two or more vectors together, in a geometric sense? How would one draw a vector diagram showing the following two vectors added together?





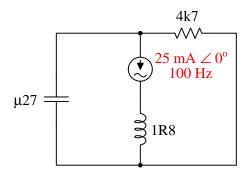
Challenges

• How would you verbally explain the process of phasor addition? If you were to describe to someone else how to add phasors together, what would you tell them?

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4.1.5 Explaining the meaning of calculations

Explain what each calculated value means in this circuit, identify its unit of measurement as well as any appropriate metric prefix(es), and identify the general principle used to compute it! Then, identify which of these calculations lend themselves to graphical expression in a phasor diagram:



1.
$$(2\pi)(100)(1.8) = 1130.98$$

2.
$$\frac{1}{(2\pi)(100)(0.27\times10^{-6})} = 5894.63$$

3.
$$\frac{1}{\frac{1}{4700 \angle 0^o} + \frac{1}{5894.63 \angle -90^o}} = 3674.85 \angle -38.57^o$$

4.
$$(3674.85 \angle -38.57^{\circ}) + 1130.98 \angle 90^{\circ} = 3098.64 \angle -21.99^{\circ}$$

5.
$$(25 \times 10^{-3} \angle 0^{\circ})(3098.64 \angle -21.99^{\circ}) = 77.4659 \angle -21.99^{\circ}$$

6.
$$(25 \times 10^{-3} \angle 0^{\circ})(1130.98 \angle 90^{\circ}) = 28.2743 \angle 90^{\circ}$$

7.
$$(25 \times 10^{-3} \angle 0^{\circ})(3674.85 \angle -38.57^{\circ}) = 91.8713 \angle -38.57^{\circ}$$

8.
$$(28.2743 \angle 90^{\circ}) + (91.8713 \angle -38.57^{\circ}) = 77.4659 \angle -21.99^{\circ}$$

9.
$$\frac{91.8713\angle -38.57^{\circ}}{5894.63\angle -90^{\circ}} = 15.5856 \times 10^{-3}\angle 51.43^{\circ}$$

10.
$$\frac{91.8713 \angle -38.57^{\circ}}{4700 \angle 0^{\circ}} = 19.5471 \times 10^{-3} \angle -38.57^{\circ}$$

11.
$$(15.5856 \times 10^{-3} \angle 51.43^{\circ}) + (19.5471 \times 10^{-3} \angle -38.57^{\circ}) = 25 \times 10^{-3} \angle 0^{\circ}$$

Challenges

- How does phasor multiplication affect the length and direction of the vector result?
- How does phasor division affect the length and direction of the vector result?

4.2 Quantitative reasoning

These questions are designed to stimulate your computational thinking. In a Socratic discussion with your instructor, the goal is for these questions to reveal your mathematical approach(es) to problem-solving so that good technique and sound reasoning may be reinforced. Your instructor may also pose additional questions based on those assigned, in order to observe your problem-solving firsthand.

Mental arithmetic and estimations are strongly encouraged for all calculations, because without these abilities you will be unable to readily detect errors caused by calculator misuse (e.g. keystroke errors).

You will note a conspicuous lack of answers given for these quantitative questions. Unlike standard textbooks where answers to every other question are given somewhere toward the back of the book, here in these learning modules students must rely on other means to check their work. My advice is to use circuit simulation software such as SPICE to check the correctness of quantitative answers. Refer to those learning modules within this collection focusing on SPICE to see worked examples which you may use directly as practice problems for your own study, and/or as templates you may modify to run your own analyses and generate your own practice problems.

Completely worked example problems found in the Tutorial may also serve as "test cases⁴" for gaining proficiency in the use of circuit simulation software, and then once that proficiency is gained you will never need to rely⁵ on an answer key!

⁴In other words, set up the circuit simulation software to analyze the same circuit examples found in the Tutorial. If the simulated results match the answers shown in the Tutorial, it confirms the simulation has properly run. If the simulated results disagree with the Tutorial's answers, something has been set up incorrectly in the simulation software. Using every Tutorial as practice in this way will quickly develop proficiency in the use of circuit simulation software.

⁵This approach is perfectly in keeping with the instructional philosophy of these learning modules: teaching students to be self-sufficient thinkers. Answer keys can be useful, but it is even more useful to your long-term success to have a set of tools on hand for checking your own work, because once you have left school and are on your own, there will no longer be "answer keys" available for the problems you will have to solve.

4.2.1 Miscellaneous physical constants

Note: constants shown in **bold** type are *exact*, not approximations. Values inside of parentheses show one standard deviation (σ) of uncertainty in the final digits: for example, the magnetic permeability of free space value given as $1.25663706212(19) \times 10^{-6}$ H/m represents a center value (i.e. the location parameter) of $1.25663706212 \times 10^{-6}$ Henrys per meter with one standard deviation of uncertainty equal to $0.000000000000019 \times 10^{-6}$ Henrys per meter.

Avogadro's number $(N_A) = 6.02214076 \times 10^{23} \text{ per mole } (\text{mol}^{-1})$

Boltzmann's constant $(k) = 1.380649 \times 10^{-23}$ Joules per Kelvin (J/K)

Electronic charge $(e) = 1.602176634 \times 10^{-19}$ Coulomb (C)

Faraday constant $(F) = 96,485.33212... \times 10^4$ Coulombs per mole (C/mol)

Magnetic permeability of free space $(\mu_0) = 1.25663706212(19) \times 10^{-6}$ Henrys per meter (H/m)

Electric permittivity of free space $(\epsilon_0) = 8.8541878128(13) \times 10^{-12}$ Farads per meter (F/m)

Characteristic impedance of free space $(Z_0) = 376.730313668(57)$ Ohms (Ω)

Gravitational constant (G) = 6.67430(15) \times 10⁻¹¹ cubic meters per kilogram-seconds squared (m³/kg-s²)

Molar gas constant (R) = 8.314462618... Joules per mole-Kelvin (J/mol-K) = 0.08205746(14) liters-atmospheres per mole-Kelvin

Planck constant $(h) = 6.62607015 \times 10^{-34}$ joule-seconds (J-s)

Stefan-Boltzmann constant (σ) = **5.670374419...** \times 10⁻⁸ Watts per square meter-Kelvin⁴ (W/m²·K⁴)

Speed of light in a vacuum (c) = 299,792,458 meters per second (m/s) = 186282.4 miles per second (mi/s)

Note: All constants taken from NIST data "Fundamental Physical Constants – Complete Listing", from http://physics.nist.gov/constants, National Institute of Standards and Technology (NIST), 2018 CODATA Adjustment.

4.2.2 Introduction to spreadsheets

A powerful computational tool you are encouraged to use in your work is a *spreadsheet*. Available on most personal computers (e.g. Microsoft Excel), *spreadsheet* software performs numerical calculations based on number values and formulae entered into cells of a grid. This grid is typically arranged as lettered columns and numbered rows, with each cell of the grid identified by its column/row coordinates (e.g. cell B3, cell A8). Each cell may contain a string of text, a number value, or a mathematical formula. The spreadsheet automatically updates the results of all mathematical formulae whenever the entered number values are changed. This means it is possible to set up a spreadsheet to perform a series of calculations on entered data, and those calculations will be re-done by the computer any time the data points are edited in any way.

For example, the following spreadsheet calculates average speed based on entered values of distance traveled and time elapsed:

	A	В	C	D
1	Distance traveled	46.9	Kilometers	
2	Time elapsed	1.18	Hours	
3	Average speed	= B1 / B2	km/h	
4				
5				

Text labels contained in cells A1 through A3 and cells C1 through C3 exist solely for readability and are not involved in any calculations. Cell B1 contains a sample distance value while cell B2 contains a sample time value. The formula for computing speed is contained in cell B3. Note how this formula begins with an "equals" symbol (=), references the values for distance and speed by lettered column and numbered row coordinates (B1 and B2), and uses a forward slash symbol for division (/). The coordinates B1 and B2 function as *variables* 6 would in an algebraic formula.

When this spreadsheet is executed, the numerical value 39.74576 will appear in cell B3 rather than the formula = B1 / B2, because 39.74576 is the computed speed value given 46.9 kilometers traveled over a period of 1.18 hours. If a different numerical value for distance is entered into cell B1 or a different value for time is entered into cell B2, cell B3's value will automatically update. All you need to do is set up the given values and any formulae into the spreadsheet, and the computer will do all the calculations for you.

Cell B3 may be referenced by other formulae in the spreadsheet if desired, since it is a variable just like the given values contained in B1 and B2. This means it is possible to set up an entire chain of calculations, one dependent on the result of another, in order to arrive at a final value. The arrangement of the given data and formulae need not follow any pattern on the grid, which means you may place them anywhere.

⁶Spreadsheets may also provide means to attach text labels to cells for use as variable names (Microsoft Excel simply calls these labels "names"), but for simple spreadsheets such as those shown here it's usually easier just to use the standard coordinate naming for each cell.

Common⁷ arithmetic operations available for your use in a spreadsheet include the following:

- Addition (+)
- Subtraction (-)
- Multiplication (*)
- Division (/)
- Powers (^)
- Square roots (sqrt())
- Logarithms (ln(), log10())

Parentheses may be used to ensure⁸ proper order of operations within a complex formula. Consider this example of a spreadsheet implementing the *quadratic formula*, used to solve for roots of a polynomial expression in the form of $ax^2 + bx + c$:

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

	A	В
1	x_1	= (-B4 + sqrt((B4^2) - (4*B3*B5))) / (2*B3)
2	x_2	= (-B4 - sqrt((B4^2) - (4*B3*B5))) / (2*B3)
3	a =	9
4	b =	5
5	C =	-2

This example is configured to compute roots⁹ of the polynomial $9x^2 + 5x - 2$ because the values of 9, 5, and -2 have been inserted into cells B3, B4, and B5, respectively. Once this spreadsheet has been built, though, it may be used to calculate the roots of any second-degree polynomial expression simply by entering the new a, b, and c coefficients into cells B3 through B5. The numerical values appearing in cells B1 and B2 will be automatically updated by the computer immediately following any changes made to the coefficients.

⁷Modern spreadsheet software offers a bewildering array of mathematical functions you may use in your computations. I recommend you consult the documentation for your particular spreadsheet for information on operations other than those listed here.

⁸Spreadsheet programs, like text-based programming languages, are designed to follow standard order of operations by default. However, my personal preference is to use parentheses even where strictly unnecessary just to make it clear to any other person viewing the formula what the intended order of operations is.

⁹Reviewing some algebra here, a *root* is a value for x that yields an overall value of zero for the polynomial. For this polynomial $(9x^2+5x-2)$ the two roots happen to be x=0.269381 and x=-0.82494, with these values displayed in cells B1 and B2, respectively upon execution of the spreadsheet.

Alternatively, one could break up the long quadratic formula into smaller pieces like this:

$$y = \sqrt{b^2 - 4ac} \qquad z = 2a$$
$$x = \frac{-b \pm y}{z}$$

	A	В	C
1	x_1	= (-B4 + C1) / C2	= sqrt((B4^2) - (4*B3*B5))
2	x_2	= (-B4 - C1) / C2	= 2*B3
3	a =	9	
4	b =	5	
5	C =	-2	

Note how the square-root term (y) is calculated in cell C1, and the denominator term (z) in cell C2. This makes the two final formulae (in cells B1 and B2) simpler to interpret. The positioning of all these cells on the grid is completely arbitrary¹⁰ – all that matters is that they properly reference each other in the formulae.

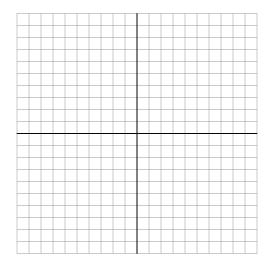
Spreadsheets are particularly useful for situations where the same set of calculations representing a circuit or other system must be repeated for different initial conditions. The power of a spreadsheet is that it automates what would otherwise be a tedious set of calculations. One specific application of this is to simulate the effects of various components within a circuit failing with abnormal values (e.g. a shorted resistor simulated by making its value nearly zero; an open resistor simulated by making its value extremely large). Another application is analyzing the behavior of a circuit design given new components that are out of specification, and/or aging components experiencing drift over time.

¹⁰My personal preference is to locate all the "given" data in the upper-left cells of the spreadsheet grid (each data point flanked by a sensible name in the cell to the left and units of measurement in the cell to the right as illustrated in the first distance/time spreadsheet example), sometimes coloring them in order to clearly distinguish which cells contain entered data versus which cells contain computed results from formulae. I like to place all formulae in cells below the given data, and try to arrange them in logical order so that anyone examining my spreadsheet will be able to figure out how I constructed a solution. This is a general principle I believe all computer programmers should follow: document and arrange your code to make it easy for other people to learn from it.

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4.2.3 Polar and rectangular forms

Sketch the phasor 5+j3 in a phasor diagram, showing how its rectangular components (i.e. 5 and j3) relate to the diagram, as well as its polar equivalent:

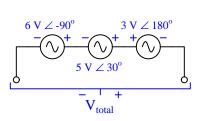


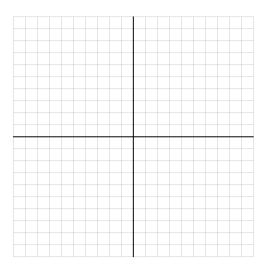
Challenges

- How do we convert a rectangular-format complex number into polar-format, using just trigonometric functions?
- How do we convert a polar-format complex number into rectangular-format?

4.2.4 Three series voltage sources

Sketch a phasor diagram showing vectors representing each of the three voltage sources as well as the resultant (total) voltage, and also use a calculator to compute V_{total} :





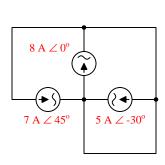
Challenges

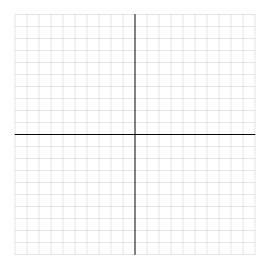
• Suppose the polarity of V_{total} was specified with + on left and - on right. How would this affect the phasor diagram, and the calculated voltage value?

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4.2.5 Three parallel current sources

Sketch a phasor diagram showing vectors representing each of the three current sources as well as the resultant (total) current, and also use a calculator to compute I_{total} :





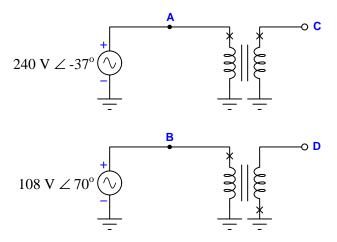
Also, sketch the location in this network where you would actually measure this I_{total} .

Challenges

• Why is it important that we know all these AC sources are at the exact same frequency?

4.2.6 Transformer effect on phasors

Calculate V_{AB} and V_{CD} in this circuit and sketch phasor diagrams for these voltages, assuming both sources and transformers share a common ground and that both transformers have 1:1 winding ratios:



Hint – since both transformers have a 1:1 turns ratio, the secondary voltage must be identical to the primary voltage for each one. This means the phasor representing a transformer's secondary winding voltage must be exactly the same length and have exactly the same angle as the phasor representing that same transformer's primary voltage. Treat each phasor as a line segment you are free to move around so long as you do not alter its length or direction, and you can see how they "stack up" onto each other according to how the windings are electrically connected to form a complete phasor diagram.

Challenges

- How would your phasor diagrams be different if the winding ratios were not 1:1?
- Calculate V_{AC} .
- Calculate V_{BD} .
- Predict the effects of the upper transformer's primary winding failing open on the phasor diagram.

4.3 Diagnostic reasoning

These questions are designed to stimulate your deductive and inductive thinking, where you must apply general principles to specific scenarios (deductive) and also derive conclusions about the failed circuit from specific details (inductive). In a Socratic discussion with your instructor, the goal is for these questions to reinforce your recall and use of general circuit principles and also challenge your ability to integrate multiple symptoms into a sensible explanation of what's wrong in a circuit. Your instructor may also pose additional questions based on those assigned, in order to further challenge and sharpen your diagnostic abilities.

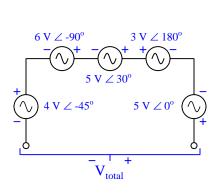
As always, your goal is to fully *explain* your analysis of each problem. Simply obtaining a correct answer is not good enough – you must also demonstrate sound reasoning in order to successfully complete the assignment. Your instructor's responsibility is to probe and challenge your understanding of the relevant principles and analytical processes in order to ensure you have a strong foundation upon which to build further understanding.

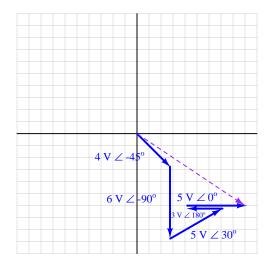
You will note a conspicuous lack of answers given for these diagnostic questions. Unlike standard textbooks where answers to every other question are given somewhere toward the back of the book, here in these learning modules students must rely on other means to check their work. The best way by far is to debate the answers with fellow students and also with the instructor during the Socratic dialogue sessions intended to be used with these learning modules. Reasoning through challenging questions with other people is an excellent tool for developing strong reasoning skills.

Another means of checking your diagnostic answers, where applicable, is to use circuit simulation software to explore the effects of faults placed in circuits. For example, if one of these diagnostic questions requires that you predict the effect of an open or a short in a circuit, you may check the validity of your work by simulating that same fault (substituting a very high resistance in place of that component for an open, and substituting a very low resistance for a short) within software and seeing if the results agree.

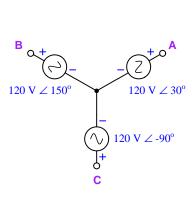
4.3.1 Find the mistakes

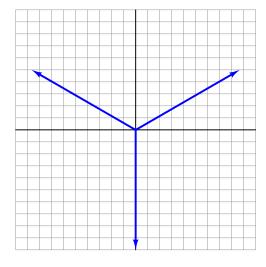
Explain what is wrong with this phasor diagram as it relates to the circuit:





Next, explain what is wrong with this student's calculated voltage between nodes A and B:





Student's incorrect result: $V_{AB}=120$ Volts $\angle~90^o$

Challenges

• What fundamental principle(s) were overlooked in these mistakes.

Appendix A

Problem-Solving Strategies

The ability to solve complex problems is arguably one of the most valuable skills one can possess, and this skill is particularly important in any science-based discipline.

- <u>Study principles, not procedures.</u> Don't be satisfied with merely knowing how to compute solutions learn *why* those solutions work.
- <u>Identify</u> what it is you need to solve, <u>identify</u> all relevant data, <u>identify</u> all units of measurement, <u>identify</u> any general principles or formulae linking the given information to the solution, and then <u>identify</u> any "missing pieces" to a solution. <u>Annotate</u> all diagrams with this data.
- <u>Sketch a diagram</u> to help visualize the problem. When building a real system, always devise a plan for that system and analyze its function *before* constructing it.
- Follow the units of measurement and meaning of every calculation. If you are ever performing mathematical calculations as part of a problem-solving procedure, and you find yourself unable to apply each and every intermediate result to some aspect of the problem, it means you don't understand what you are doing. Properly done, every mathematical result should have practical meaning for the problem, and not just be an abstract number. You should be able to identify the proper units of measurement for each and every calculated result, and show where that result fits into the problem.
- <u>Perform "thought experiments"</u> to explore the effects of different conditions for theoretical problems. When troubleshooting real systems, perform *diagnostic tests* rather than visually inspecting for faults, the best diagnostic test being the one giving you the most information about the nature and/or location of the fault with the fewest steps.
- <u>Simplify the problem</u> until the solution becomes obvious, and then use that obvious case as a model to follow in solving the more complex version of the problem.
- <u>Check for exceptions</u> to see if your solution is incorrect or incomplete. A good solution will work for *all* known conditions and criteria. A good example of this is the process of testing scientific hypotheses: the task of a scientist is not to find support for a new idea, but rather to *challenge* that new idea to see if it holds up under a battery of tests. The philosophical

principle of *reductio ad absurdum* (i.e. disproving a general idea by finding a specific case where it fails) is useful here.

- Work "backward" from a hypothetical solution to a new set of given conditions.
- <u>Add quantities</u> to problems that are qualitative in nature, because sometimes a little math helps illuminate the scenario.
- <u>Sketch graphs</u> illustrating how variables relate to each other. These may be quantitative (i.e. with realistic number values) or qualitative (i.e. simply showing increases and decreases).
- Treat quantitative problems as qualitative in order to discern the relative magnitudes and/or directions of change of the relevant variables. For example, try determining what happens if a certain variable were to increase or decrease before attempting to precisely calculate quantities: how will each of the dependent variables respond, by increasing, decreasing, or remaining the same as before?
- <u>Consider limiting cases</u>. This works especially well for qualitative problems where you need to determine which direction a variable will change. Take the given condition and magnify that condition to an extreme degree as a way of simplifying the direction of the system's response.
- <u>Check your work.</u> This means regularly testing your conclusions to see if they make sense. This does *not* mean repeating the same steps originally used to obtain the conclusion(s), but rather to use some other means to check validity. Simply repeating procedures often leads to repeating the same errors if any were made, which is why alternative paths are better.

Appendix B

Instructional philosophy

"The unexamined circuit is not worth energizing" - Socrates (if he had taught electricity)

These learning modules, although useful for self-study, were designed to be used in a formal learning environment where a subject-matter expert challenges students to digest the content and exercise their critical thinking abilities in the answering of questions and in the construction and testing of working circuits.

The following principles inform the instructional and assessment philosophies embodied in these learning modules:

- The first goal of education is to enhance clear and independent thought, in order that every student reach their fullest potential in a highly complex and inter-dependent world. Robust reasoning is *always* more important than particulars of any subject matter, because its application is universal.
- Literacy is fundamental to independent learning and thought because text continues to be the most efficient way to communicate complex ideas over space and time. Those who cannot read with ease are limited in their ability to acquire knowledge and perspective.
- Articulate communication is fundamental to work that is complex and interdisciplinary.
- Faulty assumptions and poor reasoning are best corrected through challenge, not presentation. The rhetorical technique of *reductio ad absurdum* (disproving an assertion by exposing an absurdity) works well to discipline student's minds, not only to correct the problem at hand but also to learn how to detect and correct future errors.
- Important principles should be repeatedly explored and widely applied throughout a course of study, not only to reinforce their importance and help ensure their mastery, but also to showcase the interconnectedness and utility of knowledge.

These learning modules were expressly designed to be used in an "inverted" teaching environment where students first read the introductory and tutorial chapters on their own, then individually attempt to answer the questions and construct working circuits according to the experiment and project guidelines. The instructor never lectures, but instead meets regularly with each individual student to review their progress, answer questions, identify misconceptions, and challenge the student to new depths of understanding through further questioning. Regular meetings between instructor and student should resemble a Socratic dialogue, where questions serve as scalpels to dissect topics and expose assumptions. The student passes each module only after consistently demonstrating their ability to logically analyze and correctly apply all major concepts in each question or project/experiment. The instructor must be vigilant in probing each student's understanding to ensure they are truly reasoning and not just memorizing. This is why "Challenge" points appear throughout, as prompts for students to think deeper about topics and as starting points for instructor queries. Sometimes these challenge points require additional knowledge that hasn't been covered in the series to answer in full. This is okay, as the major purpose of the Challenges is to stimulate analysis and synthesis on the part of each student.

The instructor must possess enough mastery of the subject matter and awareness of students' reasoning to generate their own follow-up questions to practically any student response. Even completely correct answers given by the student should be challenged by the instructor for the purpose of having students practice articulating their thoughts and defending their reasoning. Conceptual errors committed by the student should be exposed and corrected not by direct instruction, but rather by reducing the errors to an absurdity³ through well-chosen questions and thought experiments posed by the instructor. Becoming proficient at this style of instruction requires time and dedication, but the positive effects on critical thinking for both student and instructor are spectacular.

An inspection of these learning modules reveals certain unique characteristics. One of these is a bias toward thorough explanations in the tutorial chapters. Without a live instructor to explain concepts and applications to students, the text itself must fulfill this role. This philosophy results in lengthier explanations than what you might typically find in a textbook, each step of the reasoning process fully explained, including footnotes addressing common questions and concerns students raise while learning these concepts. Each tutorial seeks to not only explain each major concept in sufficient detail, but also to explain the logic of each concept and how each may be developed

¹In a traditional teaching environment, students first encounter new information via *lecture* from an expert, and then independently apply that information via *homework*. In an "inverted" course of study, students first encounter new information via *homework*, and then independently apply that information under the scrutiny of an expert. The expert's role in lecture is to simply *explain*, but the expert's role in an inverted session is to *challenge*, *critique*, and if necessary *explain* where gaps in understanding still exist.

²Socrates is a figure in ancient Greek philosophy famous for his unflinching style of questioning. Although he authored no texts, he appears as a character in Plato's many writings. The essence of Socratic philosophy is to leave no question unexamined and no point of view unchallenged. While purists may argue a topic such as electric circuits is too narrow for a true Socratic-style dialogue, I would argue that the essential thought processes involved with scientific reasoning on any topic are not far removed from the Socratic ideal, and that students of electricity and electronics would do very well to challenge assumptions, pose thought experiments, identify fallacies, and otherwise employ the arsenal of critical thinking skills modeled by Socrates.

³This rhetorical technique is known by the Latin phrase *reductio ad absurdum*. The concept is to expose errors by counter-example, since only one solid counter-example is necessary to disprove a universal claim. As an example of this, consider the common misconception among beginning students of electricity that voltage cannot exist without current. One way to apply *reductio ad absurdum* to this statement is to ask how much current passes through a fully-charged battery connected to nothing (i.e. a clear example of voltage existing without current).

from "first principles". Again, this reflects the goal of developing clear and independent thought in students' minds, by showing how clear and logical thought was used to forge each concept. Students benefit from witnessing a model of clear thinking in action, and these tutorials strive to be just that.

Another characteristic of these learning modules is a lack of step-by-step instructions in the Project and Experiment chapters. Unlike many modern workbooks and laboratory guides where step-by-step instructions are prescribed for each experiment, these modules take the approach that students must learn to closely read the tutorials and apply their own reasoning to identify the appropriate experimental steps. Sometimes these steps are plainly declared in the text, just not as a set of enumerated points. At other times certain steps are implied, an example being assumed competence in test equipment use where the student should not need to be told again how to use their multimeter because that was thoroughly explained in previous lessons. In some circumstances no steps are given at all, leaving the entire procedure up to the student.

This lack of prescription is not a flaw, but rather a feature. Close reading and clear thinking are foundational principles of this learning series, and in keeping with this philosophy all activities are designed to require those behaviors. Some students may find the lack of prescription frustrating, because it demands more from them than what their previous educational experiences required. This frustration should be interpreted as an unfamiliarity with autonomous thinking, a problem which must be corrected if the student is ever to become a self-directed learner and effective problem-solver. Ultimately, the need for students to read closely and think clearly is more important both in the near-term and far-term than any specific facet of the subject matter at hand. If a student takes longer than expected to complete a module because they are forced to outline, digest, and reason on their own, so be it. The future gains enjoyed by developing this mental discipline will be well worth the additional effort and delay.

Another feature of these learning modules is that they do not treat topics in isolation. Rather, important concepts are introduced early in the series, and appear repeatedly as stepping-stones toward other concepts in subsequent modules. This helps to avoid the "compartmentalization" of knowledge, demonstrating the inter-connectedness of concepts and simultaneously reinforcing them. Each module is fairly complete in itself, reserving the beginning of its tutorial to a review of foundational concepts.

This methodology of assigning text-based modules to students for digestion and then using Socratic dialogue to assess progress and hone students' thinking was developed over a period of several years by the author with his Electronics and Instrumentation students at the two-year college level. While decidedly unconventional and sometimes even unsettling for students accustomed to a more passive lecture environment, this instructional philosophy has proven its ability to convey conceptual mastery, foster careful analysis, and enhance employability so much better than lecture that the author refuses to ever teach by lecture again.

Problems which often go undiagnosed in a lecture environment are laid bare in this "inverted" format where students must articulate and logically defend their reasoning. This, too, may be unsettling for students accustomed to lecture sessions where the instructor cannot tell for sure who comprehends and who does not, and this vulnerability necessitates sensitivity on the part of the "inverted" session instructor in order that students never feel discouraged by having their errors exposed. Everyone makes mistakes from time to time, and learning is a lifelong process! Part of the instructor's job is to build a culture of learning among the students where errors are not seen as shameful, but rather as opportunities for progress.

To this end, instructors managing courses based on these modules should adhere to the following principles:

- Student questions are always welcome and demand thorough, honest answers. The only type of question an instructor should refuse to answer is one the student should be able to easily answer on their own. Remember, the fundamental goal of education is for each student to learn to think clearly and independently. This requires hard work on the part of the student, which no instructor should ever circumvent. Anything done to bypass the student's responsibility to do that hard work ultimately limits that student's potential and thereby does real harm.
- It is not only permissible, but encouraged, to answer a student's question by asking questions in return, these follow-up questions designed to guide the student to reach a correct answer through their own reasoning.
- All student answers demand to be challenged by the instructor and/or by other students. This includes both correct and incorrect answers the goal is to practice the articulation and defense of one's own reasoning.
- No reading assignment is deemed complete unless and until the student demonstrates their ability to accurately summarize the major points in their own terms. Recitation of the original text is unacceptable. This is why every module contains an "Outline and reflections" question as well as a "Foundational concepts" question in the Conceptual reasoning section, to prompt reflective reading.
- No assigned question is deemed answered unless and until the student demonstrates their ability to consistently and correctly apply the concepts to *variations* of that question. This is why module questions typically contain multiple "Challenges" suggesting different applications of the concept(s) as well as variations on the same theme(s). Instructors are encouraged to devise as many of their own "Challenges" as they are able, in order to have a multitude of ways ready to probe students' understanding.
- No assigned experiment or project is deemed complete unless and until the student demonstrates the task in action. If this cannot be done "live" before the instructor, videorecordings showing the demonstration are acceptable. All relevant safety precautions must be followed, all test equipment must be used correctly, and the student must be able to properly explain all results. The student must also successfully answer all Challenges presented by the instructor for that experiment or project.

Students learning from these modules would do well to abide by the following principles:

- No text should be considered fully and adequately read unless and until you can express every idea in your own words, using your own examples.
- You should always articulate your thoughts as you read the text, noting points of agreement, confusion, and epiphanies. Feel free to print the text on paper and then write your notes in the margins. Alternatively, keep a journal for your own reflections as you read. This is truly a helpful tool when digesting complicated concepts.
- Never take the easy path of highlighting or underlining important text. Instead, *summarize* and/or *comment* on the text using your own words. This actively engages your mind, allowing you to more clearly perceive points of confusion or misunderstanding on your own.
- A very helpful strategy when learning new concepts is to place yourself in the role of a teacher, if only as a mental exercise. Either explain what you have recently learned to someone else, or at least *imagine* yourself explaining what you have learned to someone else. The simple act of having to articulate new knowledge and skill forces you to take on a different perspective, and will help reveal weaknesses in your understanding.
- Perform each and every mathematical calculation and thought experiment shown in the text on your own, referring back to the text to see that your results agree. This may seem trivial and unnecessary, but it is critically important to ensuring you actually understand what is presented, especially when the concepts at hand are complicated and easy to misunderstand. Apply this same strategy to become proficient in the use of *circuit simulation software*, checking to see if your simulated results agree with the results shown in the text.
- Above all, recognize that learning is hard work, and that a certain level of frustration is unavoidable. There are times when you will struggle to grasp some of these concepts, and that struggle is a natural thing. Take heart that it will yield with persistent and varied⁴ effort, and never give up!

Students interested in using these modules for self-study will also find them beneficial, although the onus of responsibility for thoroughly reading and answering questions will of course lie with that individual alone. If a qualified instructor is not available to challenge students, a workable alternative is for students to form study groups where they challenge⁵ one another.

To high standards of education,

Tony R. Kuphaldt

⁴As the old saying goes, "Insanity is trying the same thing over and over again, expecting different results." If you find yourself stumped by something in the text, you should attempt a different approach. Alter the thought experiment, change the mathematical parameters, do whatever you can to see the problem in a slightly different light, and then the solution will often present itself more readily.

⁵Avoid the temptation to simply share answers with study partners, as this is really counter-productive to learning. Always bear in mind that the answer to any question is far less important in the long run than the method(s) used to obtain that answer. The goal of education is to empower one's life through the improvement of clear and independent thought, literacy, expression, and various practical skills.

Appendix C

Tools used

I am indebted to the developers of many open-source software applications in the creation of these learning modules. The following is a list of these applications with some commentary on each.

You will notice a theme common to many of these applications: a bias toward *code*. Although I am by no means an expert programmer in any computer language, I understand and appreciate the flexibility offered by code-based applications where the user (you) enters commands into a plain ASCII text file, which the software then reads and processes to create the final output. Code-based computer applications are by their very nature *extensible*, while WYSIWYG (What You See Is What You Get) applications are generally limited to whatever user interface the developer makes for you.

The GNU/Linux computer operating system

There is so much to be said about Linus Torvalds' Linux and Richard Stallman's GNU project. First, to credit just these two individuals is to fail to do justice to the *mob* of passionate volunteers who contributed to make this amazing software a reality. I first learned of Linux back in 1996, and have been using this operating system on my personal computers almost exclusively since then. It is *free*, it is completely *configurable*, and it permits the continued use of highly efficient Unix applications and scripting languages (e.g. shell scripts, Makefiles, sed, awk) developed over many decades. Linux not only provided me with a powerful computing platform, but its open design served to inspire my life's work of creating open-source educational resources.

Bram Moolenaar's Vim text editor

Writing code for any code-based computer application requires a *text editor*, which may be thought of as a word processor strictly limited to outputting plain-ASCII text files. Many good text editors exist, and one's choice of text editor seems to be a deeply personal matter within the programming world. I prefer Vim because it operates very similarly to vi which is ubiquitous on Unix/Linux operating systems, and because it may be entirely operated via keyboard (i.e. no mouse required) which makes it fast to use.

Donald Knuth's T_FX typesetting system

Developed in the late 1970's and early 1980's by computer scientist extraordinaire Donald Knuth to typeset his multi-volume magnum opus The Art of Computer Programming, this software allows the production of formatted text for screen-viewing or paper printing, all by writing plain-text code to describe how the formatted text is supposed to appear. T_FX is not just a markup language for documents, but it is also a Turing-complete programming language in and of itself, allowing useful algorithms to be created to control the production of documents. Simply put, TFX is a programmer's approach to word processing. Since T_FX is controlled by code written in a plain-text file, this means anyone may read that plain-text file to see exactly how the document was created. This openness afforded by the code-based nature of T_FX makes it relatively easy to learn how other people have created their own T_FX documents. By contrast, examining a beautiful document created in a conventional WYSIWYG word processor such as Microsoft Word suggests nothing to the reader about how that document was created, or what the user might do to create something similar. As Mr. Knuth himself once quipped, conventional word processing applications should be called WYSIAYG (What You See Is All You Get).

Leslie Lamport's LATEX extensions to TEX

Like all true programming languages, TEX is inherently extensible. So, years after the release of TEX to the public, Leslie Lamport decided to create a massive extension allowing easier compilation of book-length documents. The result was LATEX, which is the markup language used to create all ModEL module documents. You could say that TEX is to LATEX as C is to C++. This means it is permissible to use any and all TEX commands within LATEX source code, and it all still works. Some of the features offered by LATEX that would be challenging to implement in TEX include automatic index and table-of-content creation.

Tim Edwards' Xcircuit drafting program

This wonderful program is what I use to create all the schematic diagrams and illustrations (but not photographic images or mathematical plots) throughout the ModEL project. It natively outputs PostScript format which is a true vector graphic format (this is why the images do not pixellate when you zoom in for a closer view), and it is so simple to use that I have never had to read the manual! Object libraries are easy to create for <code>Xcircuit</code>, being plain-text files using PostScript programming conventions. Over the years I have collected a large set of object libraries useful for drawing electrical and electronic schematics, pictorial diagrams, and other technical illustrations.

Gimp graphic image manipulation program

Essentially an open-source clone of Adobe's PhotoShop, I use Gimp to resize, crop, and convert file formats for all of the photographic images appearing in the ModEL modules. Although Gimp does offer its own scripting language (called Script-Fu), I have never had occasion to use it. Thus, my utilization of Gimp to merely crop, resize, and convert graphic images is akin to using a sword to slice bread.

SPICE circuit simulation program

SPICE is to circuit analysis as TEX is to document creation: it is a form of markup language designed to describe a certain object to be processed in plain-ASCII text. When the plain-text "source file" is compiled by the software, it outputs the final result. More modern circuit analysis tools certainly exist, but I prefer SPICE for the following reasons: it is *free*, it is *fast*, it is *reliable*, and it is a fantastic tool for *teaching* students of electricity and electronics how to write simple code. I happen to use rather old versions of SPICE, version 2g6 being my "go to" application when I only require text-based output. NGSPICE (version 26), which is based on Berkeley SPICE version 3f5, is used when I require graphical output for such things as time-domain waveforms and Bode plots. In all SPICE example netlists I strive to use coding conventions compatible with all SPICE versions.

Andrew D. Hwang's ePiX mathematical visualization programming library

This amazing project is a C++ library you may link to any C/C++ code for the purpose of generating PostScript graphic images of mathematical functions. As a completely free and open-source project, it does all the plotting I would otherwise use a Computer Algebra System (CAS) such as Mathematica or Maple to do. It should be said that ePiX is not a Computer Algebra System like Mathematica or Maple, but merely a mathematical visualization tool. In other words, it won't determine integrals for you (you'll have to implement that in your own C/C++ code!), but it can graph the results, and it does so beautifully. What I really admire about ePiX is that it is a C++ programming library, which means it builds on the existing power and toolset available with that programming language. Mr. Hwang could have probably developed his own stand-alone application for mathematical plotting, but by creating a C++ library to do the same thing he accomplished something much greater.

gnuplot mathematical visualization software

Another open-source tool for mathematical visualization is gnuplot. Interestingly, this tool is not part of Richard Stallman's GNU project, its name being a coincidence. For this reason the authors prefer "gnu" not be capitalized at all to avoid confusion. This is a much "lighter-weight" alternative to a spreadsheet for plotting tabular data, and the fact that it easily outputs directly to an X11 console or a file in a number of different graphical formats (including PostScript) is very helpful. I typically set my gnuplot output format to default (X11 on my Linux PC) for quick viewing while I'm developing a visualization, then switch to PostScript file export once the visual is ready to include in the document(s) I'm writing. As with my use of Gimp to do rudimentary image editing, my use of gnuplot only scratches the surface of its capabilities, but the important points are that it's free and that it works well.

Python programming language

Both Python and C++ find extensive use in these modules as instructional aids and exercises, but I'm listing Python here as a tool for myself because I use it almost daily as a calculator. If you open a Python interpreter console and type from math import * you can type mathematical expressions and have it return results just as you would on a hand calculator. Complex-number (i.e. phasor) arithmetic is similarly supported if you include the complex-math library (from cmath import *). Examples of this are shown in the Programming References chapter (if included) in each module. Of course, being a fully-featured programming language, Python also supports conditionals, loops, and other structures useful for calculation of quantities. Also, running in a console environment where all entries and returned values show as text in a chronologically-ordered list makes it easy to copy-and-paste those calculations to document exactly how they were performed.

Appendix D

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Appendix E

Version history

This is a list showing all significant additions, corrections, and other edits made to this learning module. Each entry is referenced by calendar date in reverse chronological order (newest version first), which appears on the front cover of every learning module for easy reference. Any contributors to this open-source document are listed here as well.

- **27 September 2024** divided the Introduction chapter into sections, one with recommendations for students, one with a listing of challenging concepts, and one with recommendations for instructors.
- 9 February 2024 divided Tutorial chapter into sections to make this module more searchable.
- **22 June 2023** added a requirement in the "Explaining the meaning of calculations" Conceptual Question to also express each quantity using appropriate metric prefixes.
- **6-7** Mar 2023 corrected a typographical error spotted by Jessica Smith in the "Explaining the meaning of calculations" Conceptual Reasoning question. Also added more questions to the Introduction chapter and made minor edits to the Tutorial for readability.
- 8 May 2021 commented out or deleted empty chapters.
- **8-9 March 2021** added some instructor notes, and made minor edits to the Tutorial. Also added a new Case Tutorial chapter with sections showing phasor diagrams for four different AC circuits.
- **7 February 2021** significantly edited the Introduction chapter to make it more suitable as a pre-study guide and to provide cues useful to instructors leading "inverted" teaching sessions.
- **7-9 January 2021** added content to the Tutorial, as well as questions.
- 6 January 2021 made the Simplified Tutorial into the one and only Tutorial chapter.
- August 2018 content added to the Introduction.
- May 2018 document first created.

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